

Theoretical Aspects of Higgs Physics

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- Higgs phenomenon
- Unitarity, vacuum stability ...
- Why $N^i LO$ for Higgs
- Higgs with Jets, tops
- Higgs Characterisation
- Conclusion

What is next at LHC, TIFR, Jan 6-9, 2014.

Scalar field and Yukawa sectors in the SM

- Gauge principle in Quantum field theory provides framework to study interaction of elementary particles
- Gauge symmetry severely constraints the mass terms of gauge fields and matter fields.
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- The $SU(2)_L \times U(1)_Y$ invariant Yukawa interaction Lagrangian is given by

$$\mathcal{L}_Y = Y_e \bar{L} \Phi e_R + Y_u \bar{Q}_L \tilde{\Phi} u_R + Y_d \bar{Q}_L \Phi d_R + h.c$$

where $\tilde{\Phi} = i\tau_2 \Phi^*$ with $Y(\tilde{\Phi}) = -1$

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Scalar potential $\mu^2 > 0$ derives the vacuum to have non-zero vacuum expectation value

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- $\zeta_i(x)$ are called **Goldstone bosons** (massless, spinless)
- $h(x)$ is called **the Higgs boson**.

Masses of the Higgs boson and the fermions

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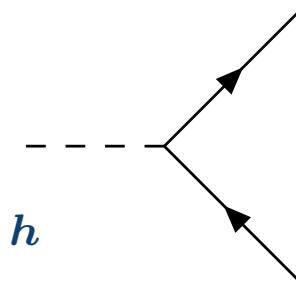
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The fermions masses and their interaction with $h(x)$

$$m_i = \frac{Y_i v}{\sqrt{2}}, \quad i = e, u, d, \quad h(x) \bar{Q} Q \implies i \frac{m_Q}{v} \quad Q = \tau, b, t$$



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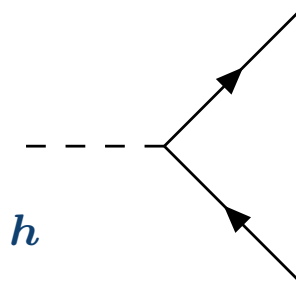
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Masses and Vertices of $W^\pm, Z, \gamma$ bosons

$$|\mathcal{D}_\mu \Phi|^2 \implies \frac{v^2}{8} \left(1 + \frac{h(x)}{v}\right)^2 \left(g^2 \left[(\mathcal{A}_\mu^{U1})^2 + (\mathcal{A}_\mu^{U2})^2 \right] + \left[g \mathcal{A}_\mu^{U3} - g' B_\mu^U \right]^2 \right)$$

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where the masses of $W^\pm, Z, \gamma$ bosons:

$$M_W^2 = \frac{g^2 v^2}{4}, \quad M_Z^2 = \frac{v^2}{4} (g^2 + g'^2), \quad M_\gamma = 0$$

The vertices are

$$h(x) V_{i\mu} V_i^{*\mu} \Rightarrow 2i \frac{M_i^2}{v} g_{\mu\nu}, \quad h(x) h(x) V_{i\mu} V_i^{*\mu} \Rightarrow 2i \frac{M_{V_i}^2}{v^2} g_{\mu\nu}$$

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- If $\Lambda_P = 10^{19}$ GeV, the higgs has to be light $m_h \leq 145$ GeV.
- If $\Lambda_P = 10^3$ GeV, the higgs has to be heavy $m_h \leq 750$ GeV.

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- Bounds are sensitive to top quark mass m_t

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- NNLO computation of various couplings in the SM by Degrandi et.al:

$$m_h \geq 129.2 + 1.8 \times \left(\frac{m_t^{\text{pole}} - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \right) - 0.5 \times \left(\frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0 \text{ GeV} .$$

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- m_t dependence:

$$\Delta m_t = 1 \text{ GeV} \quad \longrightarrow \quad \Delta m_h = \pm 2 \text{ GeV}$$

2σ variation of the top quark mass allows the upper bound $m_h \geq 125.6 \text{ GeV}$.

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$$m_h \geq 129.2 + 1.8 \times \left(\frac{m_t^{\text{pole}} - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \right) - 0.5 \times \left(\frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0 \text{ GeV}.$$

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$$\Delta m_t = 1 \text{ GeV} \quad \longrightarrow \quad \Delta m_h = \pm 2 \text{ GeV}$$

2σ variation of the top quark mass allows the upper bound $m_h \geq 125.6 \text{ GeV}$.

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$$m_t^{\overline{\text{MS}}}(m_t) = 163.3 \pm 2.7 \text{ GeV} \quad \longrightarrow \quad m_t^{\text{pole}} = 173.3 \pm 2.8 \text{ GeV},$$

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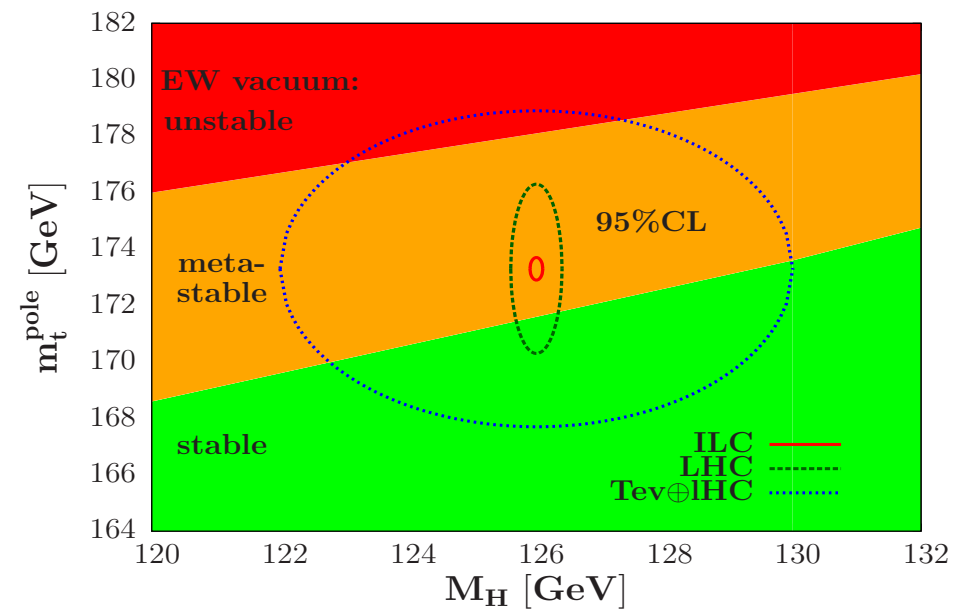
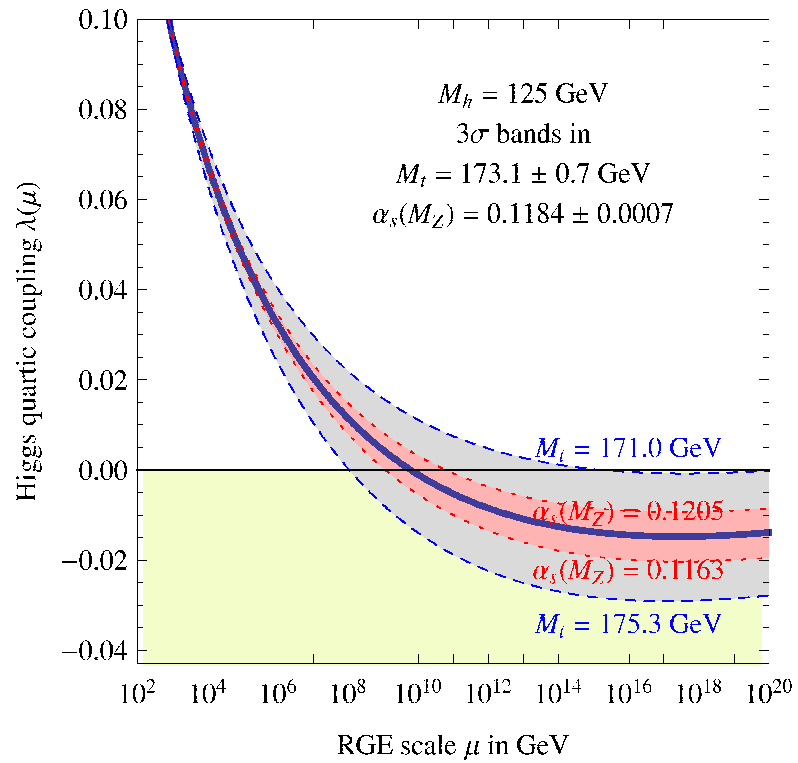
- Global average has small error

$$m_t^{\text{exp}} = 173.2 \pm 0.9 \text{ GeV}.$$

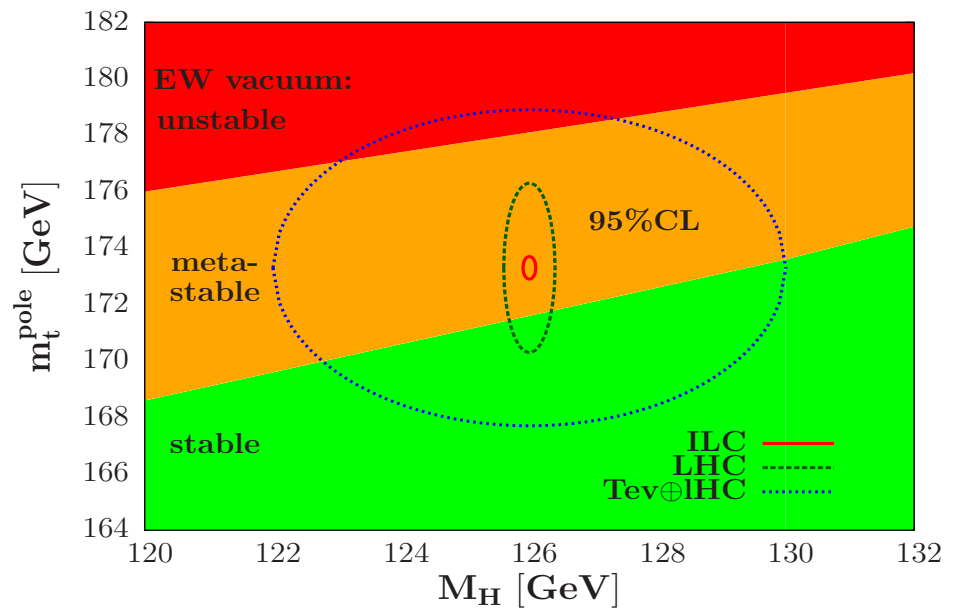
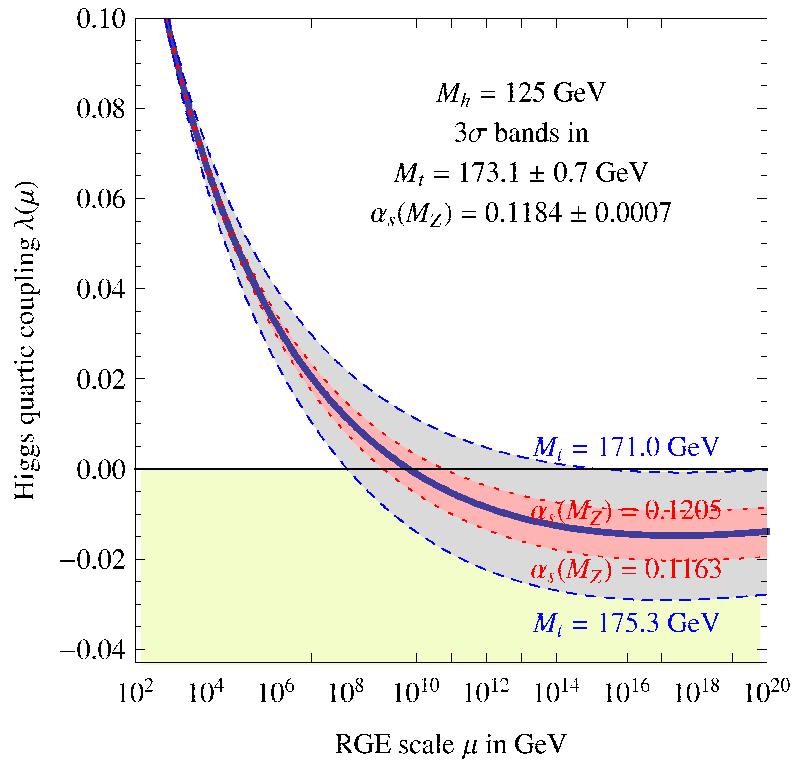
which can give stringent condition on vacuum stability with small error on the higgs mass.

Vacuum stability

Vacuum stability



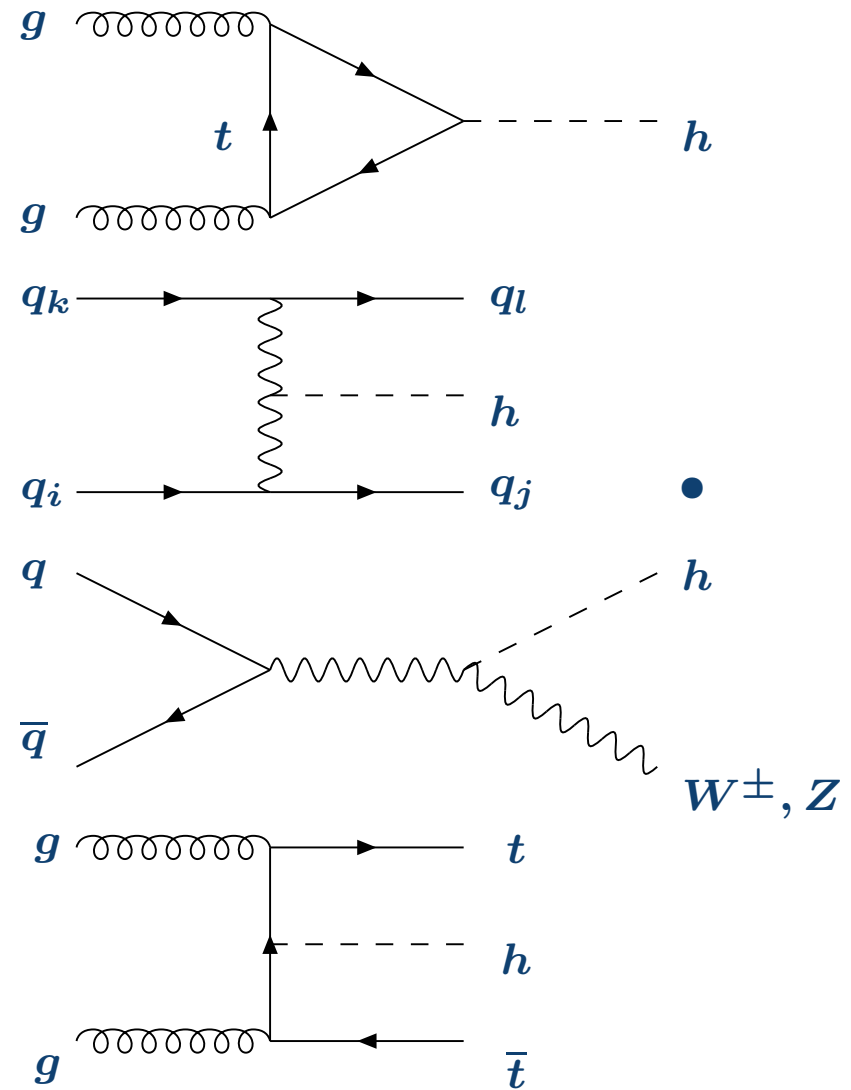
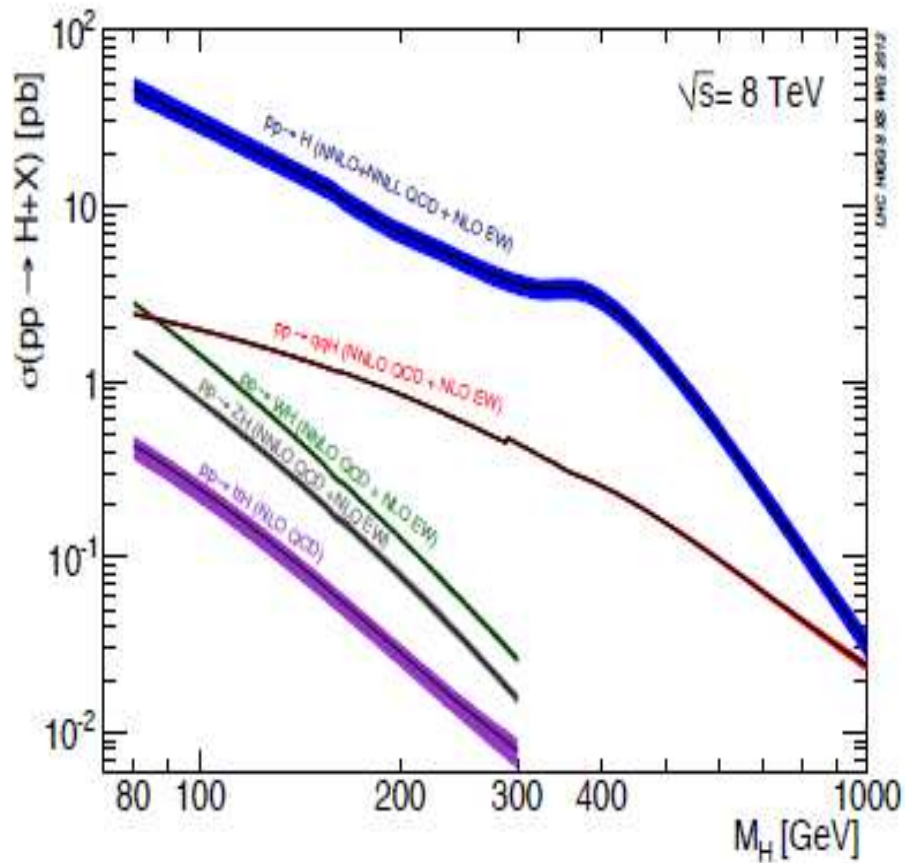
Vacuum stability



- λ is sensitive to top mass
- Stability of vacuum can be answered only if the error on the top mass goes down significantly.
- e^+e^- machine can give better measurement of top mass

Higgs Production at the LHC (8 TeV)

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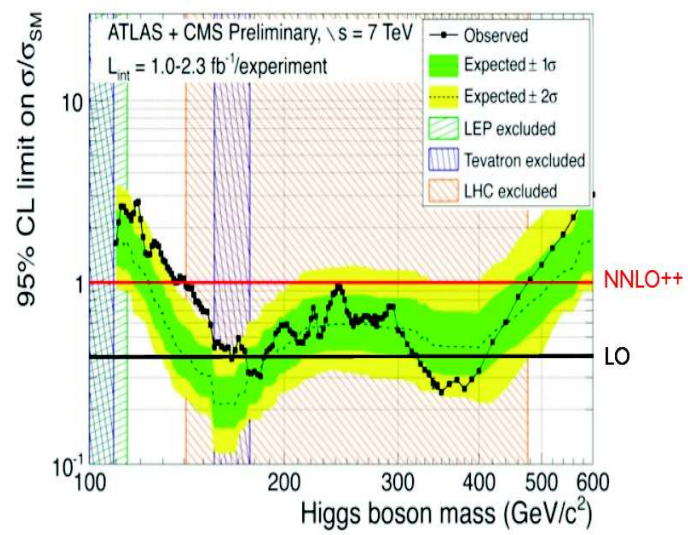


First three productions are known to NNLO level in QCD

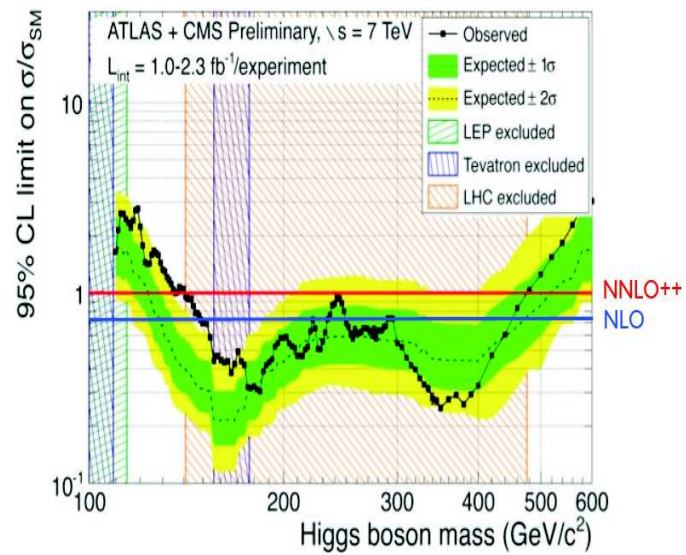
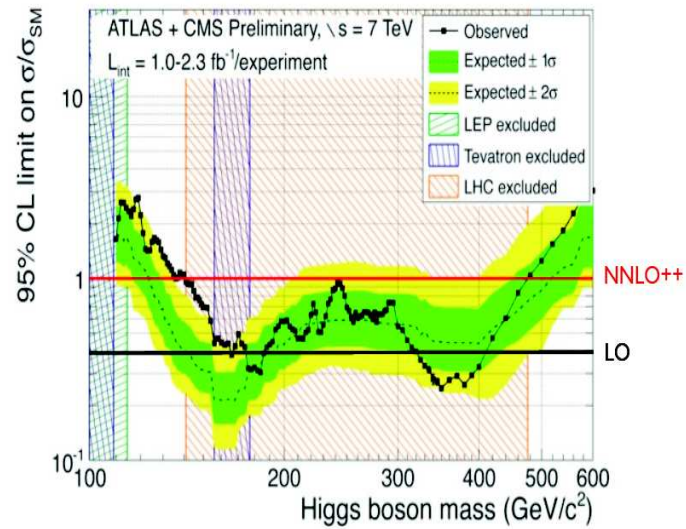
- the last one is known only upto NLO level.

Theory influence on the rates

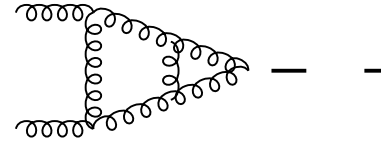
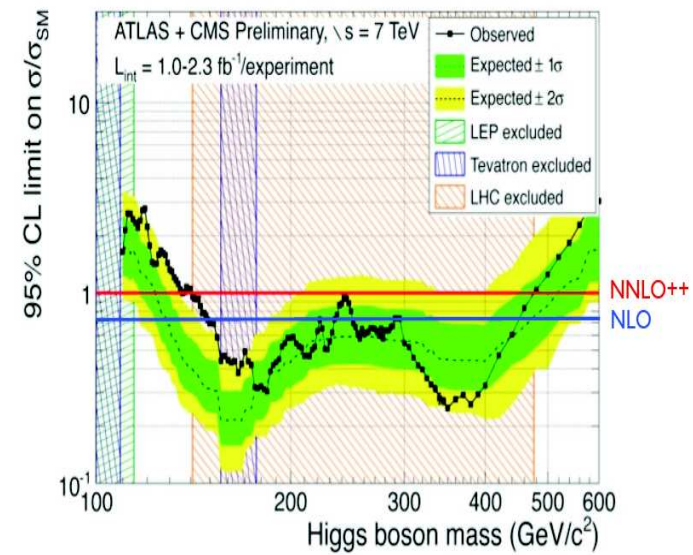
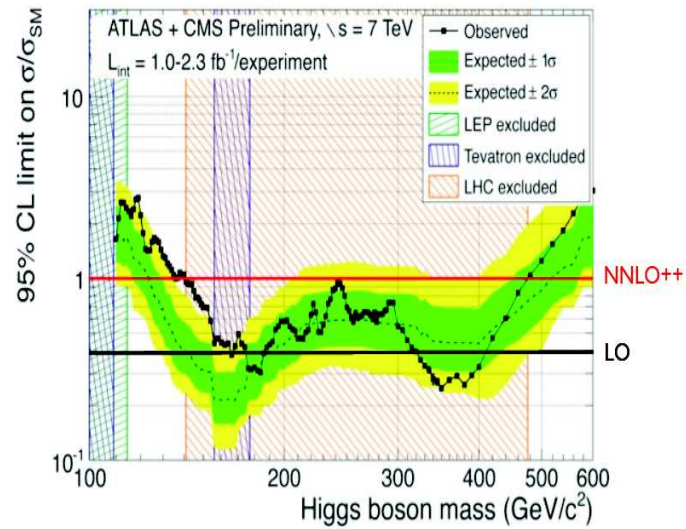
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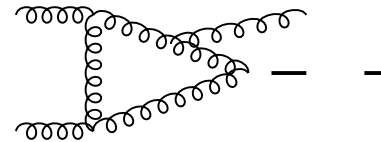
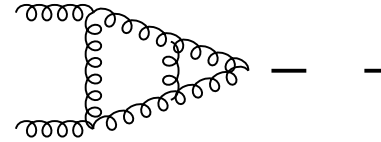
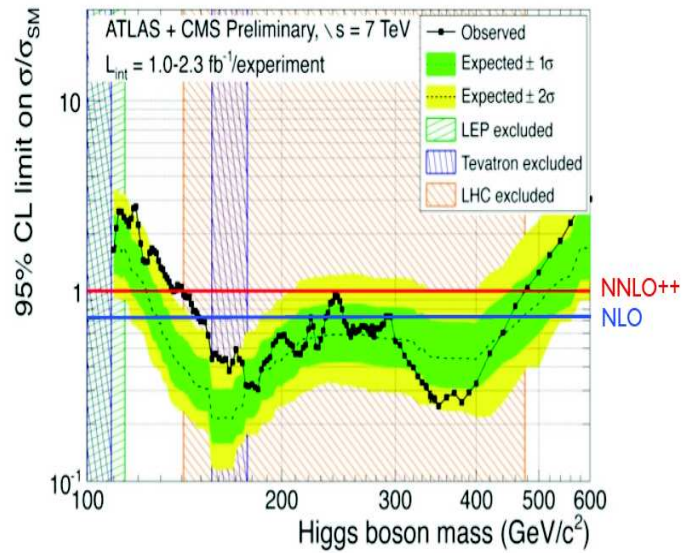
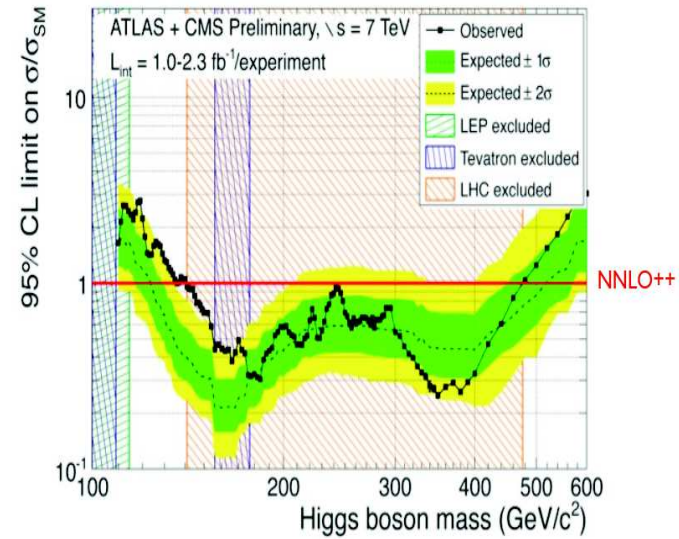
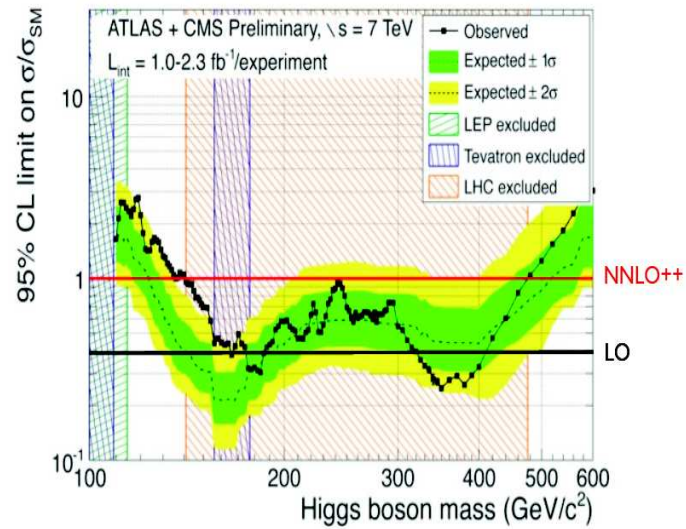
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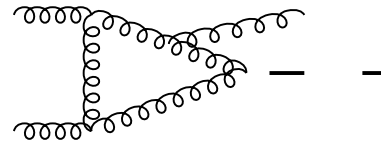
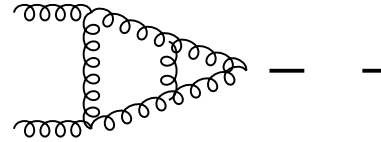
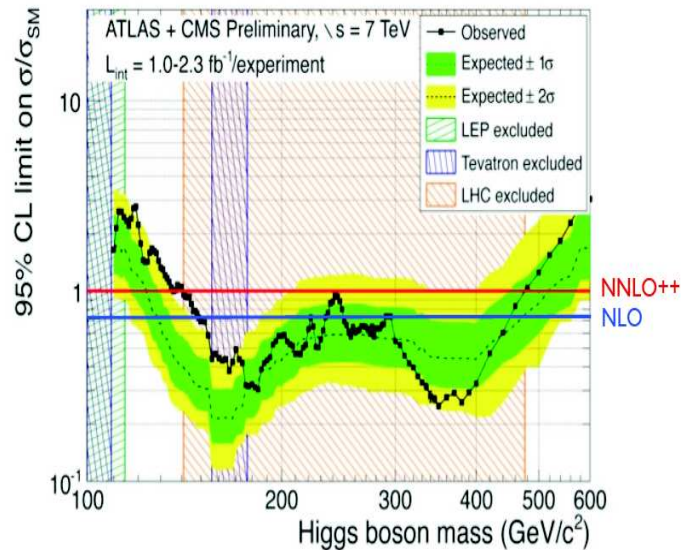
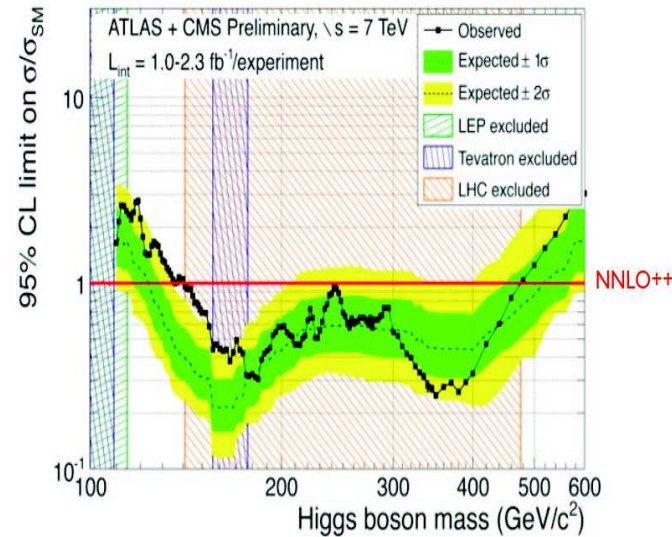
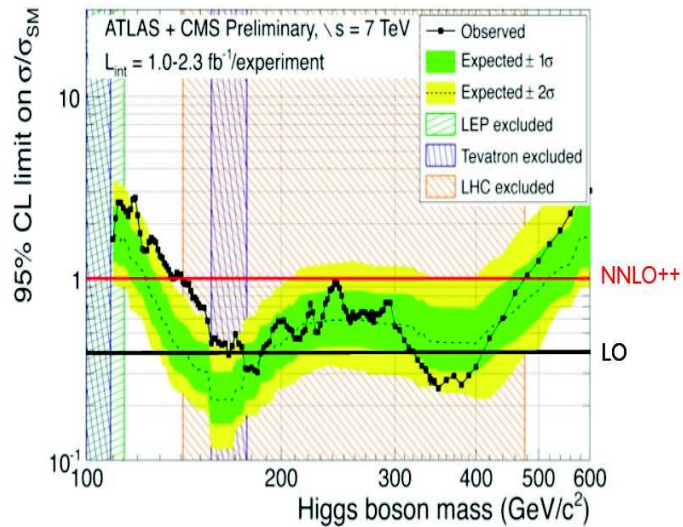
Theory influence on the rates



Theory influence on the rates



Theory influence on the rates



- To exclude something we need to understand the signal well
- To discover something we need to understand the background well

R. Harlander

Why LO, NLO and NNLO for Higgs production

$$P_1 + P_2 \rightarrow higgs + X$$

Why LO, NLO and NNLO for Higgs production

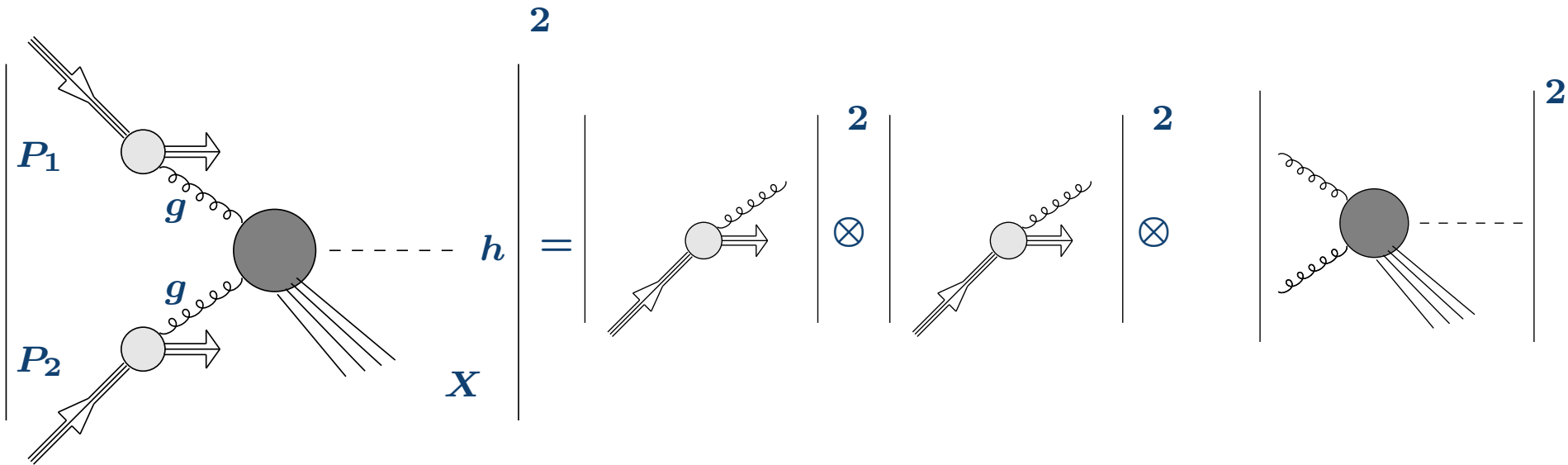
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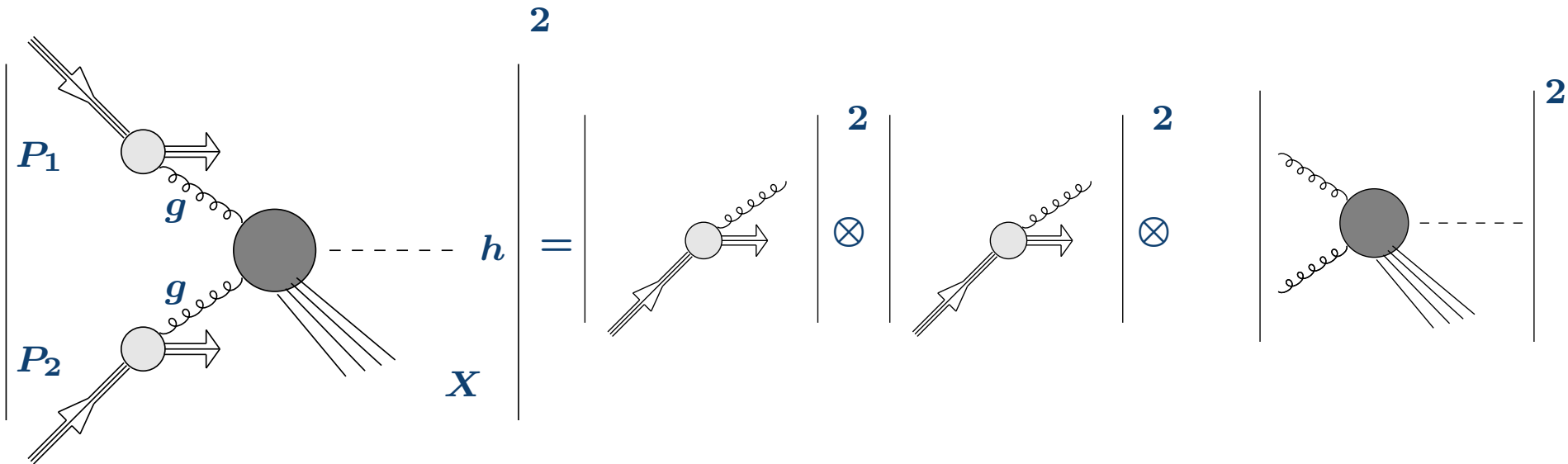
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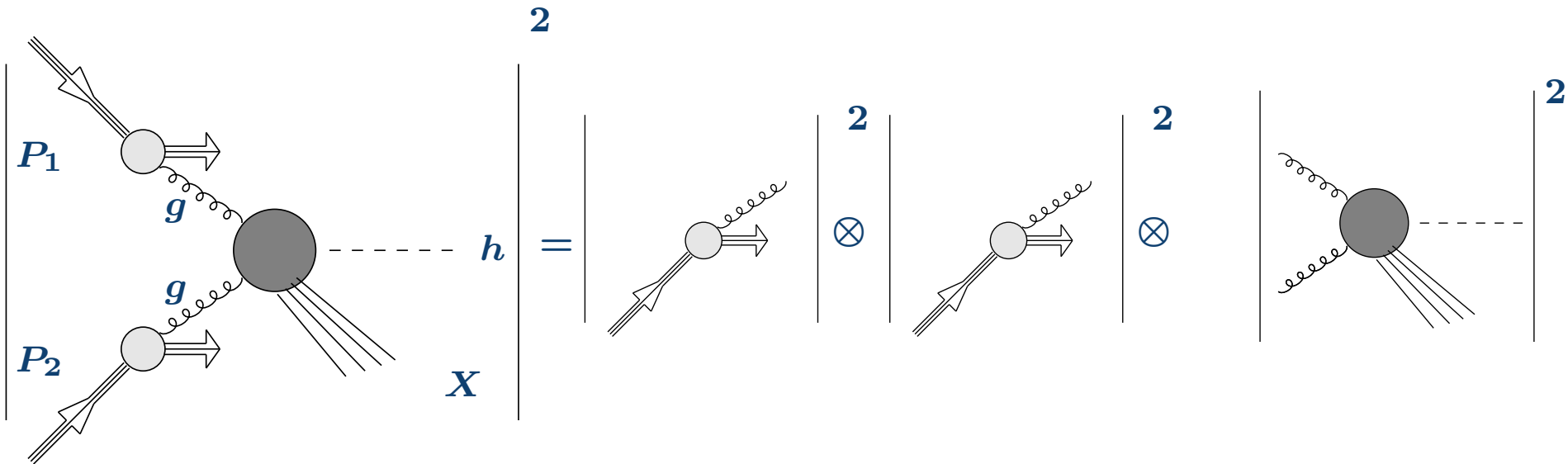
Extraction of non-perturbative functions:

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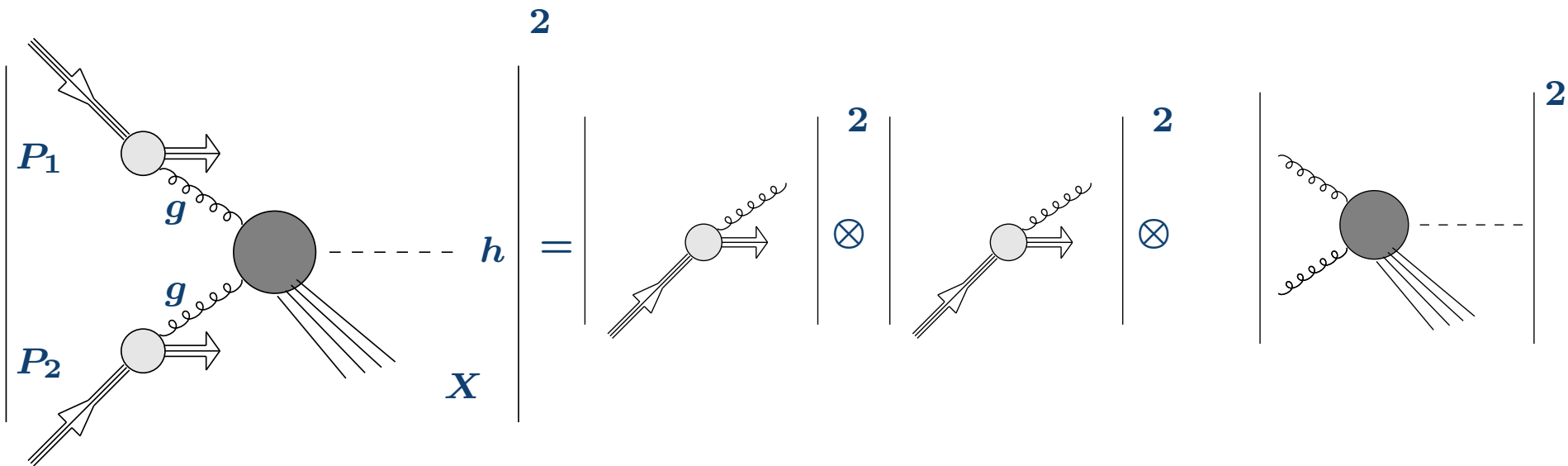
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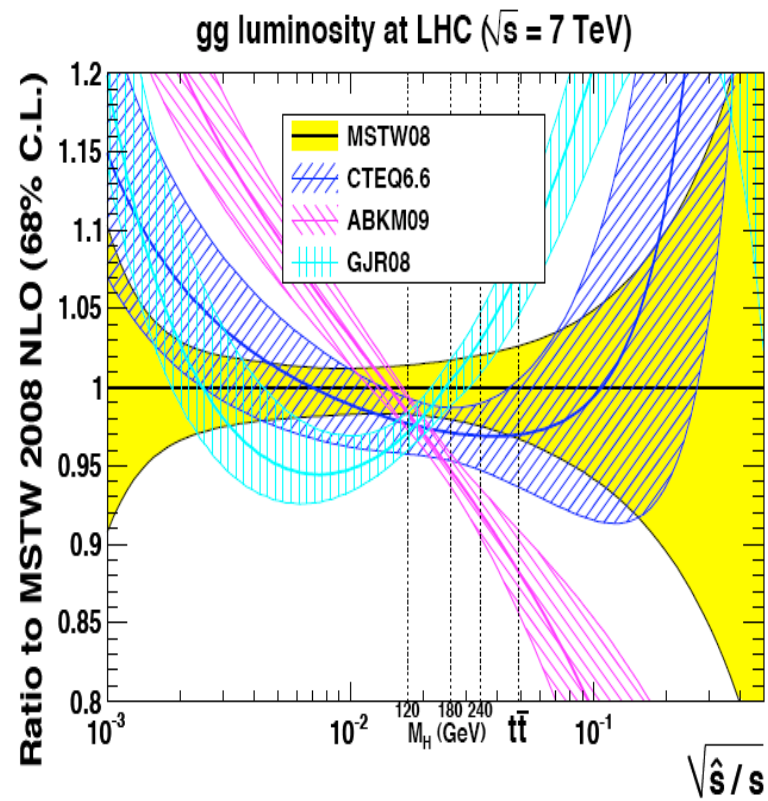
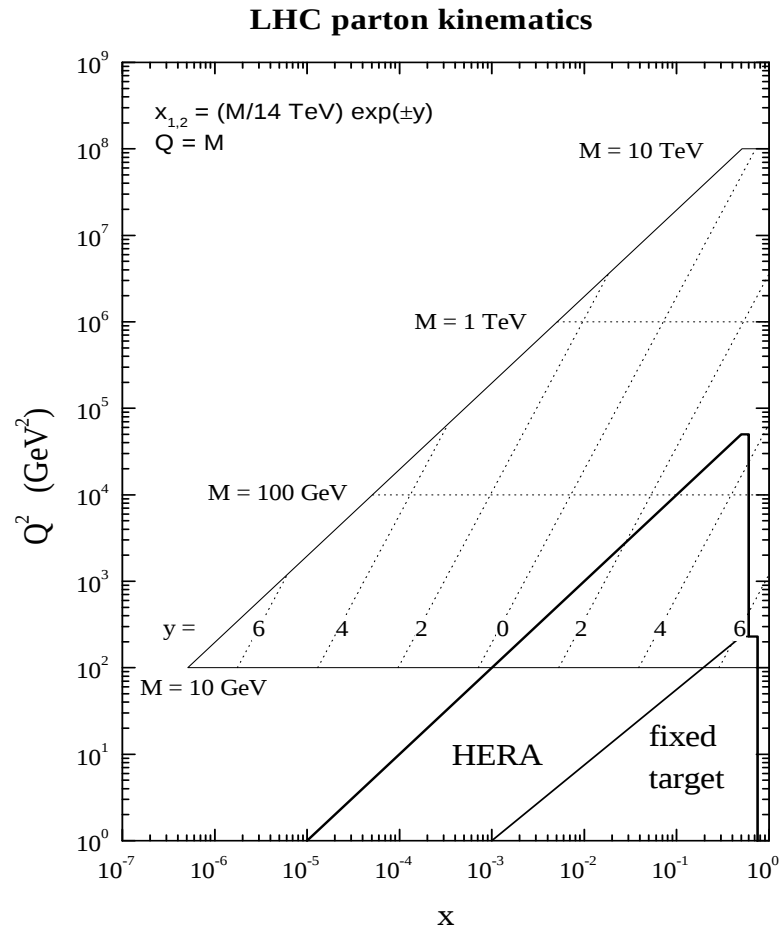
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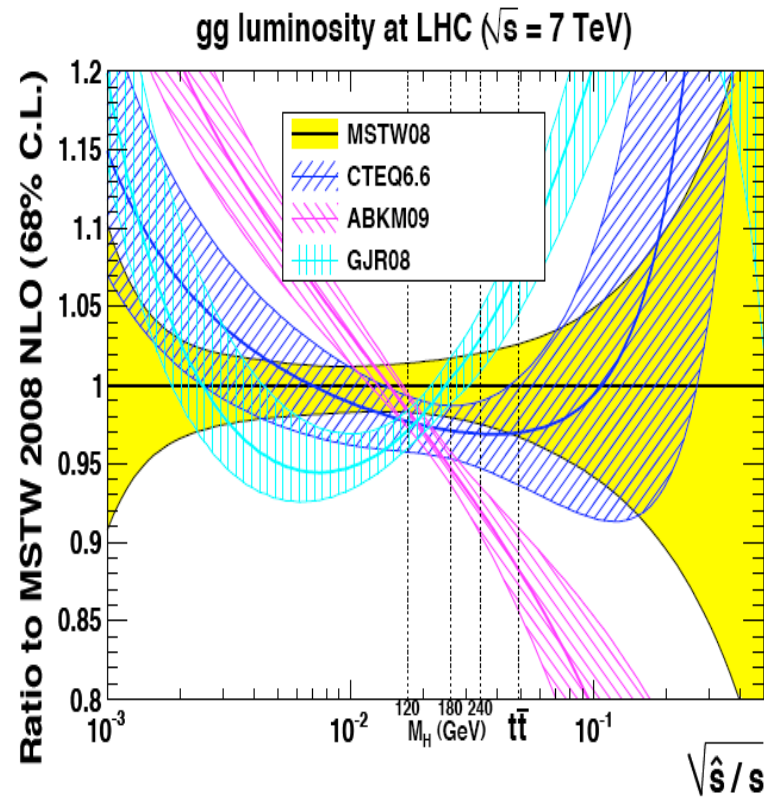
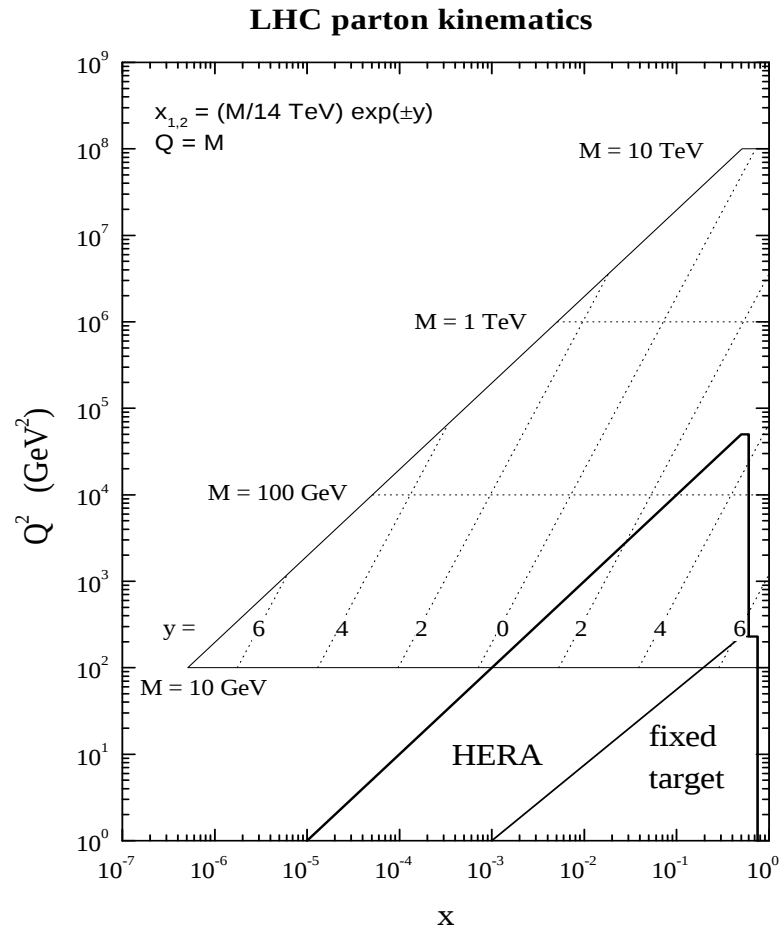
PDF from LHC

[*Martin, Roberts, Stirling, Thorne*]



PDF from LHC

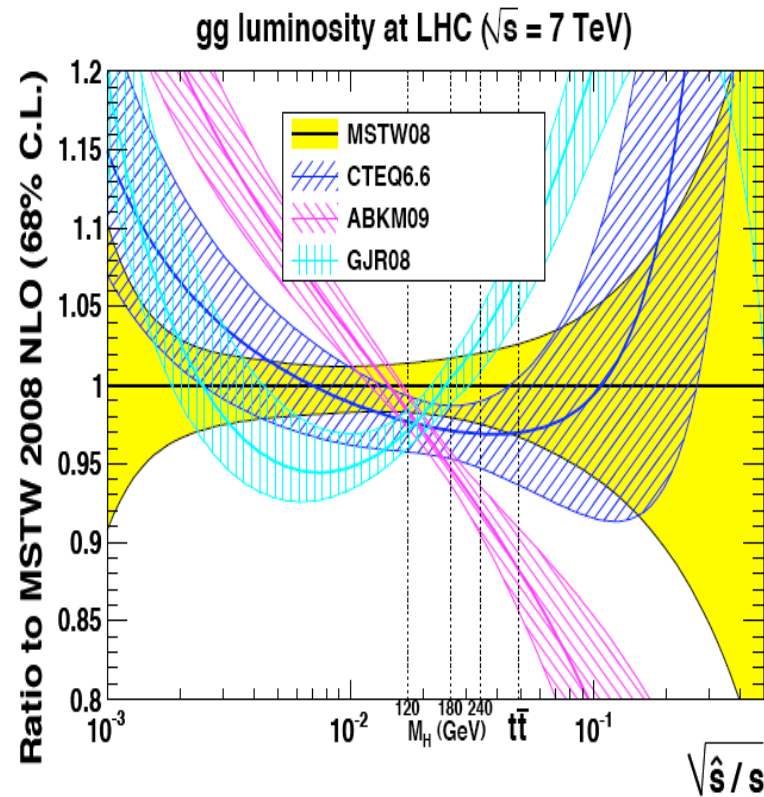
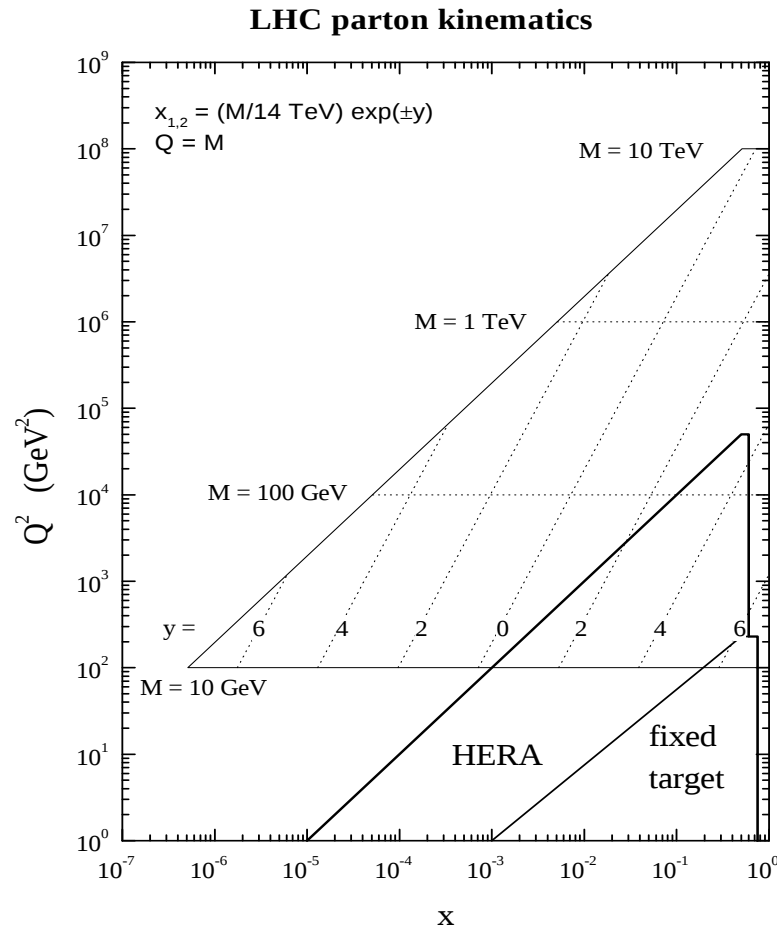
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- MSTW, ABM and NNPDF come with different PDF sets with different choices of α_s, m_c, m_b

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- MSTW, ABM and NNPDF come with different PDF sets with different choices of α_s, m_c, m_b
- Choice of PDF set can bring in significant uncertainty of the order 10 to 20%

Partonic Cross section

Partonic Cross section

$$2S \, d\sigma^{P_1 P_2}(\tau, m_h^2) = \sum_{ab} \int_{\tau}^1 \frac{dx}{x} \Phi_{ab}(x, \mu_F) \, 2\hat{s} \, d\hat{\sigma}^{ab}\left(\frac{\tau}{x}, m_h^2, \mu_F\right)$$

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- $d\hat{\sigma}^{ab}$ is perturbatively computable as a power series in $\alpha_s(\mu_R)$, where μ_R is the renormalisation scale.

$$d\hat{\sigma}^{ab}(\mu_F) = \alpha_s^d(\mu_R) \sum_{i=0} \alpha_s^i(\mu_R) d\hat{\sigma}^{ab,(i)}(\mu_F, \mu_R)$$

- Renormalisation group equation:

$$\mu_R^2 \frac{d}{d\mu_R^2} \alpha_s(\mu_R) = \beta(\alpha_s(\mu_R))$$

- Fixed order results are often sensitive to μ_R .
- Many new production channels open up beyond LO.

Gluon fusion to Higgs at Leading Order(LO)

Hinchcliff, many others

Gluon fusion to Higgs at Leading Order(LO)

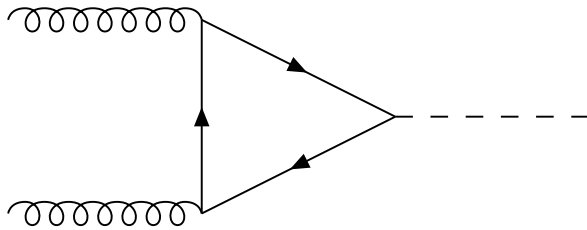
Hinchcliff, many others

$$2S \, d\sigma^{PP}(x, m_h) = \int_x^1 \frac{dz}{z} \Phi_{gg}^{(0)}(z, m_h, \mu_F) \, 2\hat{s} \, d\hat{\sigma}_{gg}^{(0)}\left(\frac{x}{z}, m_h^2, \mu_R\right) + \dots$$

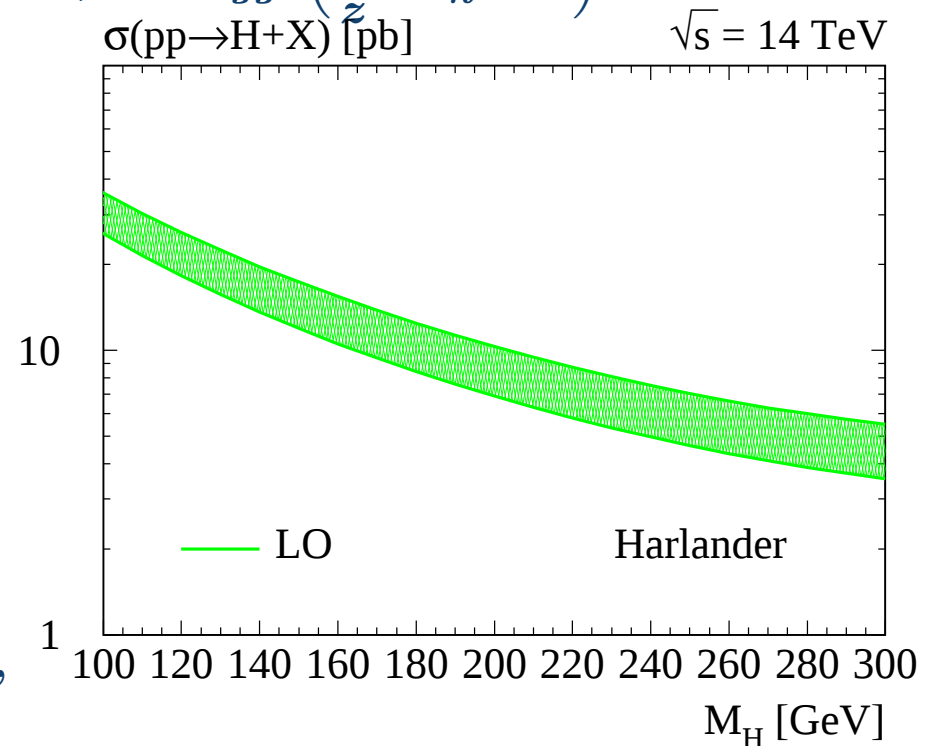
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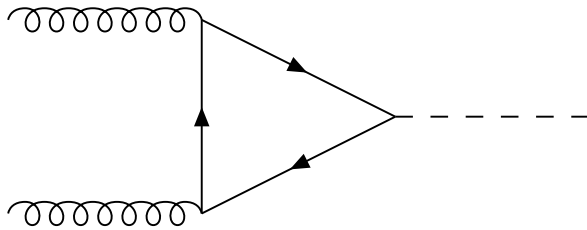
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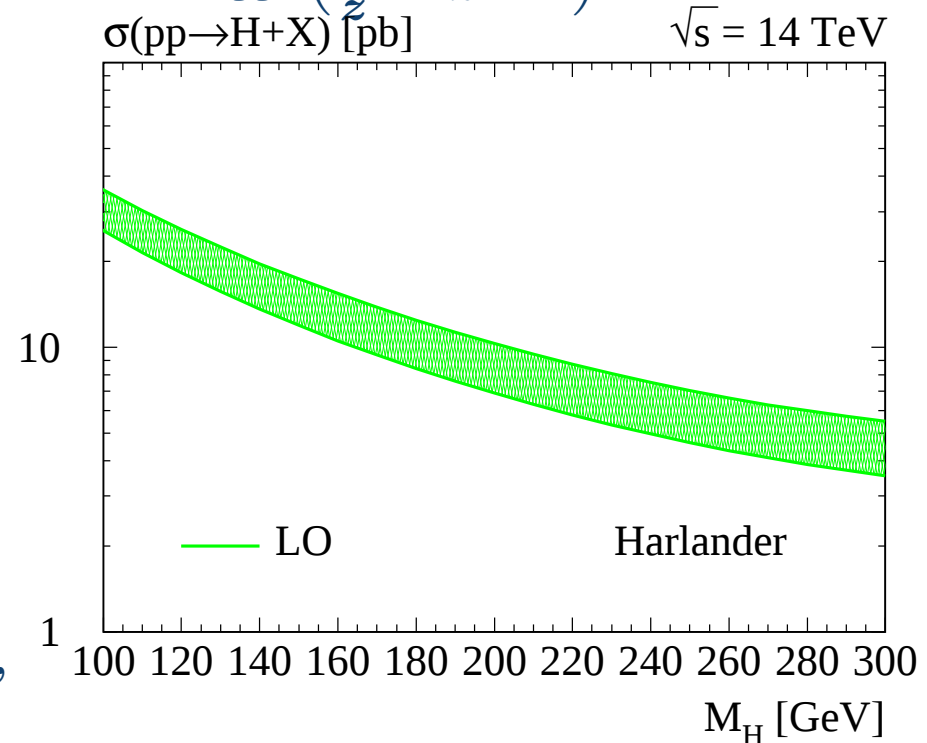
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- Leading order is uncontrollable due to μ_R scale and can not be used for any study in the present form.
- Only higher order corrections can provide sensible result thanks to RG equation

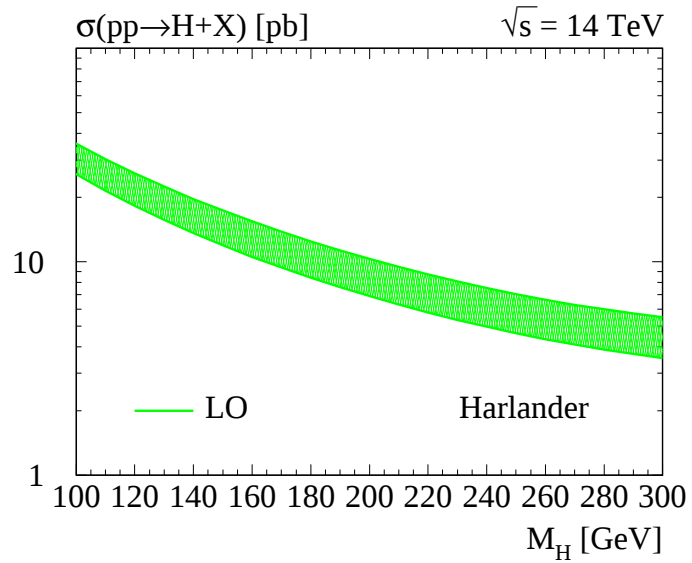
$$\mu^2 \frac{d}{d\mu^2} \sigma = 0$$

NNLO QCD corrected Higgs Cross section at $\sqrt{S} = 14$ TeV

$$m_H/2 < \mu_F = \mu_R < 2m_H$$

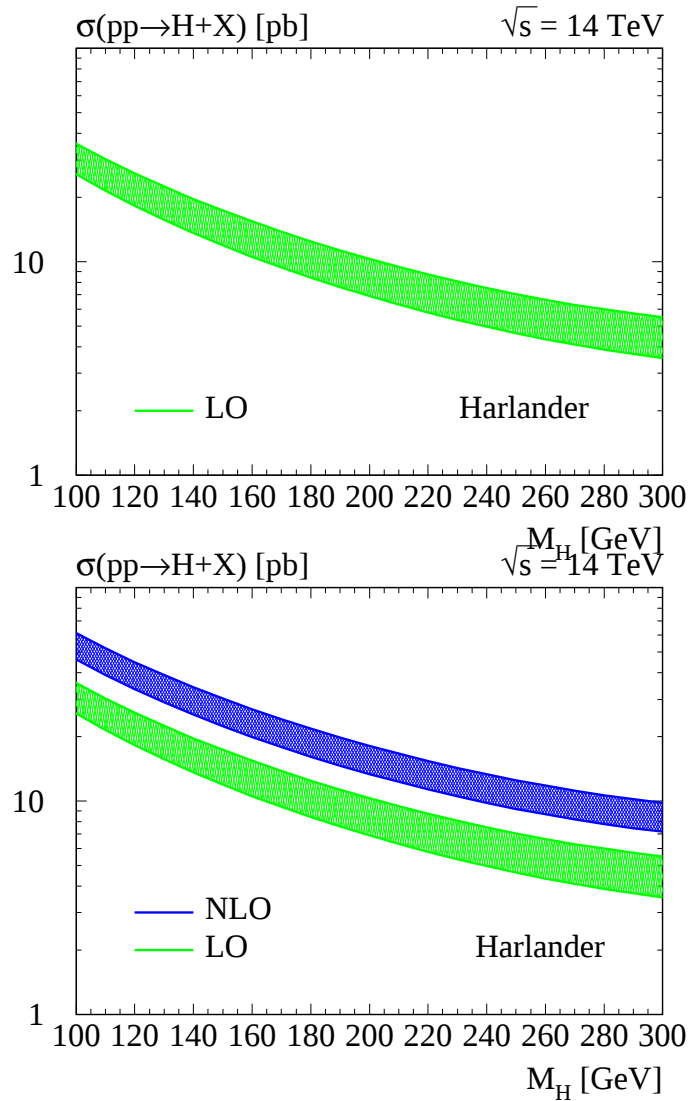
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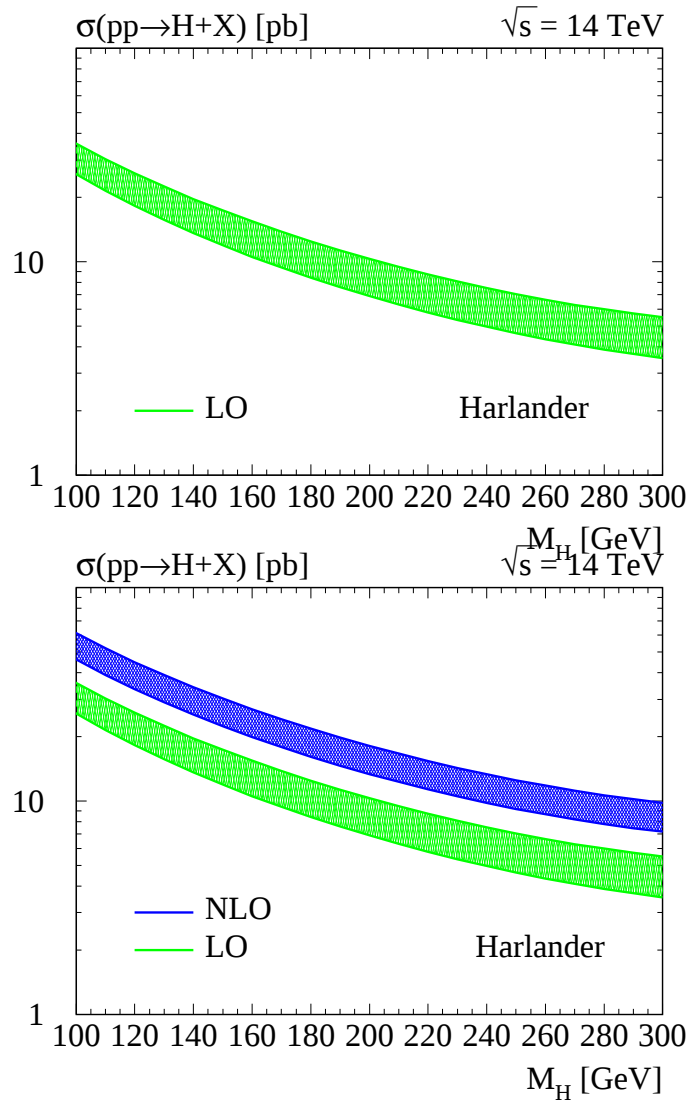
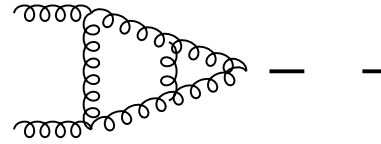
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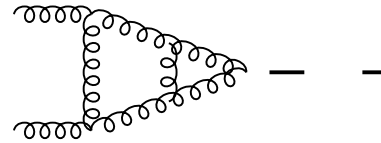
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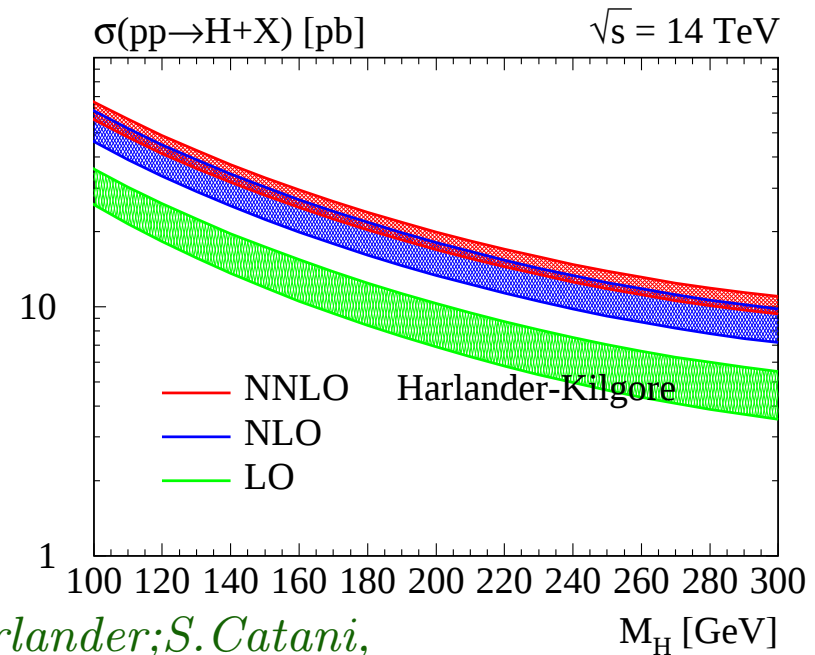
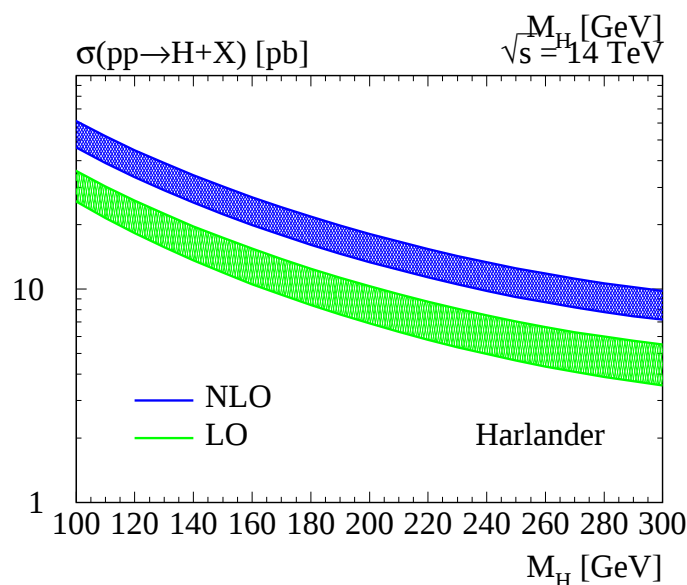
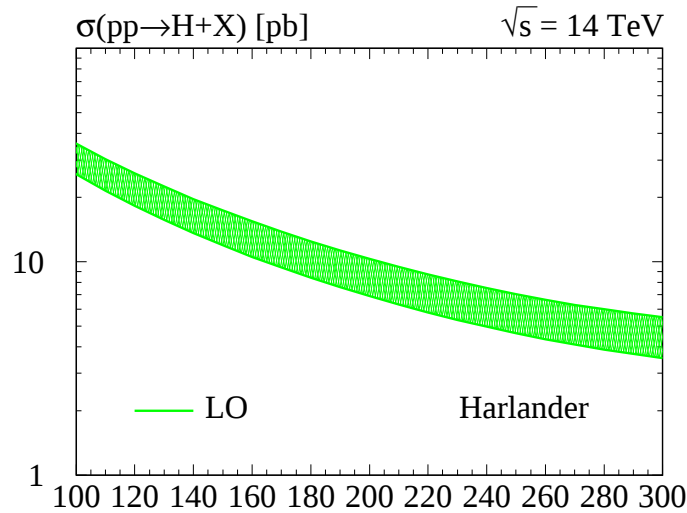


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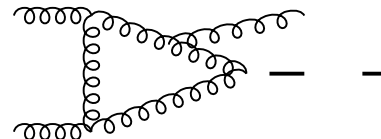
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A. Djouadi, D. Grandenz, M. Spira, P. Zerwas



*R. Harlander; S. Catani,
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R. Harlander, B. Kilgore; C. Anastasiou, Melnikov;
VR, J. Smith, W. L. van Neerven*



Soft gluons dominate!

*S. Catani, P. Nason, M. Grazzini, D. DeFlorian; R. Harlander,
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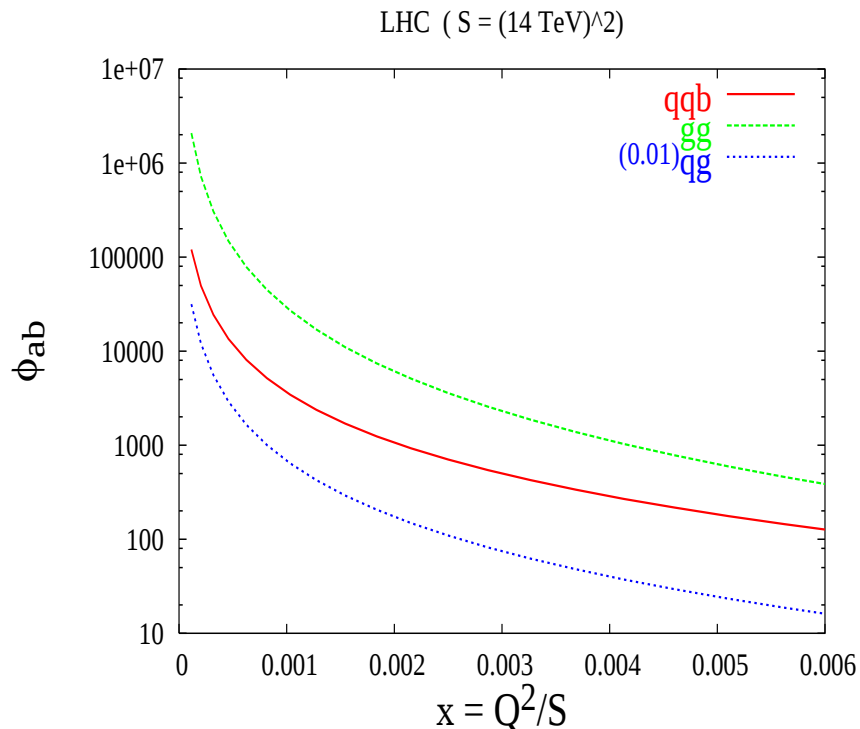
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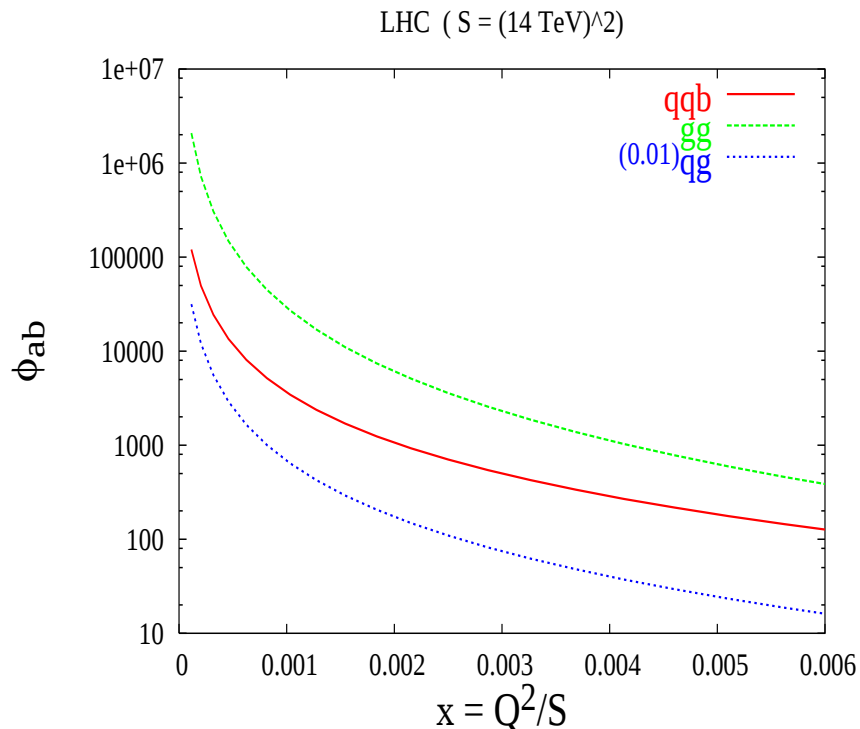
Gluon flux is largest at LHC ●
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- $\Phi_{ab}(x)$ becomes large when $x \rightarrow x_{min} = \tau$

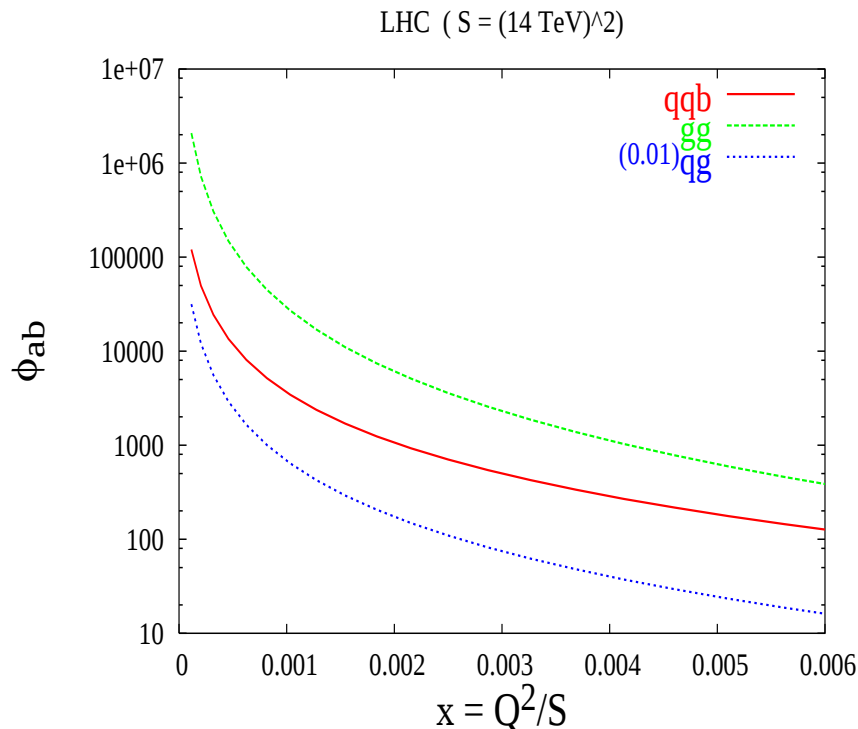
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- $\Phi_{ab}(x)$ becomes large when $x \rightarrow x_{min} = \tau$
- Dominant contribution to Higgs production comes from the region when $x \rightarrow \tau$

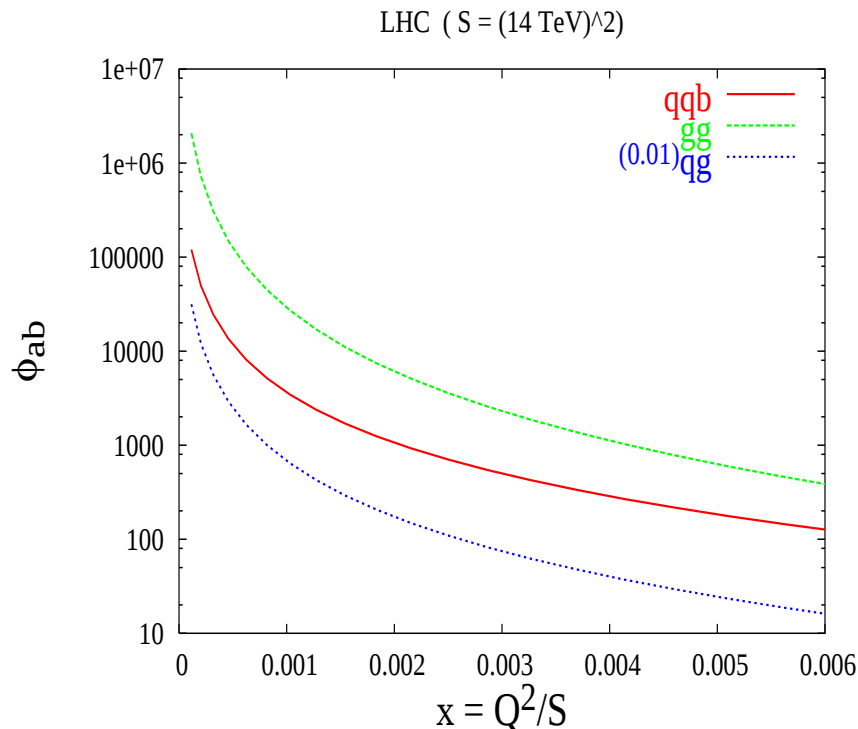
Gluon flux is largest at LHC •
Soft gluon NNLL resummation
gives less than 9% correction
at the LHC

S. Catani, D. DeFlorian, P. Nason, M. Grazzini

Soft gluons dominate!

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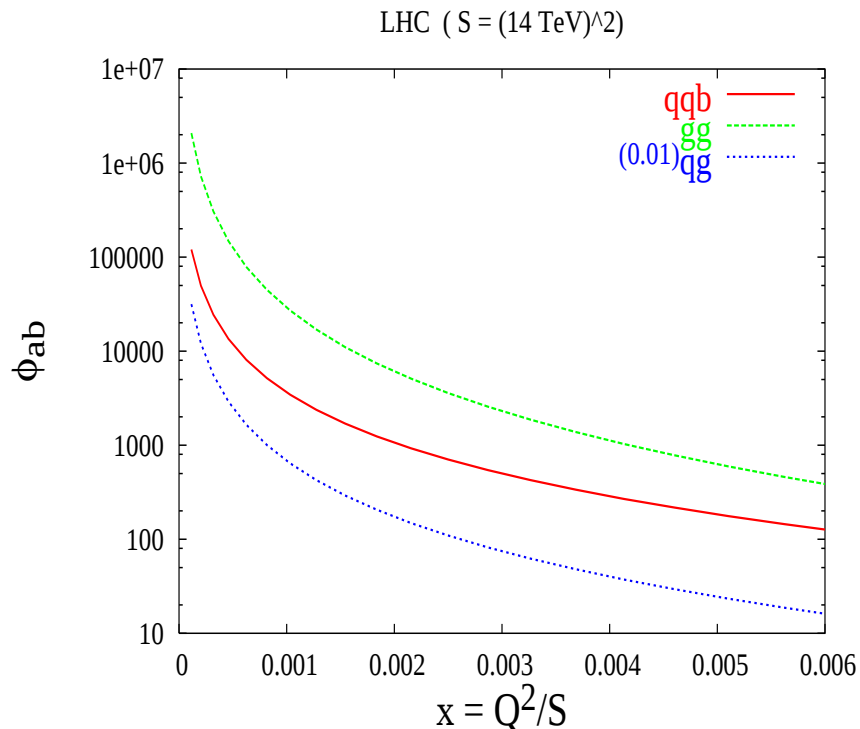
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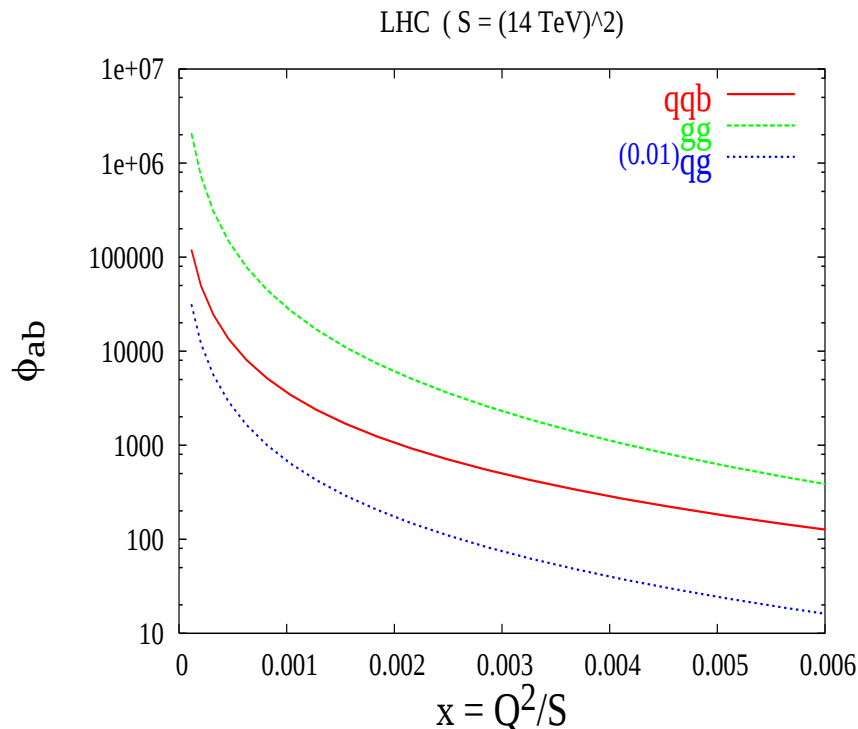
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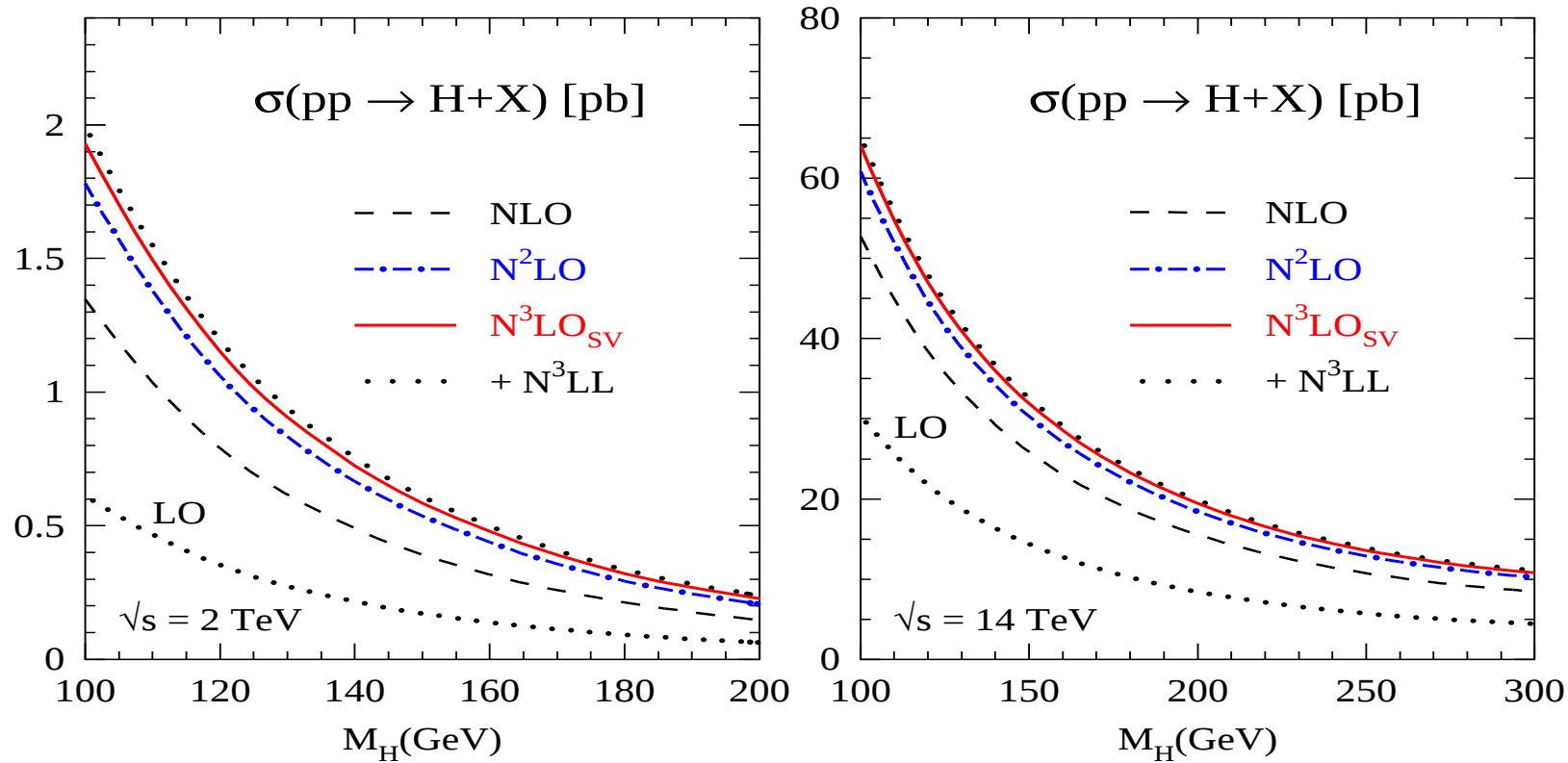
- $\Phi_{ab}(x)$ becomes large when $x \rightarrow x_{min} = \tau$
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- Expand the partonic cross section around $x = \tau$.

Soft gluon Resummation beyond $NNLL$ for Higgs production

S. Catani, P. Nason, D. DeFlorian, M. Grazzini; S. Moch, A. Vogt; E. Laenen, L. Magnea

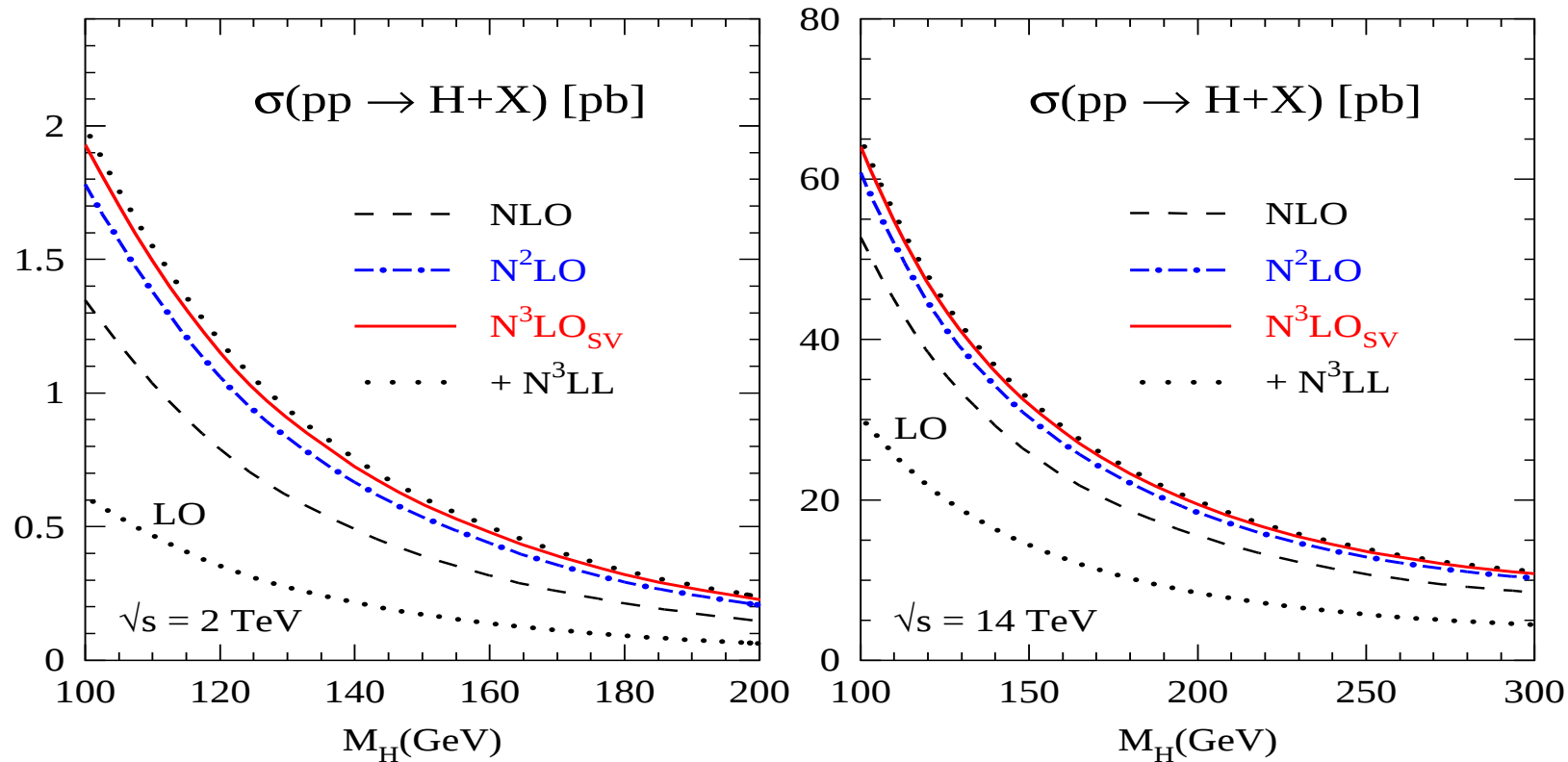
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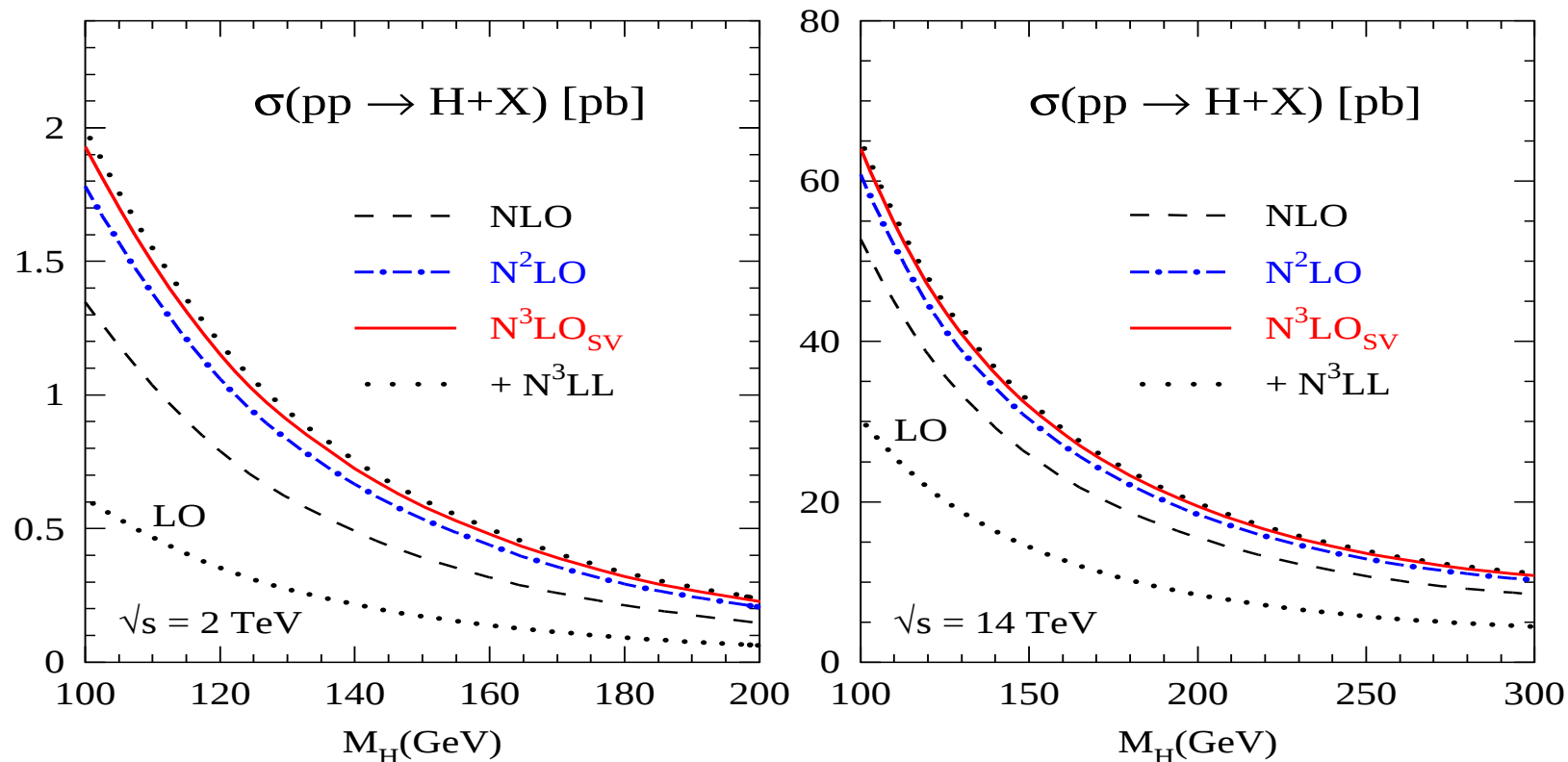
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- N^3LL resummation exponents are available now.

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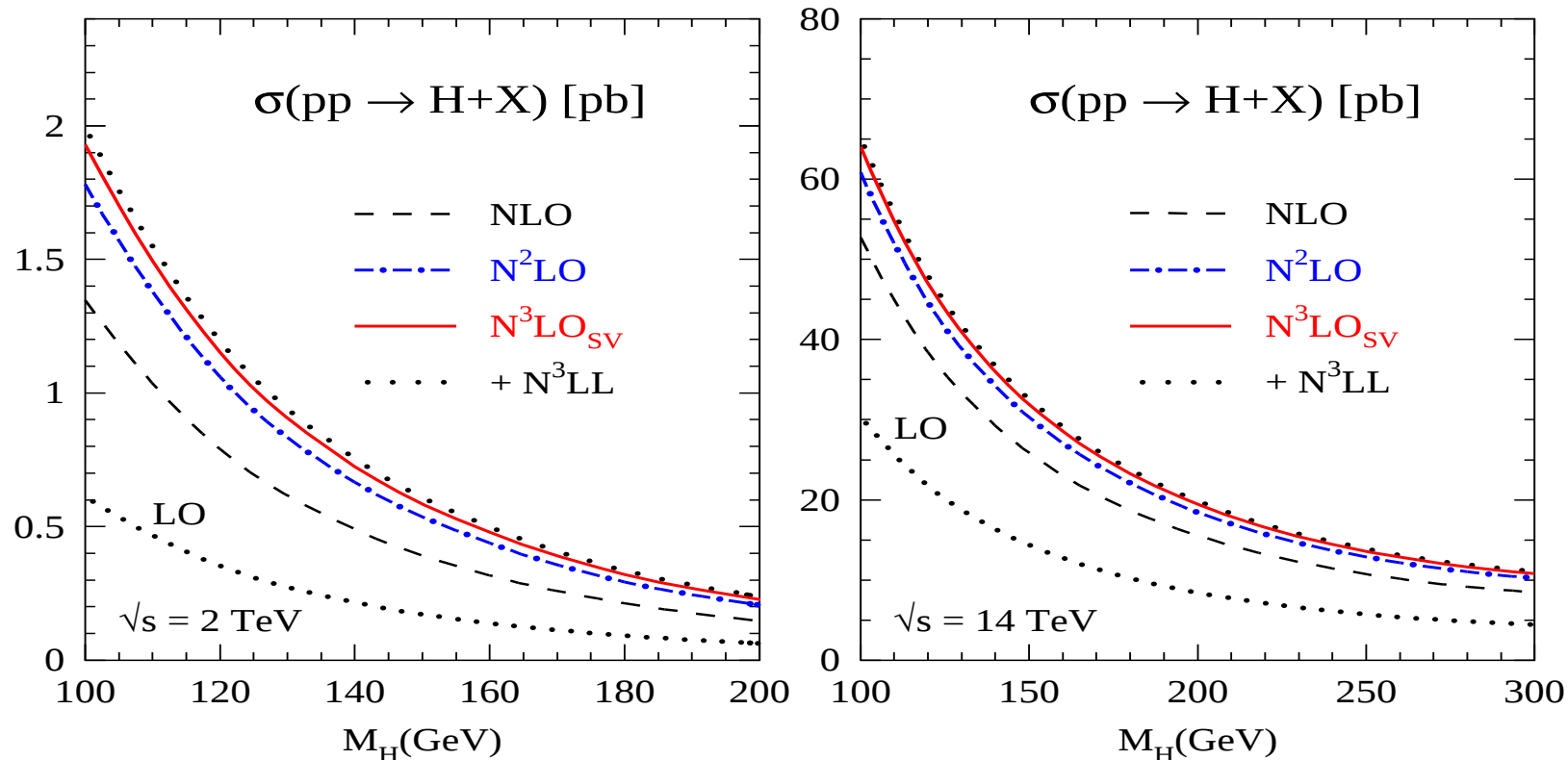
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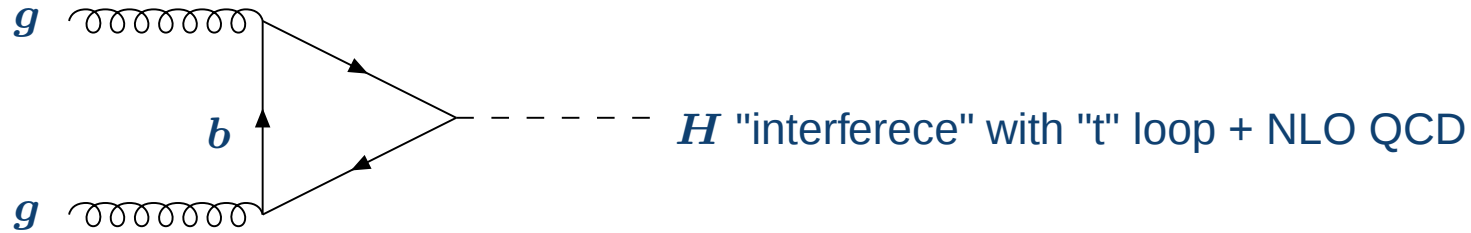
- N^3LL resummation exponents are available now.
- N^3LL resummation does not change the picture much. Fixed order N^3LO_{pSV} is very close to the N^3LL resummed result.
- Since QCD corrections can reduce the scale uncertainties only to 10% – 20%, contributions from **electroweak sector** is also important.

2-loop Electroweak, Mixed QCD and Electroweak, b quark contributions:

U. Aglietti et al; G. Degrassi, F. Maltoni; G. Passarino et al; Anastasiou et al; W. Keung, F. Petriello, O. Brein

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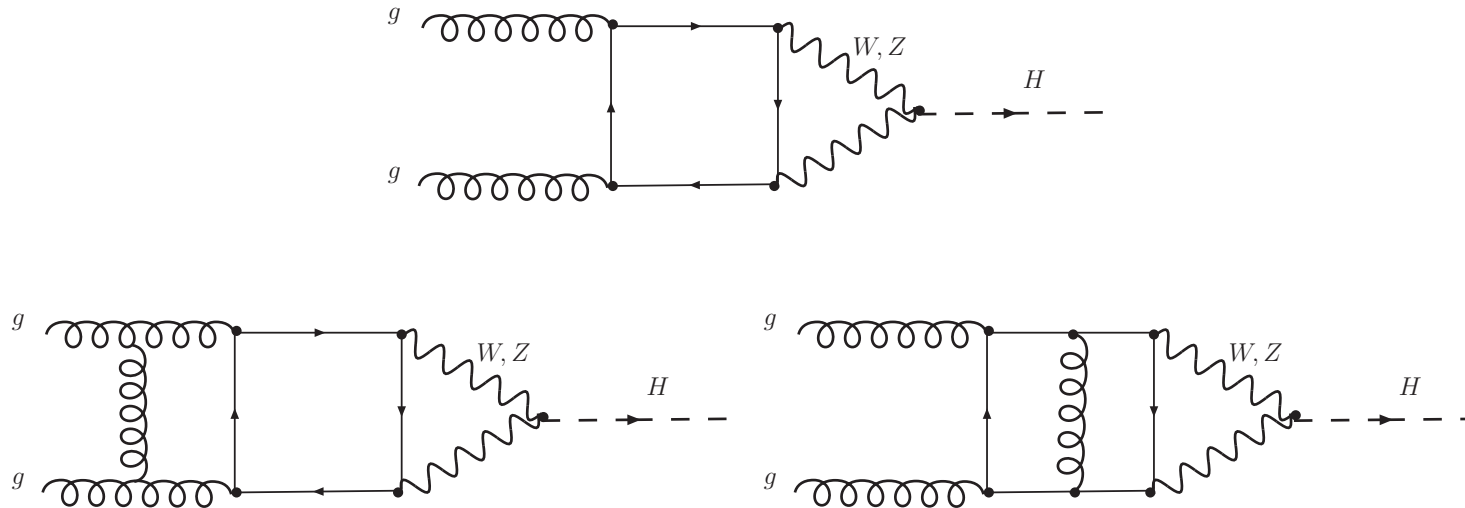


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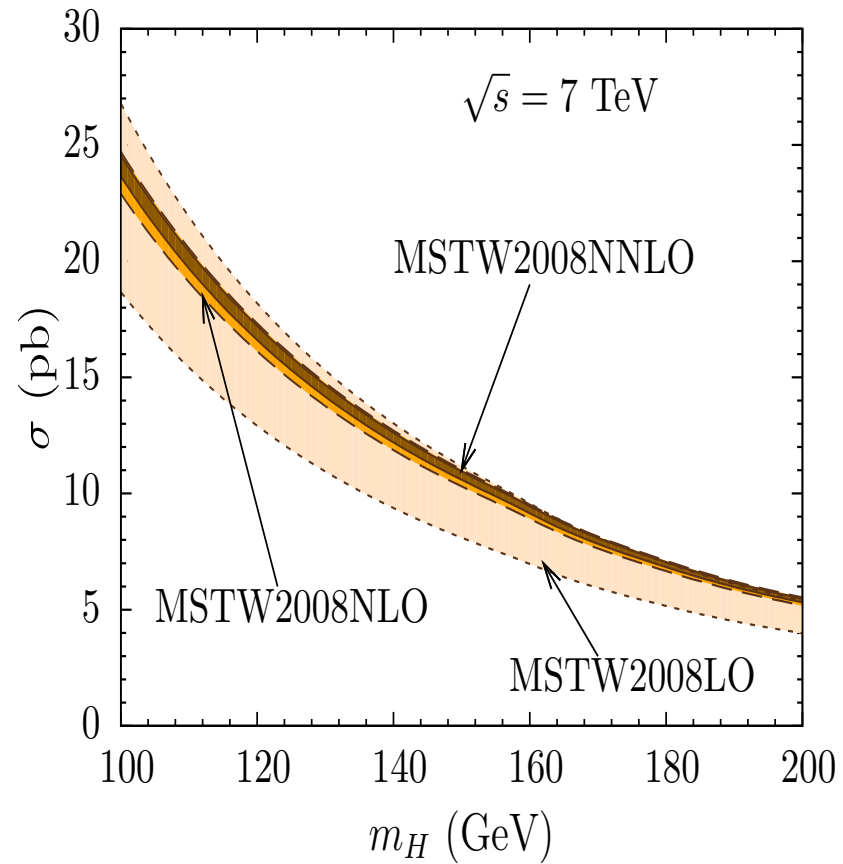
Pure QCD processes interference with Electroweak Processes:



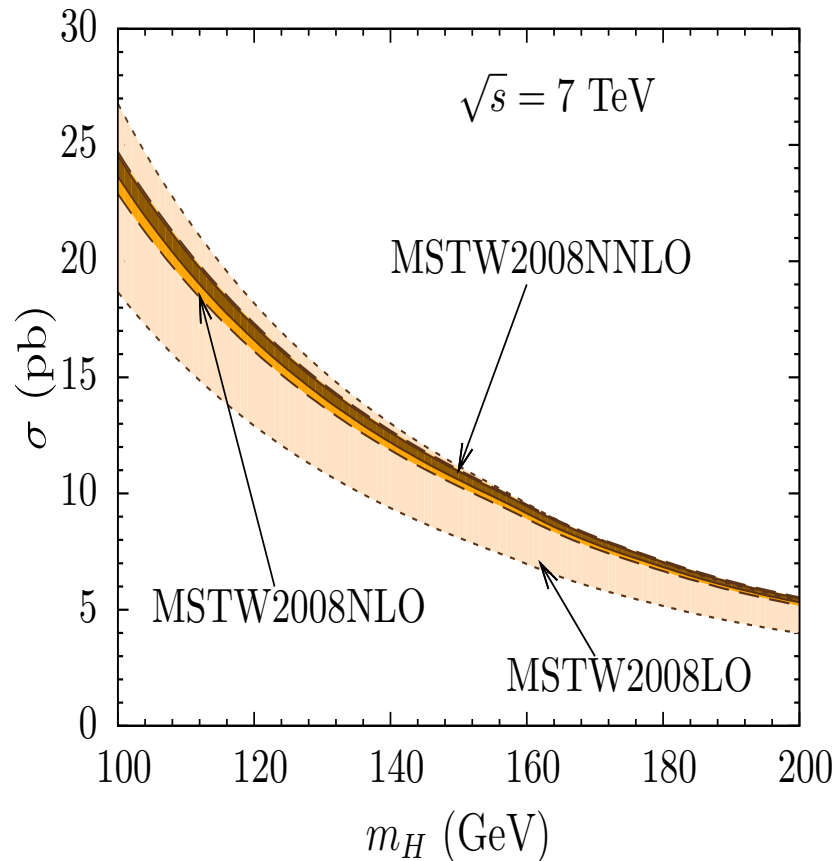
Electroweak: 5% ($m_H = 120$ GeV) and -2% ($m_H = 300$ GeV); b quark loops contribute 5 – 6% at $m_H = 120$ GeV at LHC

Renormalisation group improved result

Renormalisation group improved result



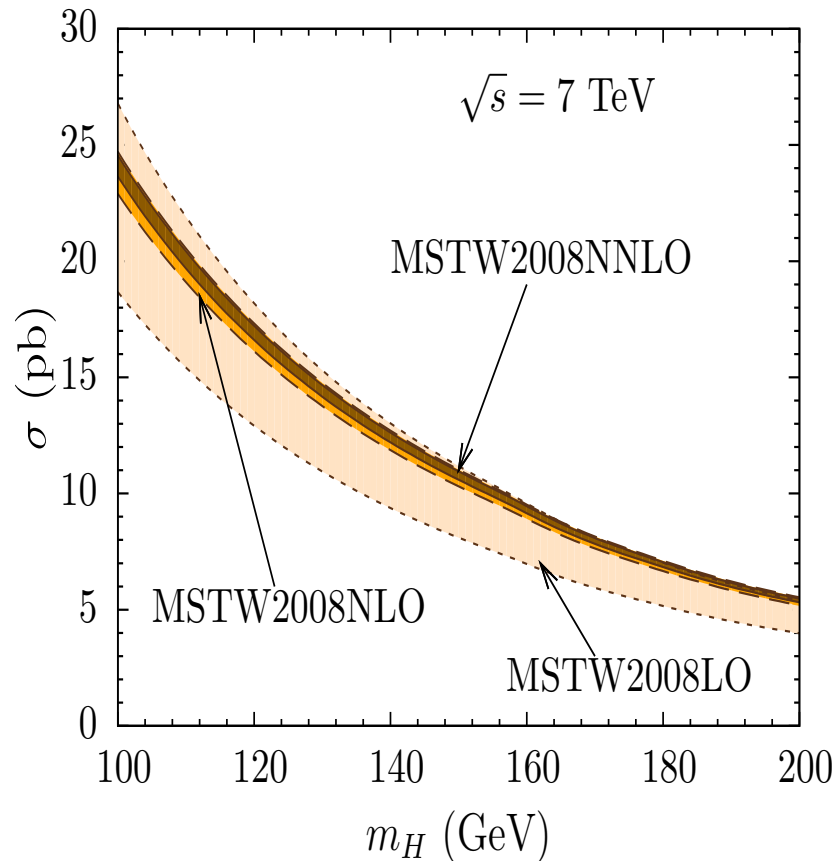
Renormalisation group improved result



Ahrens, Becher, Neubert, Yang:

- NLO with exact top quark mass contributions,
- NNLO in the large top quark mass limit,
- EW corrections given by Passarino et al
- **use exact solutions to the RG equations of soft, collinear and hard pieces** of the cross section.

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- EW corrections given by Passarino et al
- **use exact solutions to the RG equations of soft, collinear and hard pieces** of the cross section.

Good perturbative stability from LO onwards.

μ_R, μ_F and PDF dependence in Higgs production (8 TeV)

MSTW PDF set (σ in pb and errors($\pm$) in %):

VR, J. Smith

μ_R, μ_F and PDF dependence in Higgs production (8 TeV)

MSTW PDF set (σ in pb and errors($\pm$) in %):

VR, J. Smith

m_H	NNLO	μ_R	$\mu_{R,3}$	μ_F	μ	NNLO $_{\overline{\mu}}$	PDF	N ³ LO $_{sv}$	μ_R
123	18.99	+10.82 -10.41	+16.70 -16.04	-0.43 +0.53	+10.44 -9.93	20.97	+2.50 -3.12	19.79	+0.10 -2.32
124	18.68	+10.80 -10.39	+16.66 -16.01	-0.41 +0.51	+10.43 -9.94	20.62	+2.51 -3.12	19.46	+0.09 -2.28
125	18.37	+10.77 -10.37	+16.63 -15.99	-0.39 +0.50	+10.43 -9.94	20.28	+2.51 -3.13	19.13	+0.08 -2.24
126	18.07	+10.75 -10.35	+16.59 -15.96	-0.37 +0.47	+10.42 -9.94	19.95	+2.52 -3.13	18.82	+0.07 -2.19
127	17.78	+10.73 -10.33	+16.56 -15.93	-0.35 +0.45	+10.41 -9.95	19.63	+2.52 -3.13	18.51	+0.06 -2.15

μ_R, μ_F and PDF dependence in Higgs production (8 TeV)

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VR, J. Smith

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126	18.07	+10.75 -10.35	+16.59 -15.96	-0.37 +0.47	+10.42 -9.94	19.95	+2.52 -3.13	18.82	+0.07 -2.19
127	17.78	+10.73 -10.33	+16.56 -15.93	-0.35 +0.45	+10.41 -9.95	19.63	+2.52 -3.13	18.51	+0.06 -2.15

Uncertainty in NNLO result:

- μ_R variation ($m_h/2 < \mu_R < 2m_h$) gives 11%
- μ_R variation ($m_h/3 < \mu_R < 3m_h$) gives 17%
- μ_F variation ($m_h/2 < \mu_R < 2m_h$) gives 0.5%
- $\mu_R = \mu_F = 1/2m_h$ resummes soft gluons
- MSTW PDF gives 3%
- N³LO $_{sv}$ gives around 3%

μ_R, μ_F and PDF dependence in Higgs production (8 TeV)

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μ_R, μ_F and PDF dependence in Higgs production (8 TeV)

ABM PDF set: (σ in pb and errors($\pm$) in %):

VR, J. Smith

m_H	NNLO	μ_R	$\mu_{R,3}$	μ_F	μ	NNLO $_{\overline{\mu}}$	PDF	N ³ LO $_{sv}$	μ_R
123	17.58	+10.13 -9.86	+15.59 -15.25	-0.18 +0.33	+9.91 -9.63	19.33	± 4.40	19.97	+0.10 -2.25
124	17.29	+10.11 -9.85	+15.57 -15.23	-0.16 +0.31	+9.90 -9.64	19.00	± 4.43	19.63	+0.09 -2.21
125	16.99	+10.08 -9.83	+15.52 -15.20	-0.12 +0.28	+9.91 -9.65	18.67	± 4.75	19.28	+0.12 -2.15
126	16.71	+10.06 -9.81	+15.49 -15.17	-0.13 +0.25	+9.87 -9.66	18.36	± 4.54	18.96	+0.13 -2.11
127	16.43	+10.04 -9.79	+15.46 -15.15	-0.03 +0.27	+9.96 -9.63	18.07	± 4.26	18.64	+0.14 -2.06

μ_R, μ_F and PDF dependence in Higgs production (8 TeV)

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Uncertainty in NNLO result:

- μ_R variation ($m_h/2 < \mu_R < 2m_h$) gives 10%
- μ_R variation ($m_h/3 < \mu_R < 3m_h$) gives 17%
- μ_F variation ($m_h/2 < \mu_R < 2m_h$) gives 0.5%
- $\mu_R = \mu_F = 1/2m_h$ resummes soft gluons
- ABM PDF gives 5%
- N³LO $_{sv}$ gives around 2% due to μ_R

PDF dependence in Higgs production (8 TeV)

VR, J. Smith

PDF dependence in Higgs production (8 TeV)

Different PDF sets (m_h in GeV and cross sections in pb): *VR, J. Smith*

m_h	NNLO				N^3LO_{sv}			
	MSTW	ABM	CT	NNPDF	MSTW	ABM	CT	NNPDF
120	19.98	18.51	19.86	21.00	20.83	21.04	20.26	20.91
121	19.64	18.18	19.52	20.65	20.47	20.62	19.91	20.56
122	19.31	17.89	19.20	20.30	20.13	20.32	19.57	20.21
123	18.99	17.58	18.88	19.96	19.79	19.97	19.24	19.87
124	18.68	17.29	18.57	19.63	19.46	19.63	18.92	19.54
125	18.37	16.99	18.27	19.31	19.13	19.28	18.61	19.21
126	18.07	16.71	17.97	18.99	18.82	18.96	18.31	18.89
127	17.78	16.43	17.68	18.66	18.51	18.64	18.01	18.53
128	17.49	16.16	17.39	18.52	18.21	18.32	17.72	18.61
129	17.21	15.91	17.12	18.09	17.91	18.04	17.43	17.99

PDF dependence in Higgs production (8 TeV)

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128	17.49	16.16	17.39	18.52	18.21	18.32	17.72	18.61
129	17.21	15.91	17.12	18.09	17.91	18.04	17.43	17.99

- ABM is 7.4% smaller than MSTW
- CT is just 0.5% smaller than MSTW
- NNPDF is 5% larger than MSTW
- All PDFs give almost same results for N^3LO_{sv} corrected cross section.

Soft gluons at N^3LO_{pSV} for Higgs production (8 TeV)

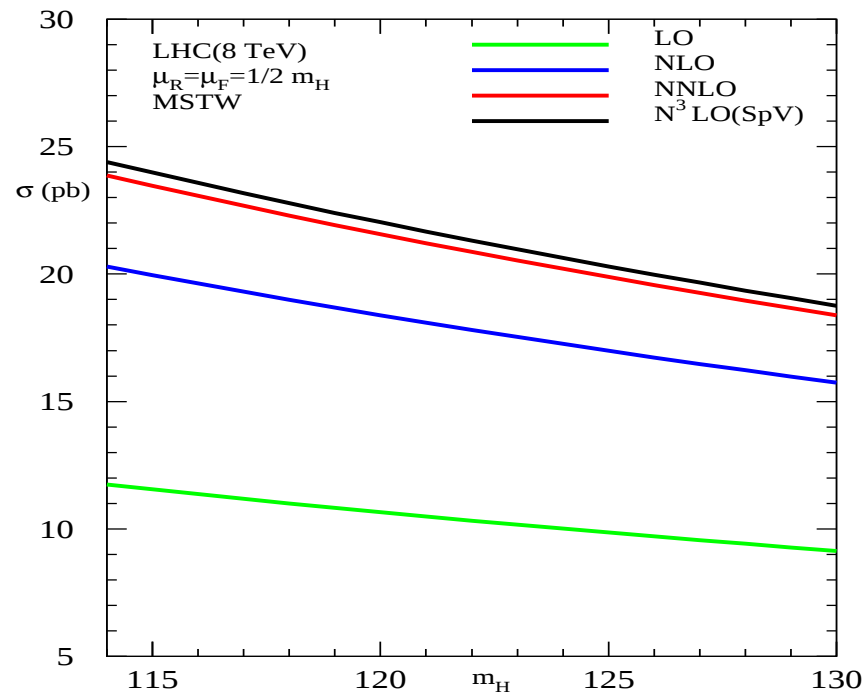
VR, J. Smith

$$R = \frac{\sigma_{N^3LO}(\mu)}{\sigma_{N^3LO}(\mu_0)}$$

Soft gluons at N^3LO_{pSV} for Higgs production (8 TeV)

VR, J. Smith

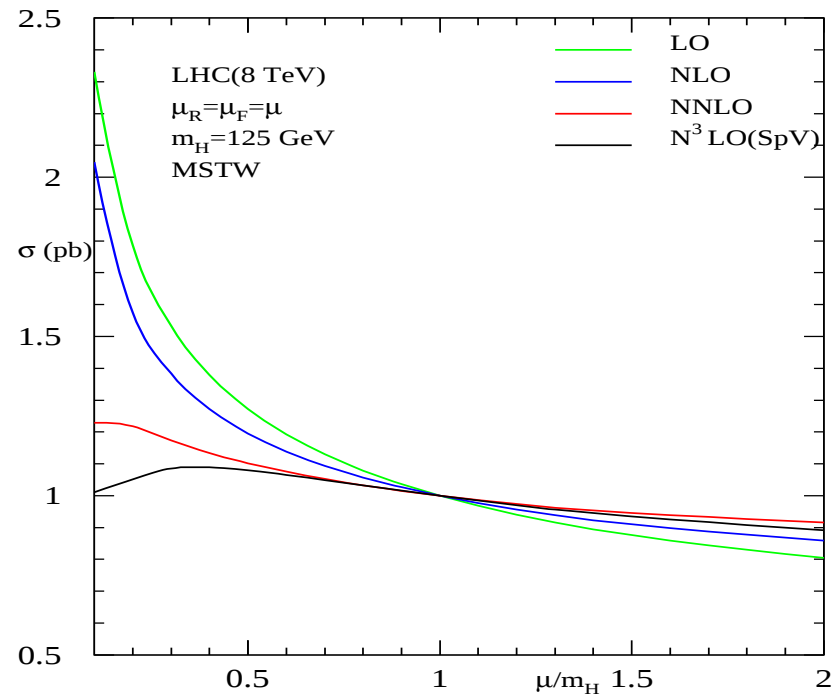
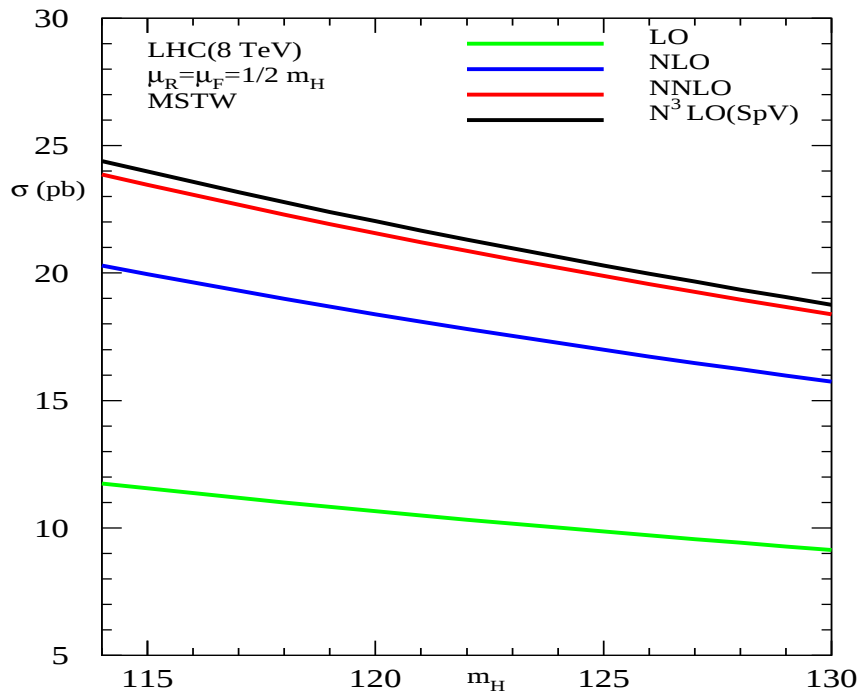
$$R = \frac{\sigma_{N^iLO}(\mu)}{\sigma_{N^iLO}(\mu_0)}$$



Soft gluons at N^3LO_{pSV} for Higgs production (8 TeV)

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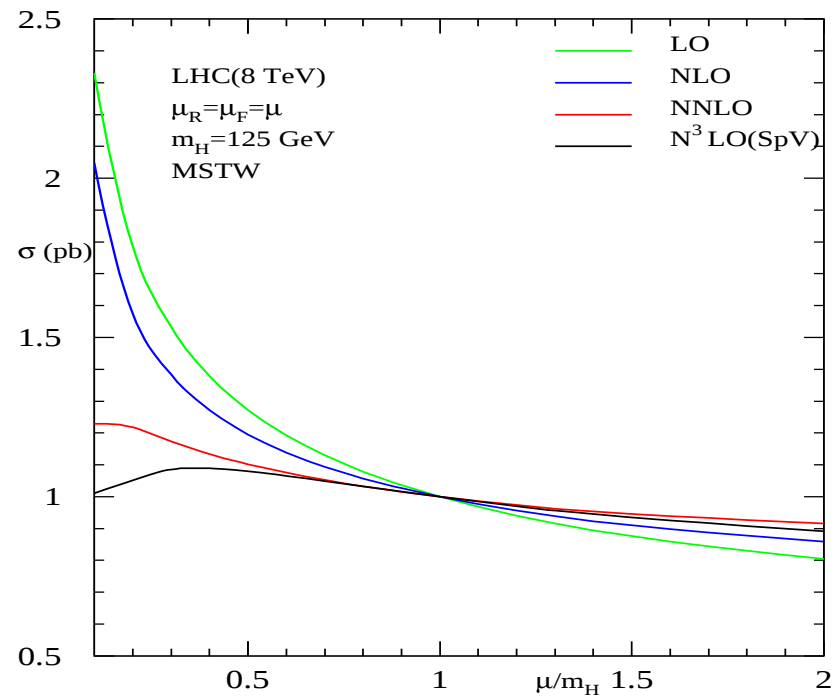
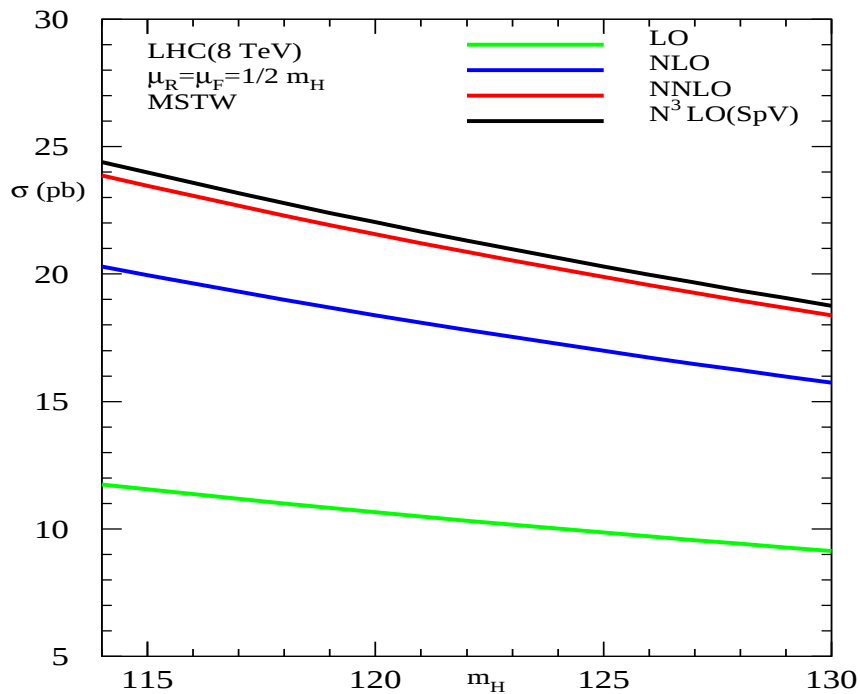
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Soft gluons at N^3LO_{pSV} for Higgs production (8 TeV)

VR, J. Smith

$$R = \frac{\sigma_{N^iLO}(\mu)}{\sigma_{N^iLO}(\mu_0)}$$



- NLO increases the cross section by 80%,
- NNLO to 30%,
- resummation to 10% and electroweak effects by 5%

Update-1: Anastasiou-Boughezal-Petriello-Stoeckli:

Update-1: Anastasiou-Boughezal-Petriello-Stoeckli:

- Exact NLO cross section with full dependence on the top- and bottom-quark masses
- NNLO cross section-Effective Field Theory, i.e., in the large- m_t limit
- EW contributions evaluated in the complete factorization scheme

$$\sigma = \sum_{i=0}^{\infty} \alpha_s^i \sigma_{QCD}^{(i)} \otimes (1 + \delta_{EW})$$

- Mixed QCD-EW contributions are also accounted for, together with some effects from EW corrections at finite transverse momentum.
- The effect of soft-gluon resummation is mimicked by choosing the central value of the renormalization and factorization scales as $\mu_R = \mu_F = M_H/2$.

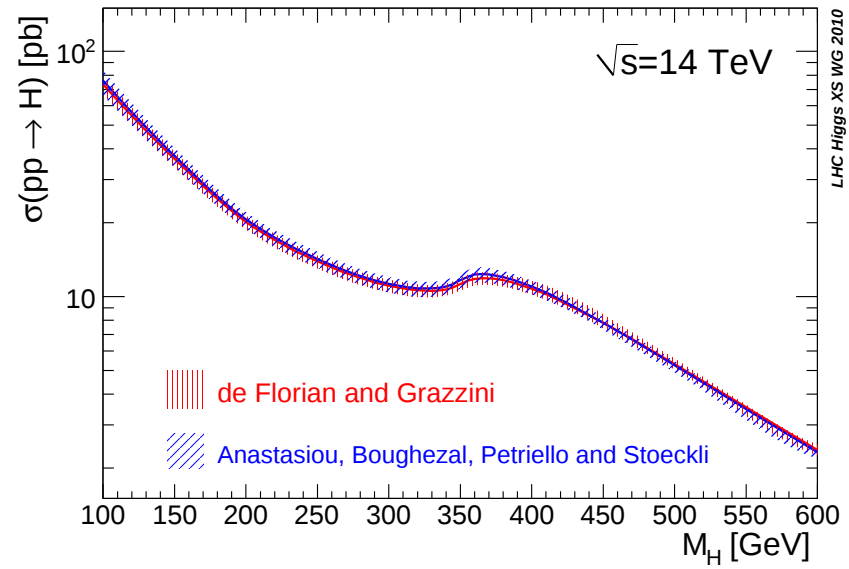
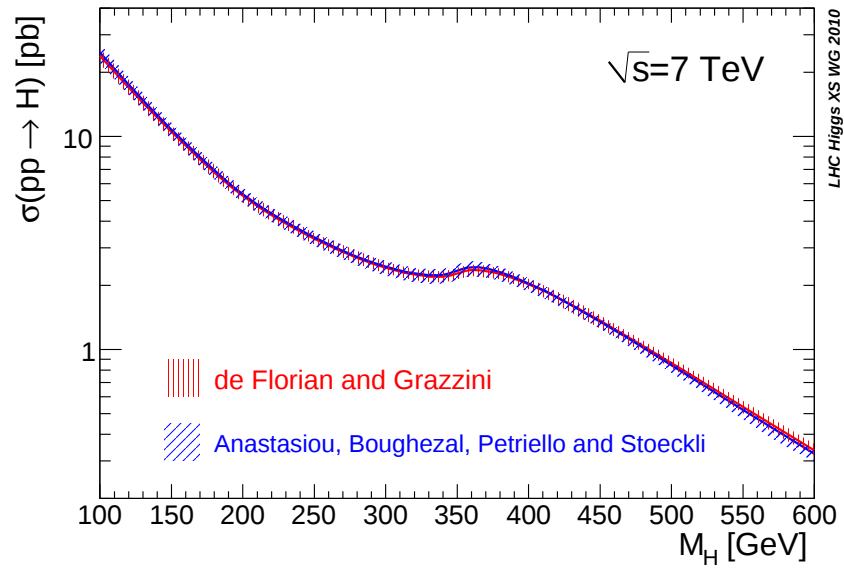
Update-2: de Florian-Grazzini:

Update-2: de Florian-Grazzini:

- Exact NLO cross section with full dependence on the top- and bottom-quark masses, computed with the program HIGLU,
- the NLL resummation of soft-gluons,
- the NNLL+NNLO corrections are consistently added in the large- m_t limit
- corrected for EW contributions in the complete factorization scheme.
- The central value of factorization and renormalization scales is chosen to be $\mu_F = \mu_R = M_H$

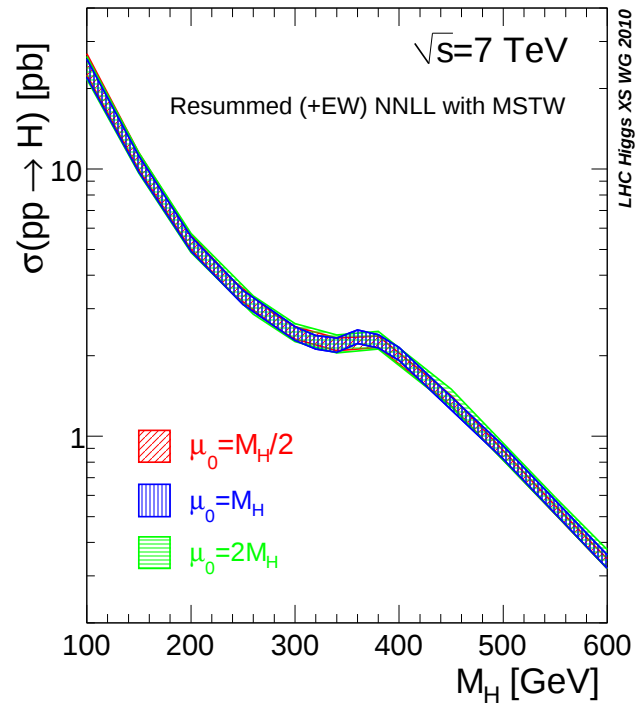
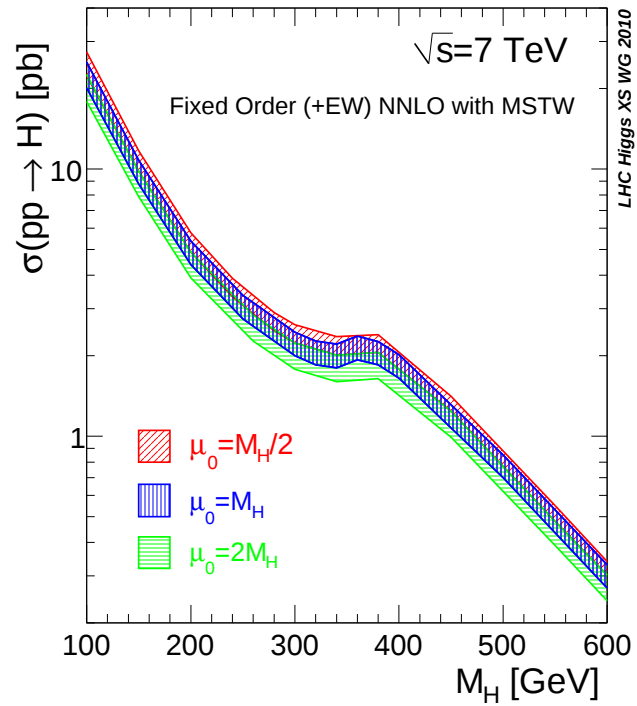
Comparison

Comparison



Fixed vs Resummed at 7 TeV

Fixed vs Resummed at 7 TeV



- Comparison of NNLO and NNLL bands with different choice of the central scale.

Final numbers for gluon fusion for $m_h = 125$ GeV

Final numbers for gluon fusion for $m_h = 125$ GeV

Production cross section at $\sqrt{s} = 7$ TeV with $\text{scale}(\mu_R = \mu_F)$ and $\text{PDF}(+\alpha_s)$ uncertainties:

$$\sigma = 15.31_{-7.8\%}^{+11.7\%}(\text{scale})_{-7.3\%}^{+7.8\%}(\text{PDF} + \alpha_s)pb$$

Production cross section at $\sqrt{s} = 8$ TeV:

- de Florian et al:

$$\sigma = 19.52_{-7.8\%}^{+7.2\%}(\text{scale})_{-6.9\%}^{+7.5\%}(\text{PDF} + \alpha_s)pb$$

- Anastasiou et al:

$$\sigma = 20.69_{-9.3\%}^{+8.4\%}(\text{scale})_{-7.5\%}^{+7.8\%}(\text{PDF} + \alpha_s)pb$$

Towards N^3LO corrected Higgs cross section

Anastasiou et.al

Towards N^3LO corrected Higgs cross section

Anastasiou et.al

- Square of one-loop virtuals to N^3LO

$$g(p_1) + g(p_2) \rightarrow g(p_3) + H(p_4)$$

$$q(p_1) + g(p_2) \rightarrow q(p_3) + H(p_4)$$

$$q(p_1) + \bar{q}(p_2) \rightarrow g(p_3) + H(p_4)$$

Towards N^3LO corrected Higgs cross section

Anastasiou et.al

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$$q(p_1) + \bar{q}(p_2) \rightarrow g(p_3) + H(p_4)$$

- Performing a loop-expansion of the amplitudes

$$\mathcal{A}_X = \sum_{j=0}^{\infty} \mathcal{A}_X^{(j)}$$

in the effective theory with j being the number of loops, we have:

$$|\mathcal{A}_X|^2 = \left| \mathcal{A}_X^{(0)} \right|^2 + 2\Re \left(\mathcal{A}_X^{(0)} \mathcal{A}_X^{(1)*} \right) + \left[\left| \mathcal{A}_X^{(1)} \right|^2 + 2\Re \left(\mathcal{A}_X^{(0)} \mathcal{A}_X^{(2)*} \right) \right] + \dots$$

Towards N^3LO corrected Higgs cross section

Anastasiou et.al

- Square of one-loop virtuals to N^3LO

$$g(p_1) + g(p_2) \rightarrow g(p_3) + H(p_4)$$

$$q(p_1) + g(p_2) \rightarrow q(p_3) + H(p_4)$$

$$q(p_1) + \bar{q}(p_2) \rightarrow g(p_3) + H(p_4)$$

- Performing a loop-expansion of the amplitudes

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$$\sigma_X^{1\otimes 1} = s^{-1-\varepsilon} \frac{\mathcal{N}_X (4\pi)^\varepsilon}{16\pi \Gamma(1-\varepsilon)} \delta^{1-2\varepsilon} \int_0^1 d\lambda [\lambda (1-\lambda)]^{-\varepsilon} \sum \left| \mathcal{A}_X^{(1)} \right|^2.$$

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- Reverse Unitarity and Integration parts lead to 19 master integrals
- Differential equation method is used to solve the master integrals

Alternate approach towards N^3LO

Kilgore

Alternate approach towards N^3LO

Kilgore

- Threshold expansion
- Square of the one-loop contribution to the cross section as an extended threshold expansion.
- Obtain enough terms to invert the series and determine the closed functional form through order ϵ .
- The method has been applied to get earlier results at NLO and NNLO level for inclusive cross sections in closed form, in terms of G-functions and the hypergeometric functions ${}_2F_1$ and ${}_3F_2$.
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$${}_2F_1(1, -\varepsilon; 1 - \varepsilon; -xy/\bar{y}) = \sum_{n=0}^{\infty} \frac{\bar{x}}{n!} \frac{(-\varepsilon)_n}{n!} \left({}_2F_1(1, -\varepsilon, 1 - \varepsilon, -y/\bar{y}) - \bar{y} \sum_{m=0}^{n-1} y^m \frac{m!}{(1 - \varepsilon)_m} \right)$$

Higgs with 0, 1, 2 jets

Petriello et al

Higgs with 0, 1, 2 jets

Petriello et al

- σ_{tot} - Inclusive cross section
- $\sigma_0(p_T^{\text{cut}})$ - the 0-jet cross section: no jets with $p_T^{\text{jet}} > p_T^{\text{cut}}$ NNLO in QCD
- $\sigma_{\geq 1}(p_T^{\text{cut}})$ - the inclusive 1-jet cross section, with at least 1 jet with $p_T^{\text{jet}} > p_T^{\text{cut}}$ in QCD NLO
- $\sigma_1([p_{Ta}, p_{Tb}]; p_T^{\text{cut}})$ - the exclusive 1-jet cross section, with $p_{Tb} > p_{TJ} > p_{Ta}$ NLO
- $\sigma_{\geq 2}(p_T^{\text{cut}})$ - the inclusive 2-jet cross section, with at least 2 jets with $p_T^{\text{jet}} > p_T^{\text{cut}}$ LO

Consistency conditions:

$$\sigma_{\text{tot}} = \sigma_0(p_T^{\text{cut}}) + \sigma_{\geq 1}(p_T^{\text{cut}}),$$

$$\sigma_{\geq 1}(p_T^{\text{cut}}) = \sigma_1([p_T^{\text{cut}}, \infty]; p_T^{\text{cut}}) + \sigma_{\geq 2}(p_T^{\text{cut}}).$$

- This leads to correlated errors

Theory Uncertainties

Petriello et al

Theory Uncertainties

Petriello et al

rate [pb]	ATLAS ($p_T^{\text{cut}} = 25\text{GeV}$, $R = 0.4$)	CMS ($p_T^{\text{cut}} = 30\text{GeV}$, $R = 0.5$)
$\sigma_{\text{tot}}^{\text{NNLO}}$	19.27 ± 1.50	19.27 ± 1.50
$\sigma_{\geq 1}^{\text{NLO}}$	7.85 ± 1.41	6.47 ± 1.27
$\sigma_{\geq 2}^{\text{LO}}$	2.42 ± 1.80	1.73 ± 1.31
σ_0^{NNLO}	11.69 ± 2.06	12.80 ± 1.97
σ_1^{NLO}	5.16 ± 2.29	4.75 ± 1.82

- Fixed order cross sections and their uncertainties for ATLAS and CMS parameters. The central scale is $\mu = m_H/2$.

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Petriello et al

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rate [pb]	ATLAS ($p_T^{\text{cut}} = 25\text{GeV}, R = 0.4$)	CMS ($p_T^{\text{cut}} = 30\text{GeV}, R = 0.5$)
σ_{tot}	21.69 ± 1.49	21.69 ± 1.49
σ_0	$12.67 \pm 0.87_{\mu} \pm 0.86_{\text{res}} (\pm 1.22_{\text{tot}})$	$13.86 \pm 0.70_{\mu} \pm 0.52_{\text{res}} (\pm 0.87_{\text{tot}})$
σ_1	$5.68 \pm 0.30_{\mu} \pm 0.89_{\text{res}} (\pm 0.94_{\text{tot}})$	$4.97 \pm 0.43_{\mu} \pm 0.61_{\text{res}} (\pm 0.74_{\text{tot}})$
$\sigma_{\geq 2}$	$3.34 \pm 0.32_{\mu} \pm 0.47_{\text{res}} (\pm 0.57_{\text{tot}})$	$2.86 \pm 0.36_{\mu} \pm 0.44_{\text{res}} (\pm 0.57_{\text{tot}})$

- The total, 0-jet, 1-jet, and inclusive 2-jet cross sections and their uncertainties.

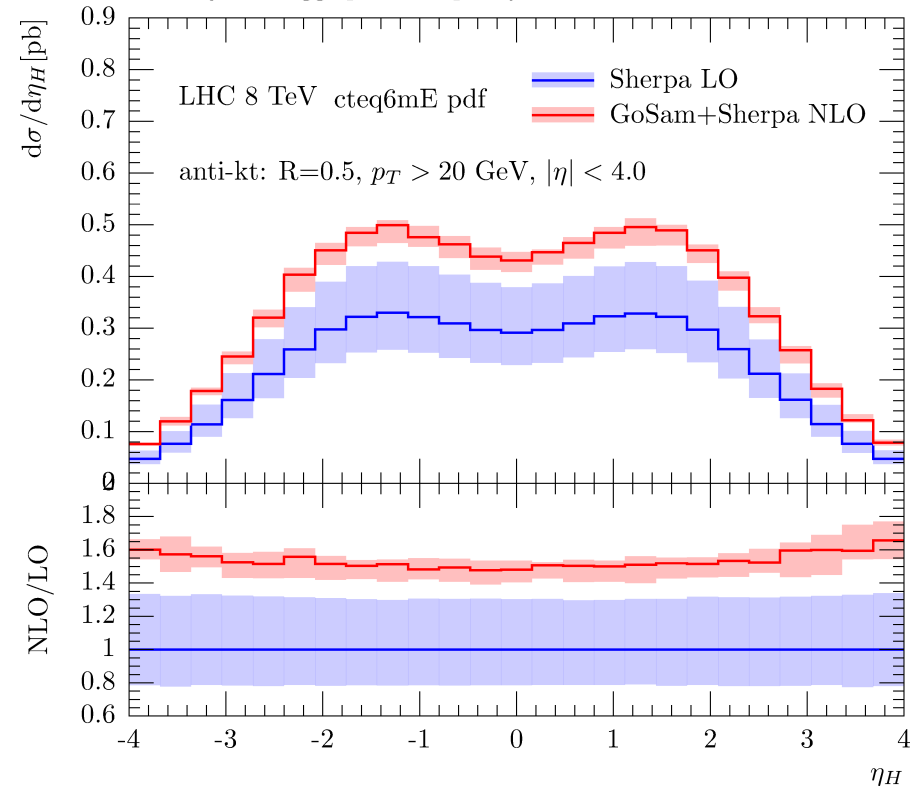
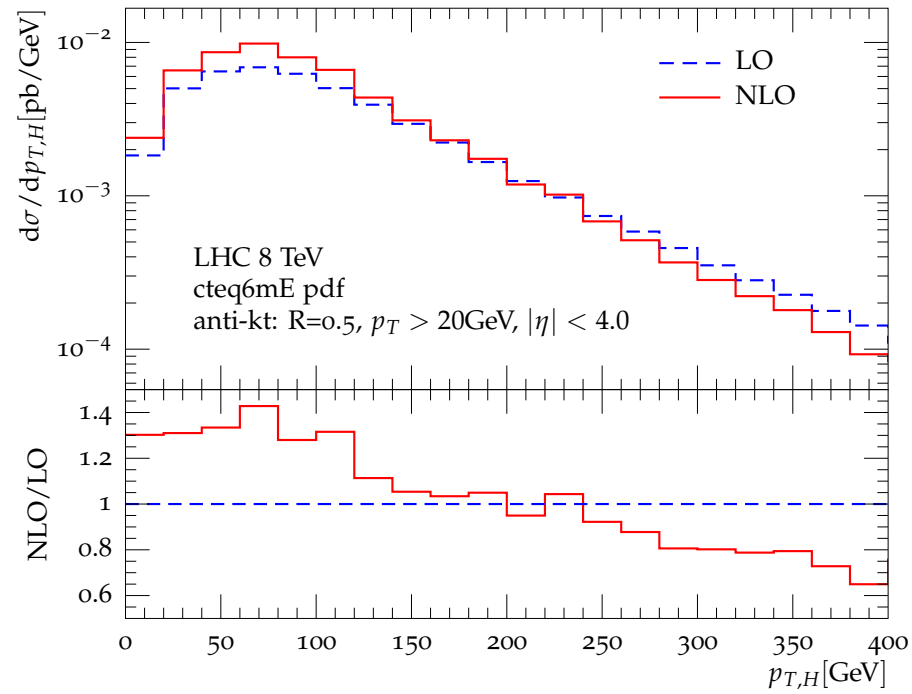
Higgs + 2 jets at NLO

H. van Deurzen et al.

Higgs + 2 jets at NLO

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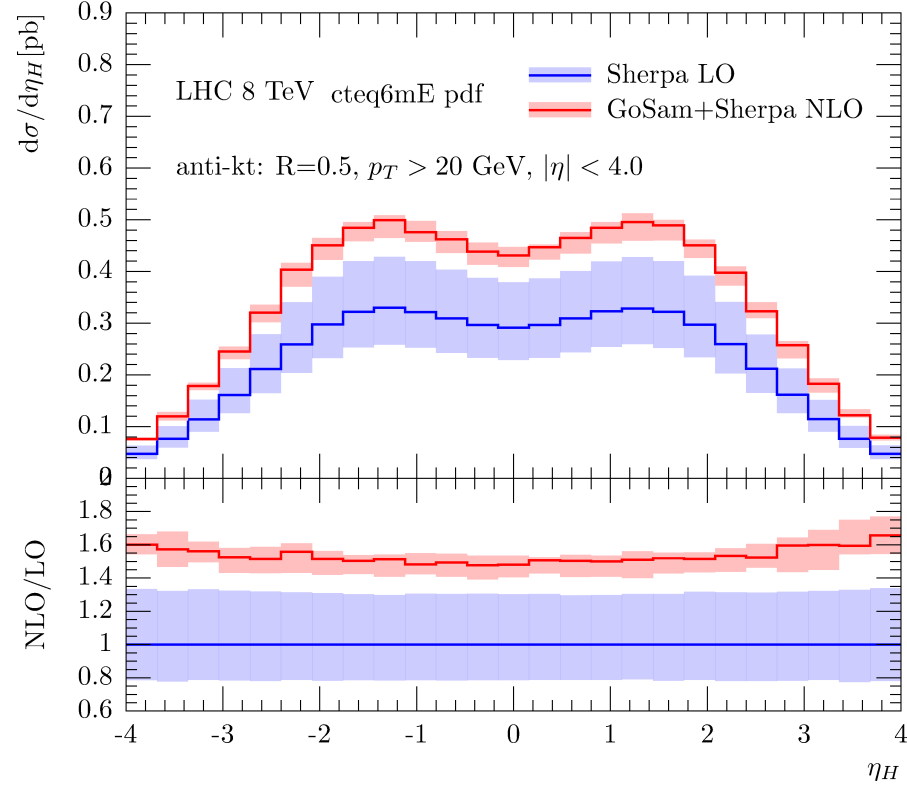
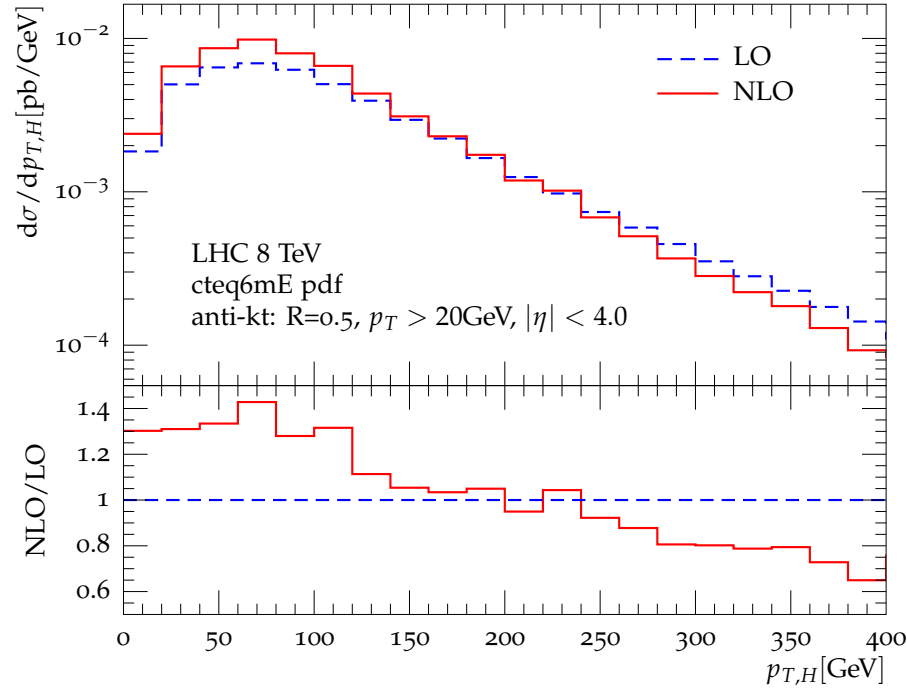
$H + 2$ jets: Higgs pseudorapidity



Higgs + 2 jets at NLO

H. van Deurzen et al.

$H + 2$ jets: Higgs pseudorapidity



- Transverse momentum p_T and Pseudorapidity η of the Higgs boson are plotted.
- The jets are clustered by using the anti- k_T algorithm provided by the FastJet package:

$$p_{t,j} \geq 20 \text{ GeV}, \quad |\eta_j| \leq 4.0, \quad R = 0.5.$$

- The factorization and the renormalization scale are set to be

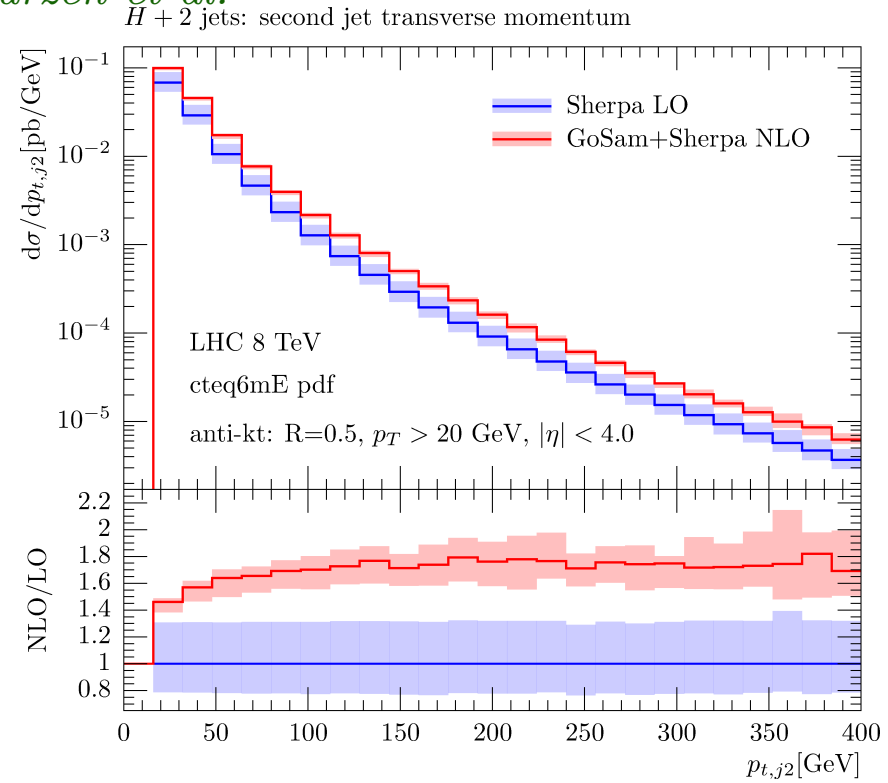
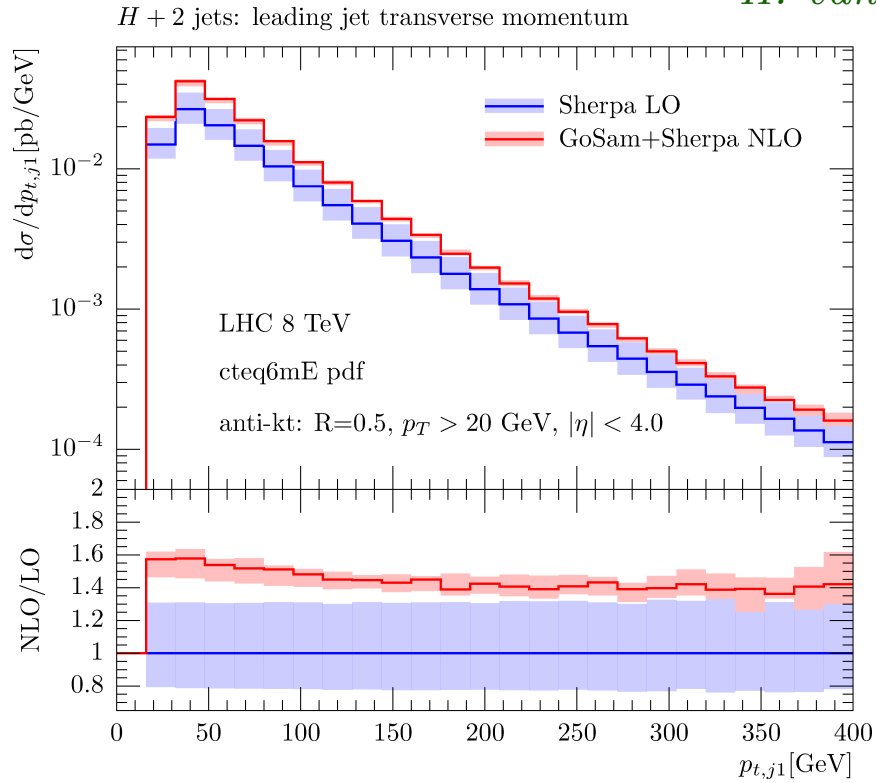
$$\hat{H}_t = \sqrt{M_H^2 + p_{t,H}^2} + \sum_j p_{t,j}.$$

Higgs + 2 jets at NLO

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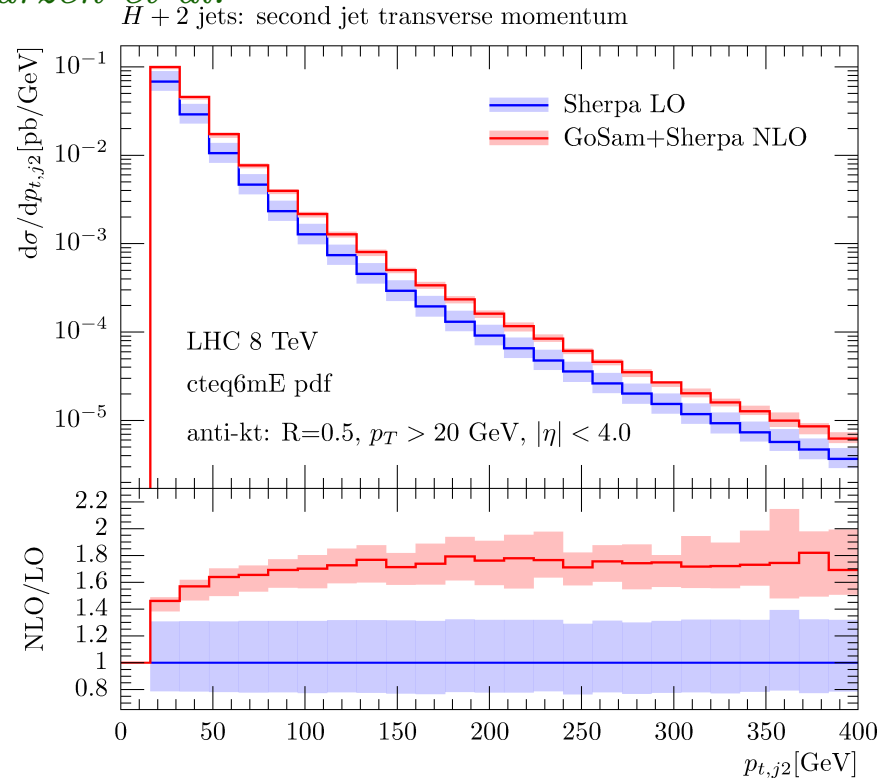
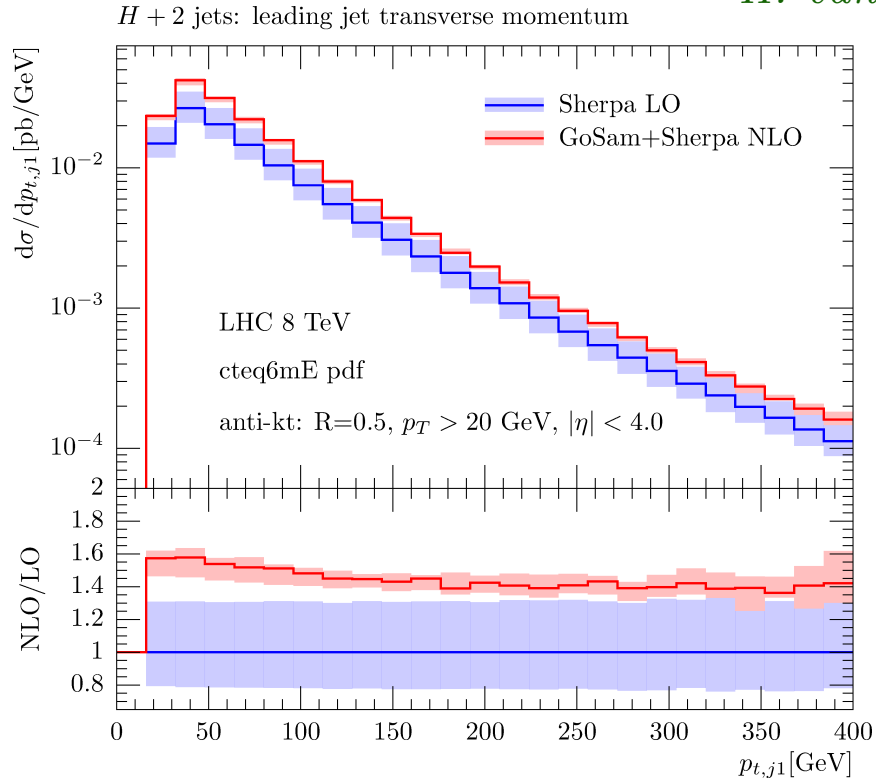
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Higgs + 2 jets at NLO

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- Transverse momentum p_T of the first and the second jet.

$$\sigma_{\text{LO}} [\text{pb}] = 1.90^{+0.58}_{-0.41}, \quad \sigma_{\text{NLO}} [\text{pb}] = 2.90^{+0.05}_{-0.20},$$

- Scale variation:

$$\frac{1}{2} \hat{H}_t < \mu < 2 \hat{H}_t.$$

GOSAM framework

G. Heinrich et al.

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- GoSam performs one-loop virtual contributions to physical processes automatically.
- Amplitudes are generated via Feynman diagrams, using QGRAF, FORM, SPINNEY and HAGGIES.
- The input required:
 - the *process*, such as a list of initial and final state particles, the order in the coupling constants, and the model;
 - the *scheme* employed, such as the regularization and renormalization schemes;
 - the *system* , such as paths to libraries or compiler options;
 - optional information to control the code generation.
- the virtual corrections are evaluated using the d -dimensional integrand-level reduction method, as implemented in SAMURAI library, which allows for the combined determination of both cut-constructible and rational terms at once.
- Embedding the virtual corrections within a Monte Carlo framework (MC), such as SHERPA, POWHEG, MADGRAPH, HERWIG, or aMC@NLO, that can take care of the phase-space integration and showering.

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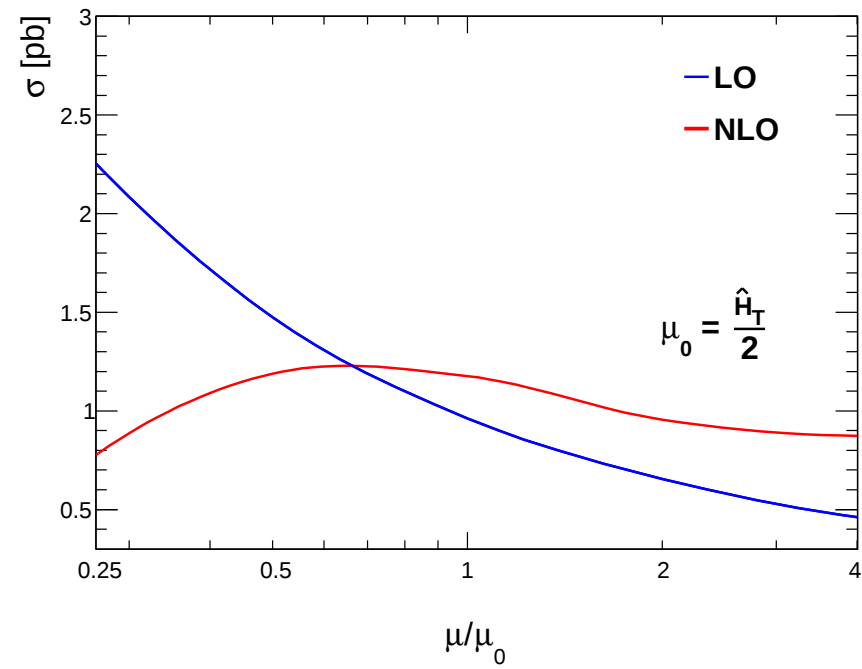
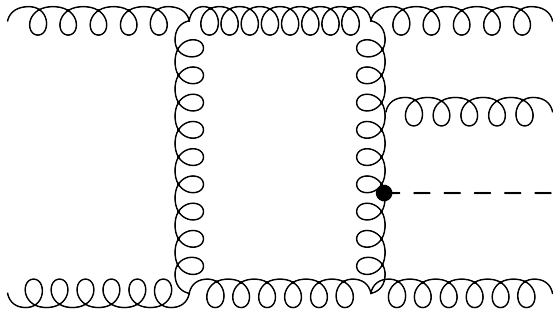
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Higgs + 3-jets in gluon-gluon fusion

G. Cullen et al.

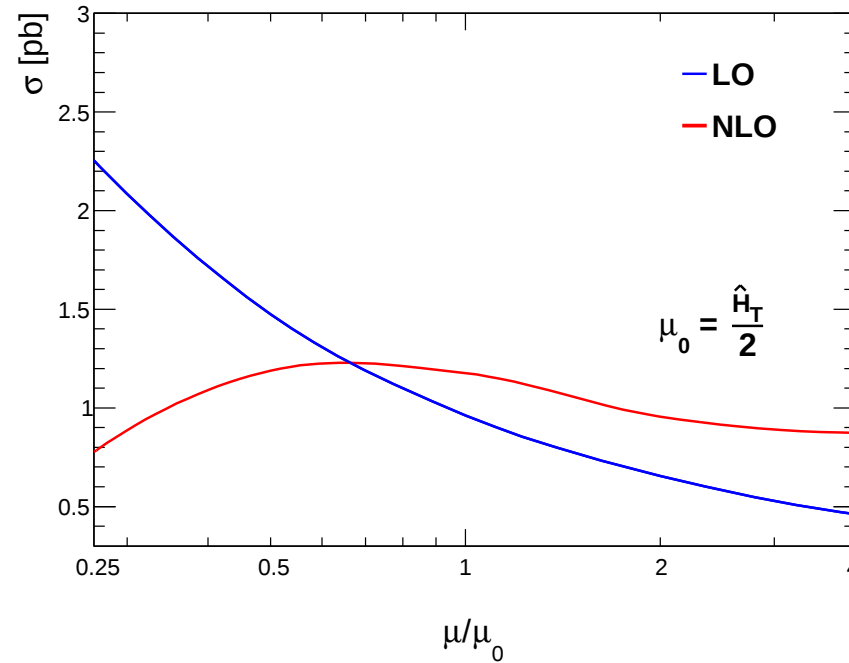
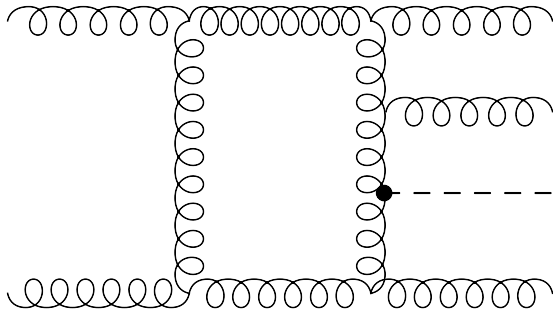
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- Jets are clustered using the anti- k_t -algorithm implemented in FastJet with radius $R = 0.5$ and a minimum transverse momentum of $p_{T,jet} > 20$ GeV and pseudorapidity $|\eta| < 4.0$.
- The renormalization and factorization scales are set to

$$\mu_F = \mu_R = \frac{\hat{H}_T}{2} = \frac{1}{2} \left(\sqrt{m_H^2 + p_{T,H}^2} + \sum_i |p_{T,i}| \right),$$

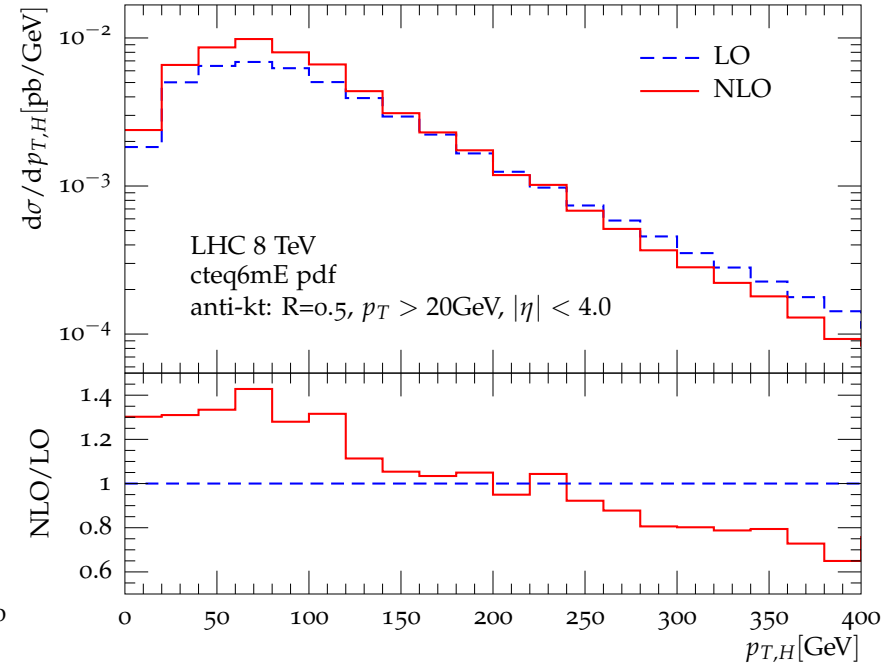
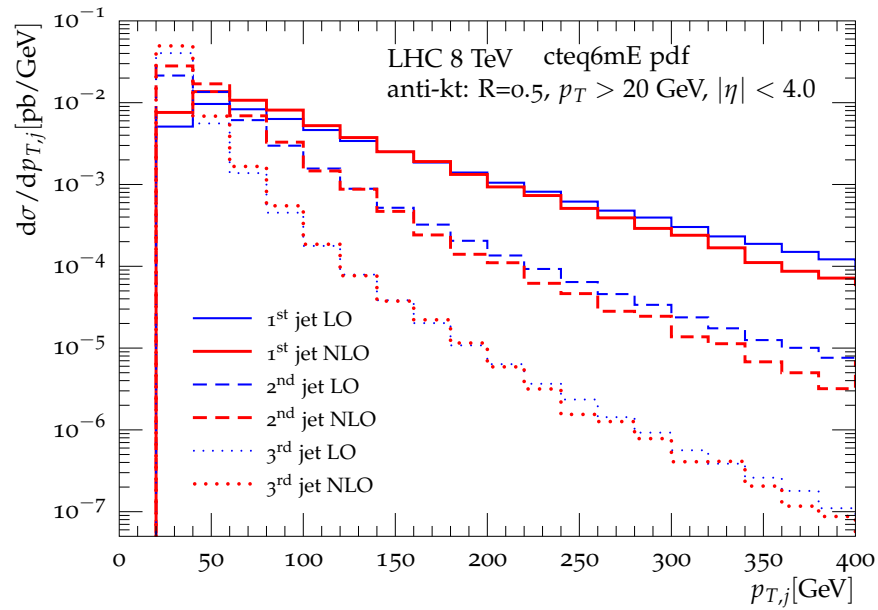
- The strong coupling is therefore evaluated at different scales according to $\alpha_s^5 \rightarrow \alpha_s^2(m_H)\alpha_s^3(\hat{H}_T/2)$.

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G. Cullen et al.

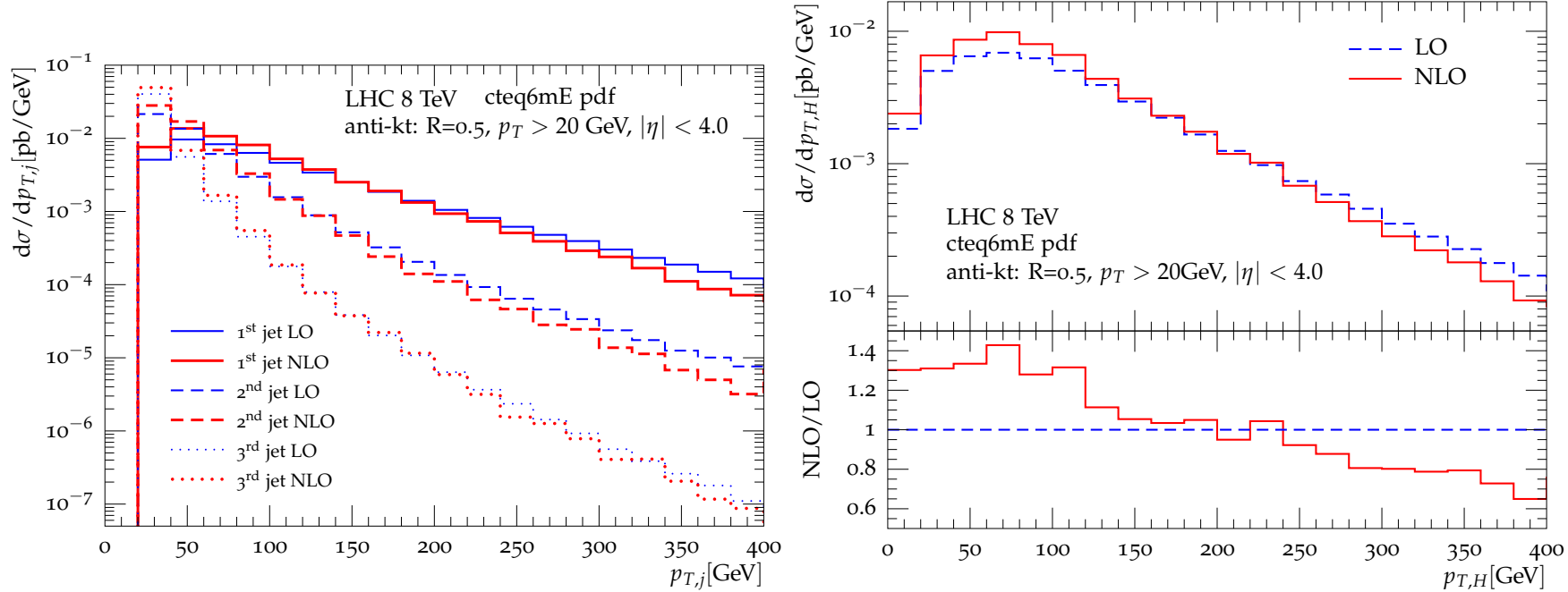
Higgs + 3-jets in gluon-gluon fusion

G. Cullen et al.



Higgs + 3-jets in gluon-gluon fusion

G. Cullen et al.



- Transverse momentum (p_T) distributions for the first, second, and third leading jet and the Higgs boson
- The theoretical uncertainties are estimated by varying the scales by factors of 0.5 and 2.0.
- In the effective coupling the scale is kept at m_H .

$$\sigma_{LO}[\text{pb}] = 0.962^{+0.51}_{-0.31}, \quad \sigma_{NLO}[\text{pb}] = 1.18^{+0.01}_{-0.22}.$$

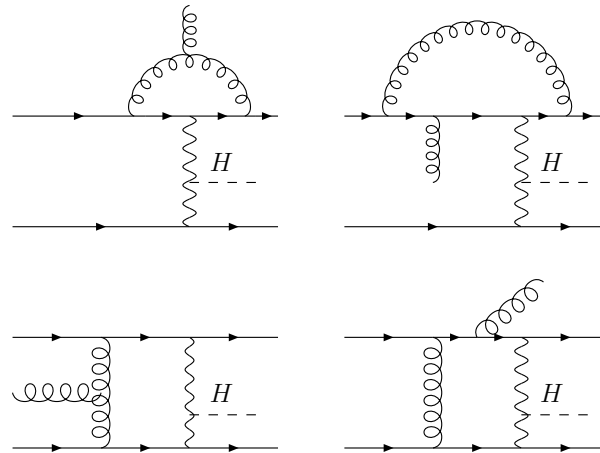
- The scale dependence of the total cross section is strongly reduced by the inclusion of the NLO contributions.

Higgs + 3-jets via vector boson fusion (VBF)

F. Campanario et al.

Higgs + 3-jets via vector boson fusion (VBF)

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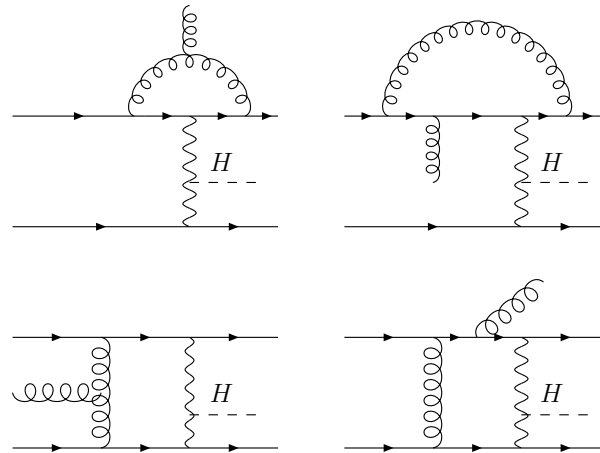
- Higgs production via Vector Boson Fusion (VBF) can disentangle the Higgs boson's coupling to fermions and gauge bosons.
- Tagging two jets with Higgs and vetoing soft jets in the central region can significantly reduce the QCD background as well as Higgs plus two jets from gluon-gluon fusion.
- Ratio of Higgs+3 jets to Higgs+2 jets need to be known accurately.

Method:

- Spin helicity package MATCHBOX provides real emission amplitudes, spin summation, subtraction terms for IR singularities
- ColorFull and ColorMath packages to do color algebra
- Passarino-Veltman reduction and Denner-Dittmaier scheme to do one-loop reduction and evaluation.

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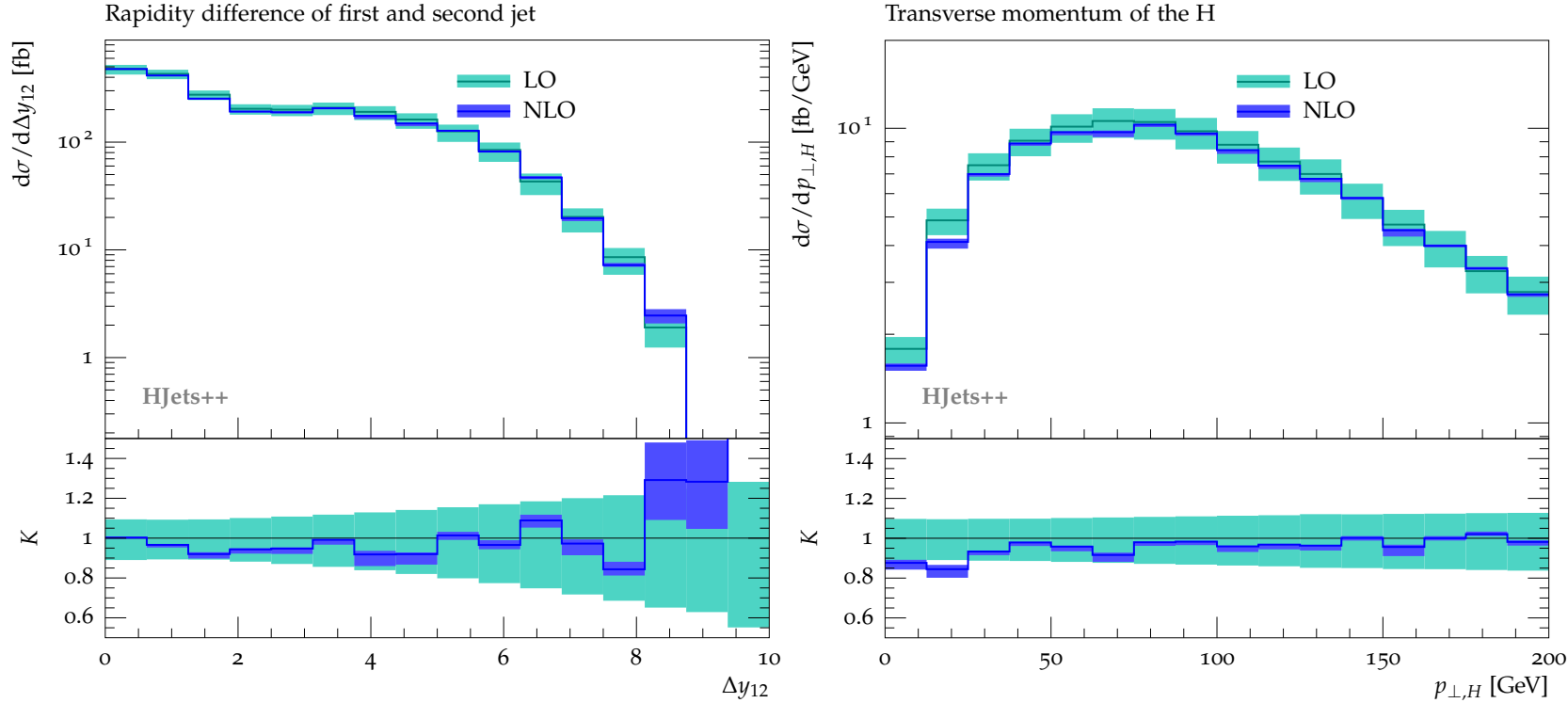
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Higgs+3 jets via VBF

F. Campanario et al.

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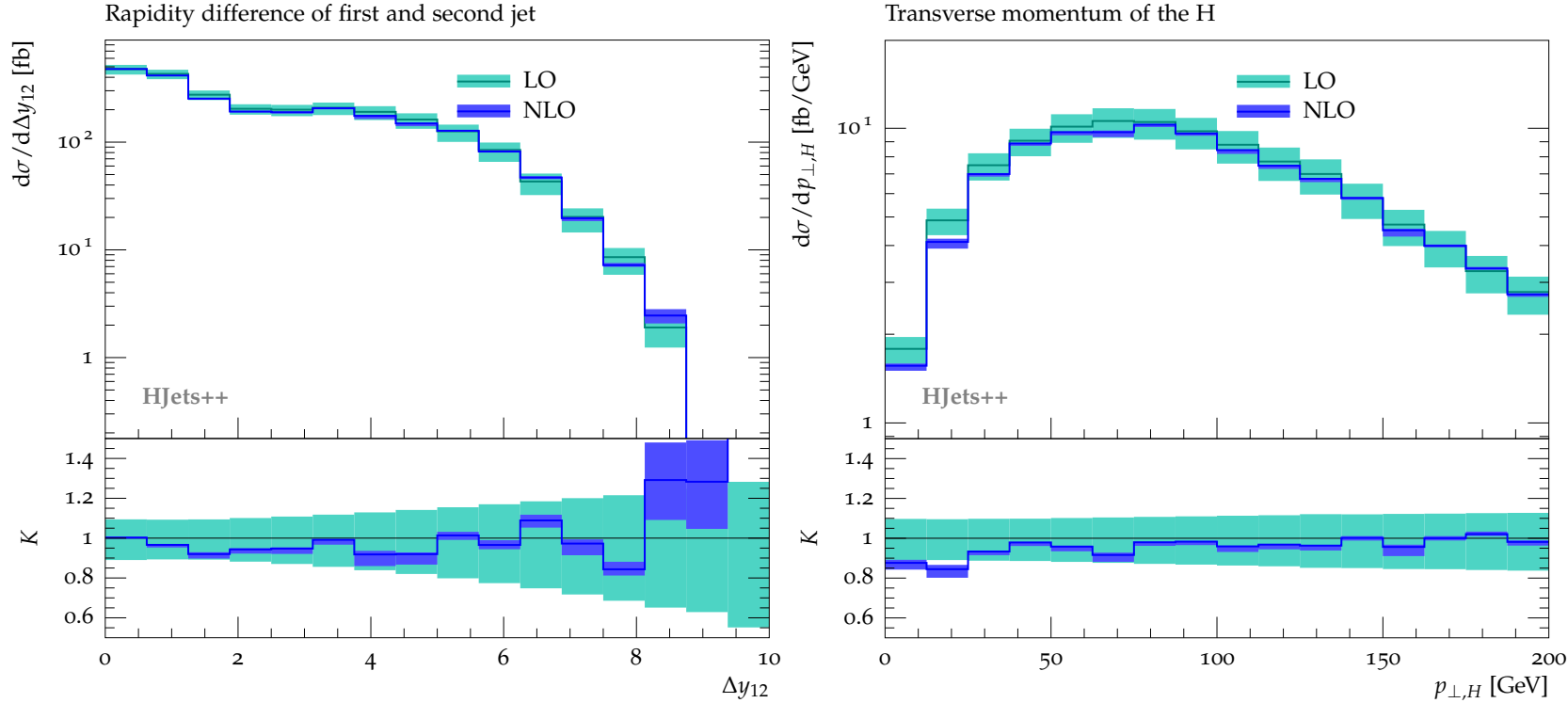
F. Campanario et al.



- Cluster jets with the anti- k_T algorithm using FastJet with $D = 0.4$, E -scheme recombination and require at least three jets with transverse momentum $p_{T,j} \geq 20$ GeV and rapidity $|y_j| \leq 4.5$. Jets are ordered in decreasing transverse momenta.
- The bands correspond to varying $\mu_F = \mu_R$ by factors 1/2 and 2 around the central value $H_T/2$.
- Differential cross section and K factor for the p_T of the Higgs. The bands correspond to varying $\mu_F = \mu_R$ by factors 1/2 and 2 around the central value $H_T/2$.

Higgs+3 jets via VBF

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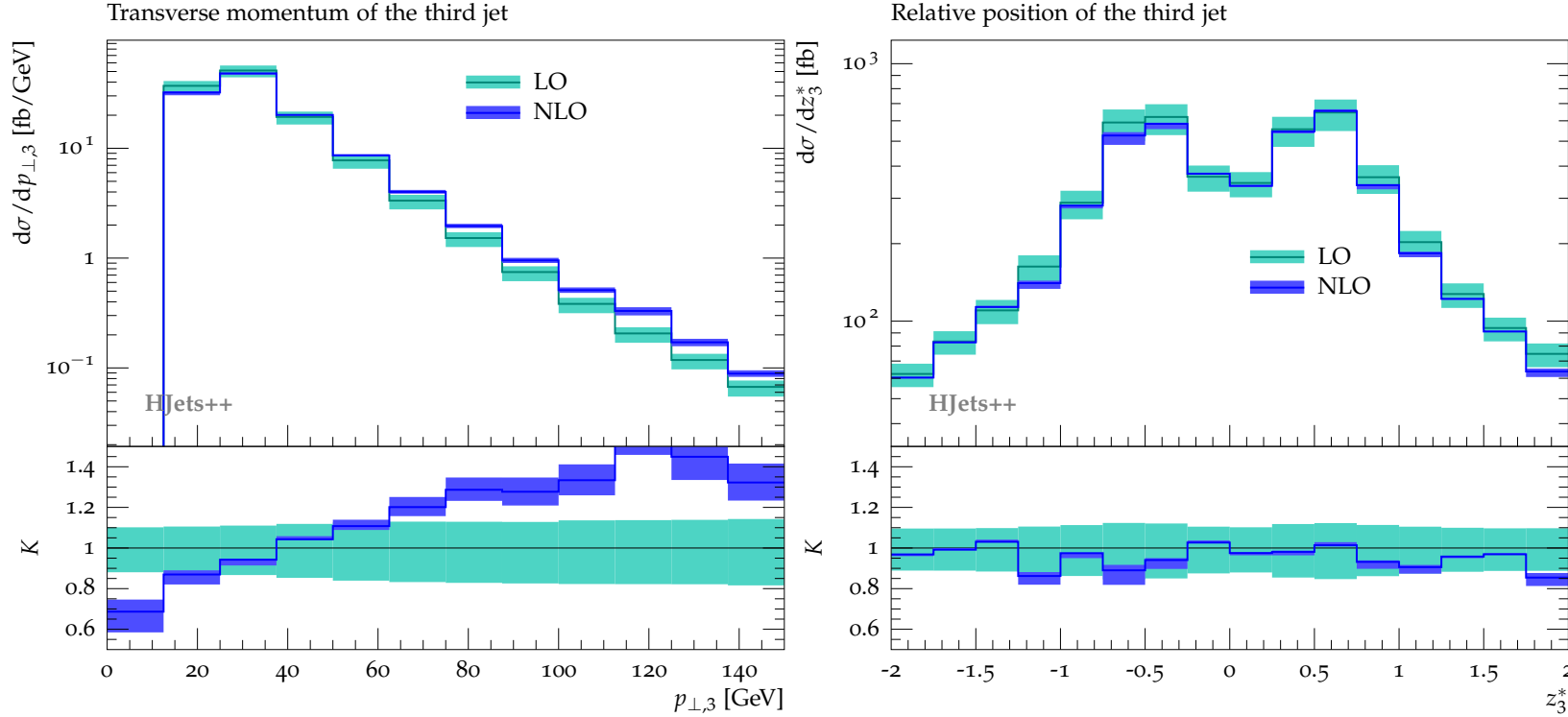
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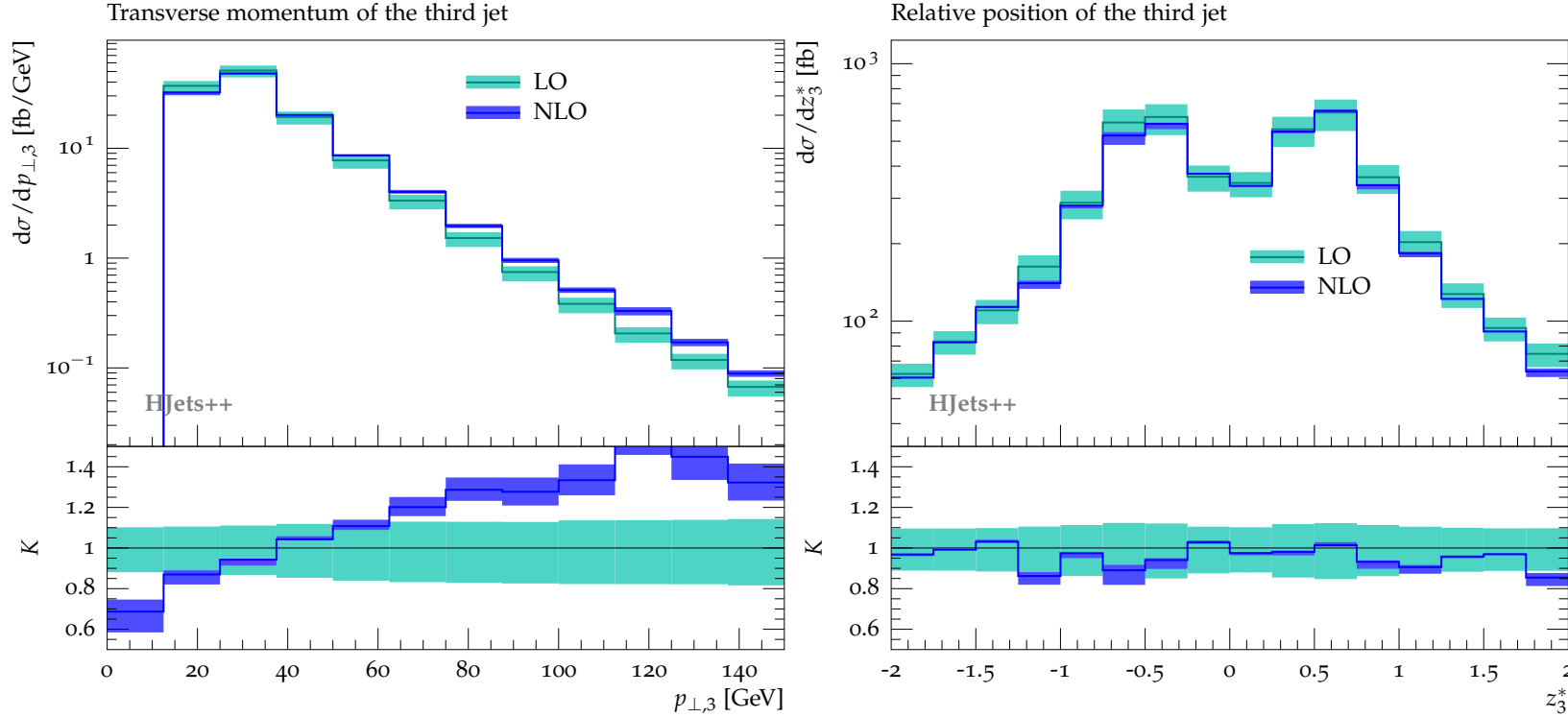
F. Campanario et al.



- Differential cross section and K factor for the p_T of the third hardest jet.
- Differential cross section and K factor for the normalized centralized rapidity distribution of the third jet w.r.t. the tagging jets.
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Higgs+3 jets via VBF

F. Campanario et al.



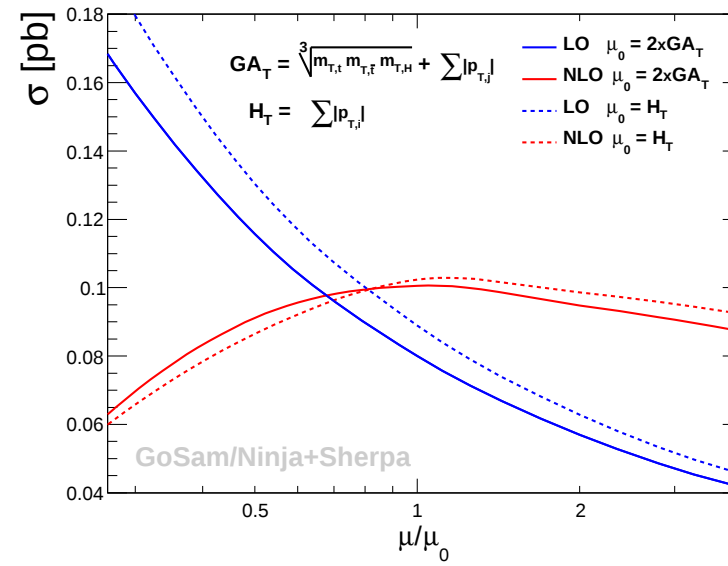
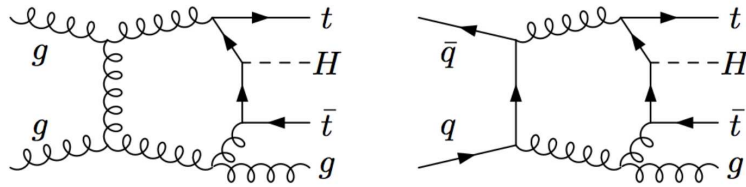
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$t\bar{t}H + \text{jet}$ at NLO

H. van Deurzen et al.

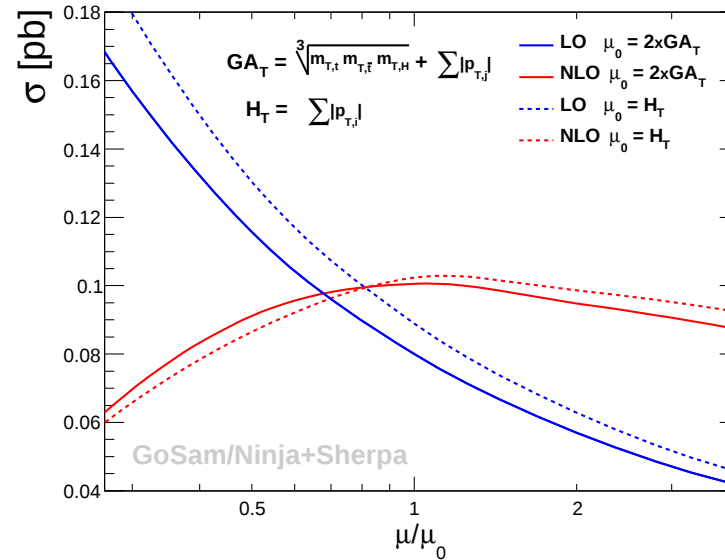
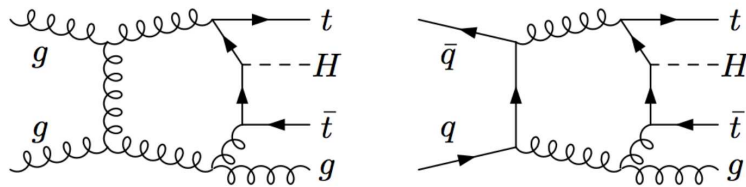
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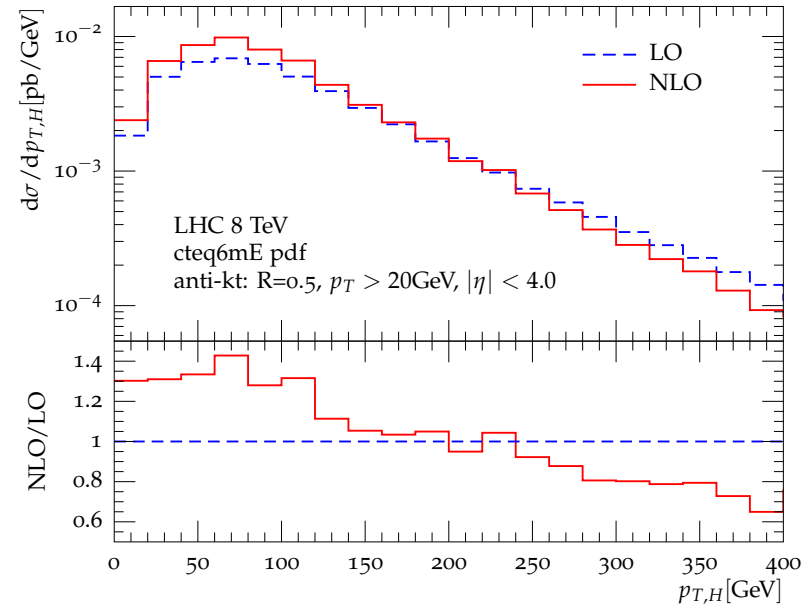
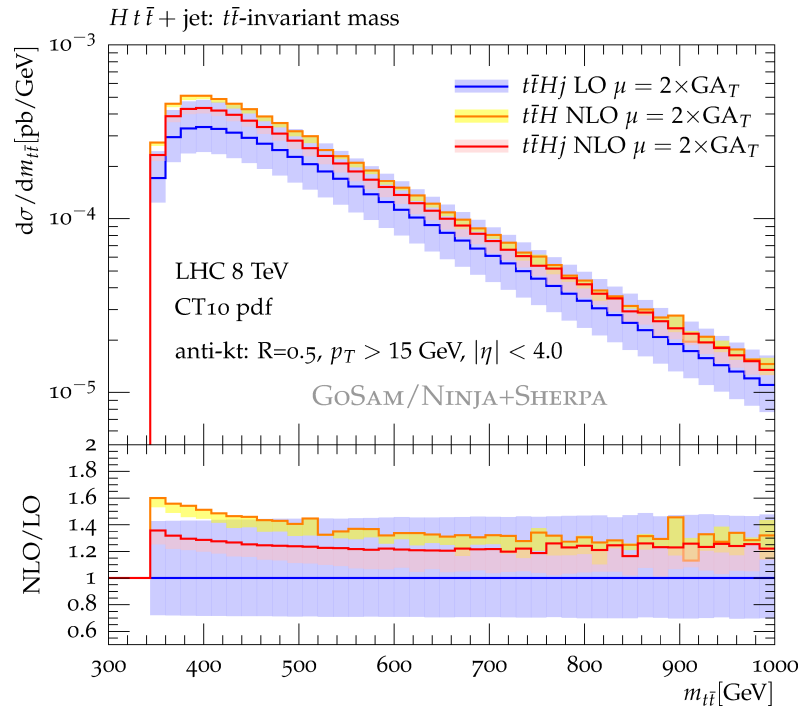
- The Born and the real emission matrix elements are computed using SHERPA and the library AMEGIC which implements the Catani-Seymour dipole formalism. SHERPA also performs the integration over the phase space and the analysis.
- The virtual corrections are generated with the GOSAM which combines automated diagram generation and algebraic manipulation with d -dimensional integrand-level reduction.
- The virtual amplitudes of $t\bar{t}Hj$ have been decomposed in terms of MIs using for the first time the *integrand reduction via Laurent expansion*, implemented in the $C++$ library NINJA.

$t\bar{t}H + \text{jet}$ at NLO

H. van Deurzen et al.

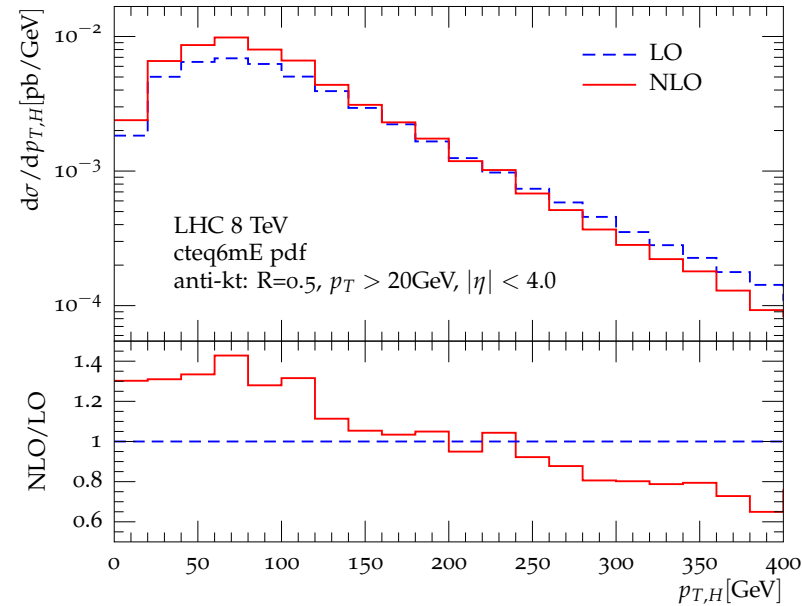
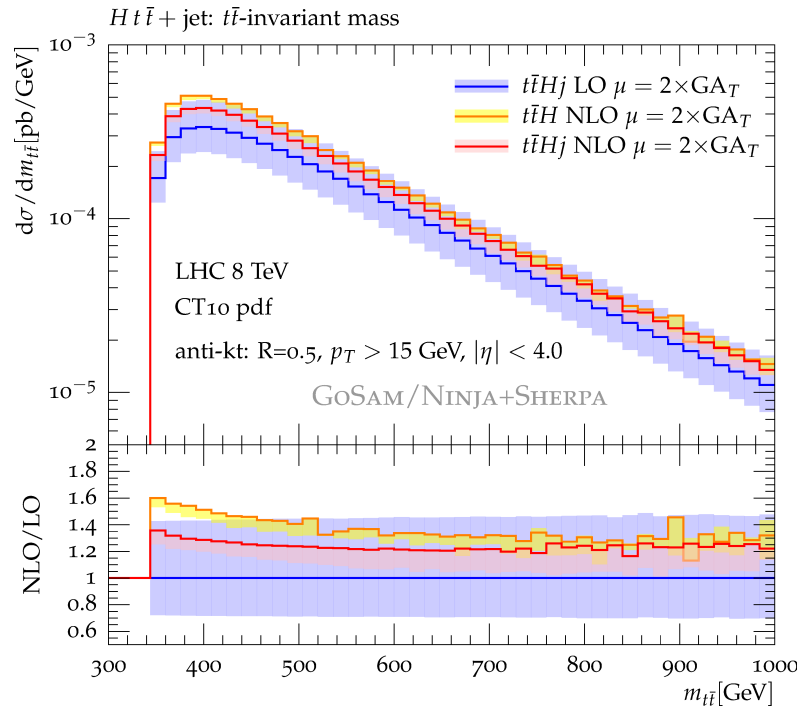
$t\bar{t}H + \text{jet}$ at NLO

H. van Deurzen et al.



$t\bar{t}H + \text{jet}$ at NLO

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- To cluster the jets the anti- k_t -algorithm is implemented in FASTJET with radius $R = 0.5$, a minimum transverse momentum of $p_{T,jet} > 15$ GeV and pseudorapidity $|\eta| < 4.0$.
- In order to study the scale dependence of the total cross section, two different choices of the renormalization and factorization scales $\mu_R = \mu_F = \mu_0$, namely $\mu_0 = H_T$ and $\mu_0 = 2 \times GA_T$ with

$$H_T = \sum_{\substack{\text{final} \\ \text{states } f}} |p_{T,f}|, \quad GA_T = \sqrt[3]{m_{T,H} m_{T,t} m_{T,\bar{t}}} + \sum_{\text{jets } j} |p_{T,j}|.$$

Higgs Characterisation at NLO

F. Maltoni, Prakash Mathews, VR et al.

Higgs Characterisation at NLO

F. Maltoni, Prakash Mathews, VR et al.

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- Higgs boson with various **spin-parity** assignment
- EFT has been implemented in FeynRules and passed to the **Madgraph5** and **aMC@NLO framework** by means of UFO model file.
 - improvable with new operators,
 - higher order QCD effects can be incorporated systematically.
 - multi-parton tree-level computation with parton shower,
 - next to leading order calculations matched with parton showers.

Higgs Characterisation for spin-0 Higgs

Buchmuller et al, Grzadkowski et al

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dimension-6 operators with pair of fermions

$$\mathcal{L}_0^f = - \sum_{f=t,b,\tau} \bar{\psi}_f (c_\alpha \kappa_{Hff} g_{Hff} + i s_\alpha \kappa_{Aff} g_{Aff} \gamma_5) \psi_f X_0 ,$$

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dimension-6 operators with pair of vector bosons

$$\begin{aligned} \mathcal{L}_0^V = & \left\{ c_\alpha \kappa_{\text{SM}} \left[\frac{1}{2} g_{HZZ} Z_\mu Z^\mu + g_{HWW} W_\mu^+ W^{-\mu} \right] \right. \\ & - \frac{1}{4} [c_\alpha \kappa_{H\gamma\gamma} g_{H\gamma\gamma} A_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{A\gamma\gamma} g_{A\gamma\gamma} A_{\mu\nu} \tilde{A}^{\mu\nu}] \\ & - \frac{1}{2} [c_\alpha \kappa_{HZ\gamma} g_{HZ\gamma} Z_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{AZ\gamma} g_{AZ\gamma} Z_{\mu\nu} \tilde{A}^{\mu\nu}] \\ & - \frac{1}{4} [c_\alpha \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + s_\alpha \kappa_{Agg} g_{Agg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}] \\ & - \frac{1}{4} \frac{1}{\Lambda} [c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} + s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu}] \\ & - \frac{1}{2} \frac{1}{\Lambda} [c_\alpha \kappa_{HWW} W_{\mu\nu}^+ W^{-\mu\nu} + s_\alpha \kappa_{AWW} W_{\mu\nu}^+ \tilde{W}^{-\mu\nu}] \\ & \left. - \frac{1}{\Lambda} c_\alpha [\kappa_{H\partial\gamma} Z_\nu \partial_\mu A^{\mu\nu} + \kappa_{H\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + (\kappa_{H\partial W} W_\nu^+ \partial_\mu W^{-\mu\nu} + h.c.)] \right\} X_0 , \end{aligned}$$

$$c_\alpha \equiv \cos \alpha , \quad s_\alpha \equiv \sin \alpha ,$$

Higgs Characterisation with spin-2 Higgs

J. Ellis et al

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Minimal coupling to spin-2 Higgs with fermions:

$$\mathcal{L}_2^f = -\frac{1}{\Lambda} \sum_{f=q,\ell} \kappa_f T_{\mu\nu}^f X_2^{\mu\nu} ,$$

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$$\mathcal{L}_2^V = -\frac{1}{\Lambda} \sum_{V=Z,W,\gamma,g} \kappa_V T_{\mu\nu}^V X_2^{\mu\nu} .$$

where $T^{\mu\nu}$ is the energy momentum tensor of SM fields.

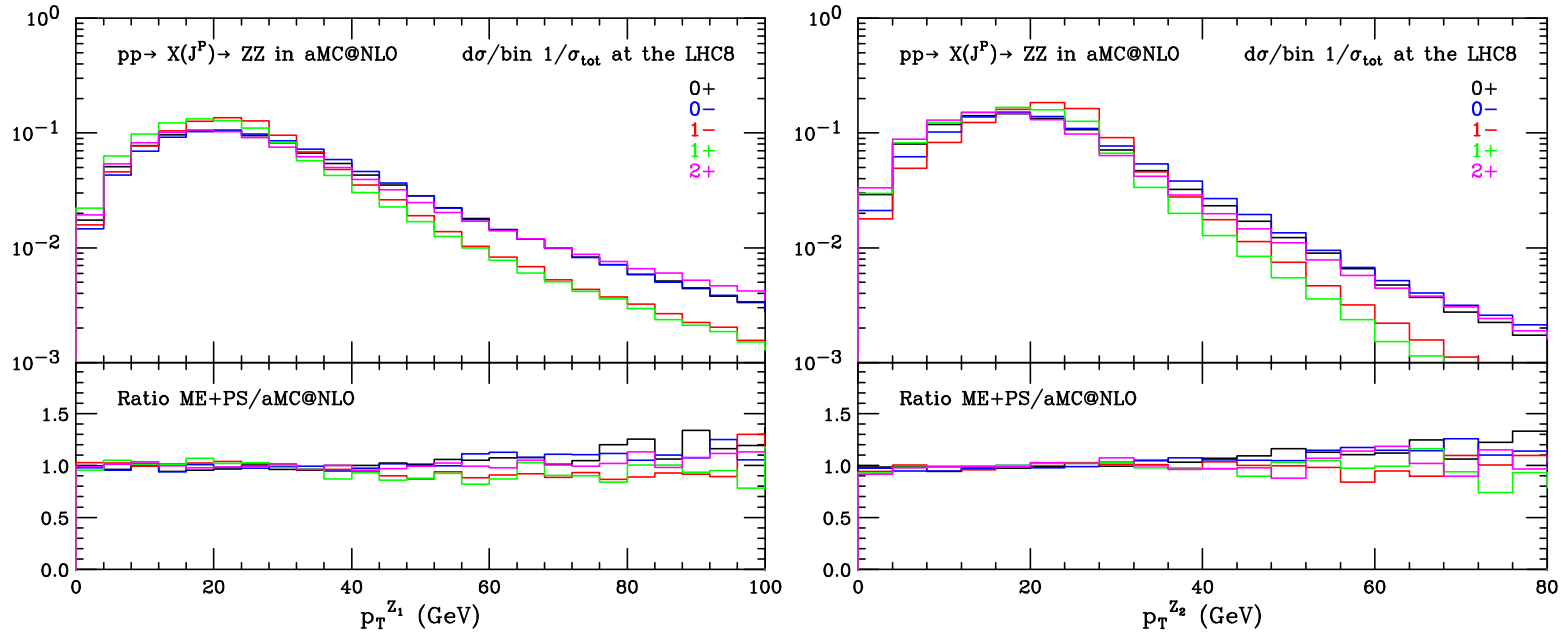
$$\begin{aligned} T_{\mu\nu}^f &= -g_{\mu\nu} \left[\bar{\psi}_f (i\gamma^\rho D_\rho - m_f) \psi_f - \frac{1}{2} \partial^\rho (\bar{\psi}_f i\gamma_\rho \psi_f) \right] \\ &\quad + \left[\frac{1}{2} \bar{\psi}_f i\gamma_\mu D_\nu \psi_f - \frac{1}{4} \partial_\mu (\bar{\psi}_f i\gamma_\nu \psi_f) + (\mu \leftrightarrow \nu) \right] , \\ T_{\mu\nu}^\gamma &= -g_{\mu\nu} \left[-\frac{1}{4} A^{\rho\sigma} A_{\rho\sigma} + \partial^\rho \partial^\sigma A_\sigma A_\rho + \frac{1}{2} (\partial^\rho A_\rho)^2 \right] \\ &\quad - A_\mu^\rho A_{\nu\rho} + \partial_\mu \partial^\rho A_\rho A_\nu + \partial_\nu \partial^\rho A_\rho A_\mu , \end{aligned}$$

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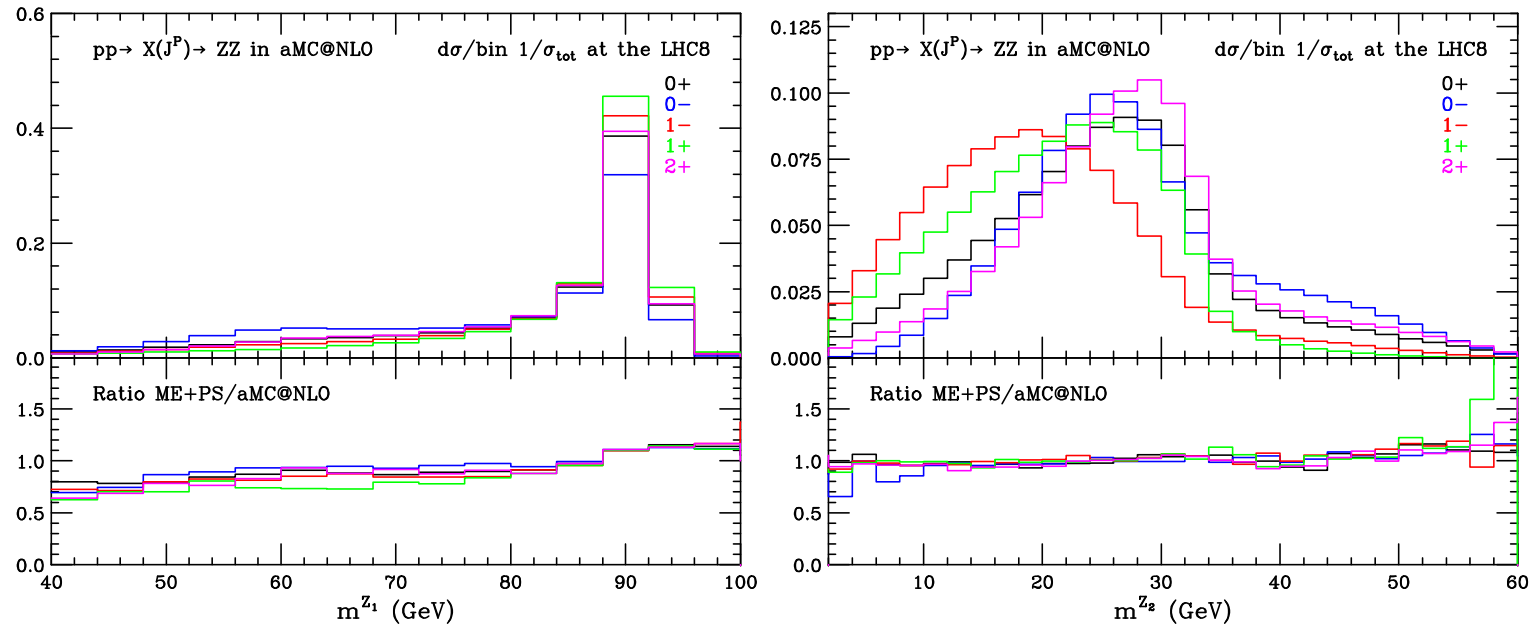
The transverse momentum of the Z boson with the highest and lowest reconstructed mass, $p_T^{Z_1}$ and $p_T^{Z_2}$, in $X(\rightarrow ZZ^*) \rightarrow \mu^+ \mu^- e^+ e^-$.

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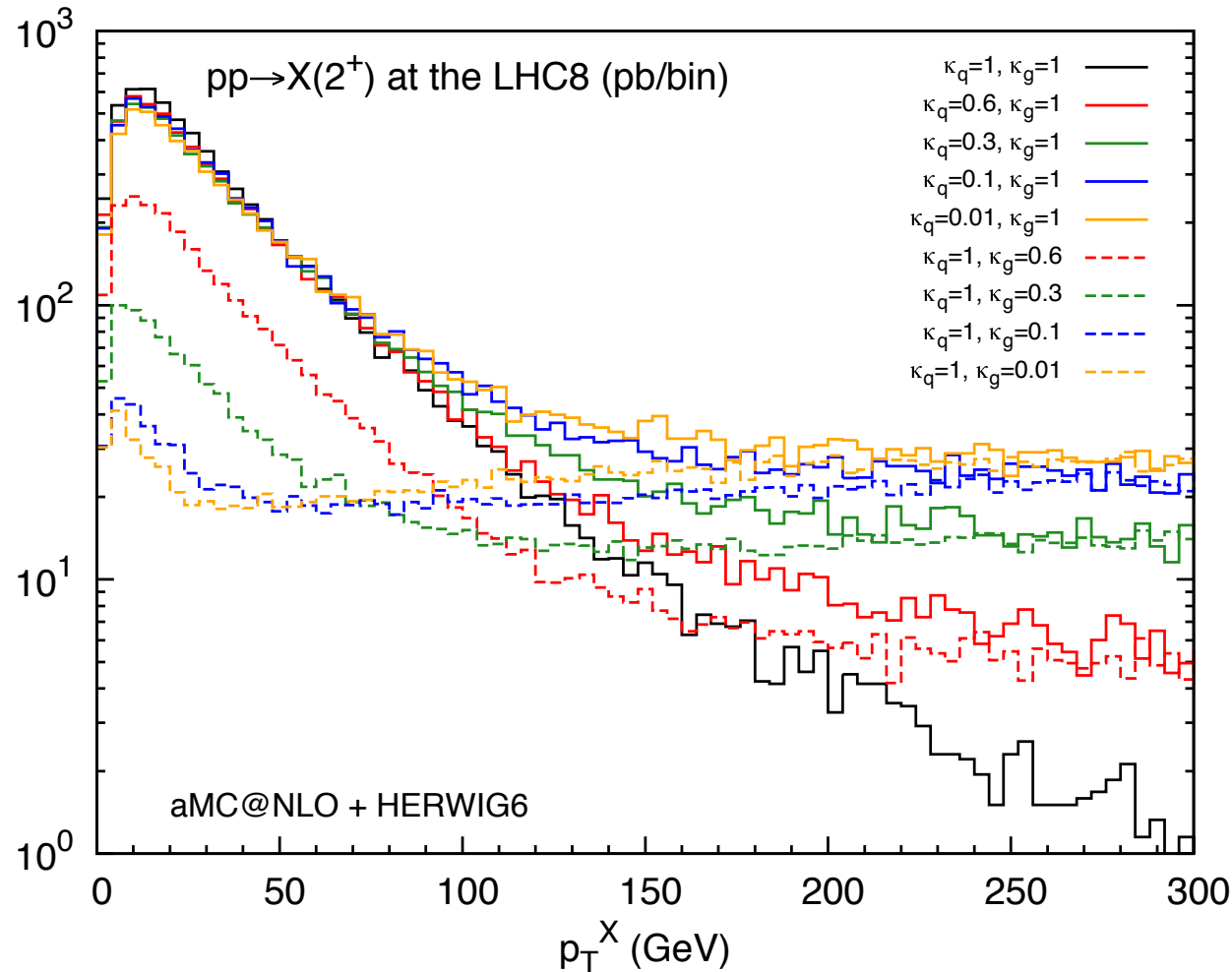
The invariant mass of the two leptons $m_{\ell\ell}$ from Z bosons

Higgs Characterisation: Non-universal couplings

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Higgs Characterisation: Non-universal couplings

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The transverse momentum p_T^X of a spin-2 state with non universal couplings to quarks and gluons $\kappa_q \neq \kappa_g$ as obtained from aMC@NLO. ● It violates unitarity.

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Characterisation with MADGRAF frame work is a new tool in the market to analyse Higgs boson's spin-parity and its coupling to SM particles in a model independent way.