

# GRBs AND FRBs: SUPRAMASSIVE MAGNETAR AS A COMMON PROGENITOR?

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Workshop on  
Gamma Ray Bursts - from  
Prompt emission to Afterglows, July 4-7, 2017  
NCRA (TIFR), Pune

## GAMMA-RAY BURST SOURCES:

- Long GRBs are associated with supernovae of type Ib/c  $\Rightarrow$  Progenitors are likely to be massive Wolf-Rayet (WR) stars (i.e. stars that have lost their H envelope)  $\Rightarrow$  Relatively small helium stars with size  $\sim$  few  $\times 10^{10}$  cm
- Long GRB rates are only  $\sim 4 \times 10^{-3} - 10^{-2}$  times rates of SN Ib/c (Frail et al. 2001)
- Rate per volume of long GRBs has been estimated to be  $\sim 10^2 - 10^3$  Gpc $^{-3}$ yr $^{-1}$
- Prompt  $\gamma$  emission is along bi-polar narrow jets with  $\Delta\Omega \sim 0.01$  str (or, equivalently,  $\theta_j \sim 0.1$  radian)

High Lorentz factor of the jet,  $\Gamma_j \sim 100 \Rightarrow$  relativistic beaming,  $\Delta\theta \sim 0.01 \Rightarrow$  In the prompt emission phase, we see only a tiny fraction of the jet

- Short GRBs ( $T_{90} < 2$  s) form only 30% of the total population (in this context, see Rezzolla and Kumar, 2015, for extended X-Ray emissions and magnetars)

## FAST RADIO BURSTS:

- Flux density  $\sim 0.1 - 10$  Jy at  $\sim 1$  GHz, lasting for  $\sim$  few ms

FRBs have been seen at  $\sim 800$  MHz -  $\sim 2$  GHz

- High dispersion measure (DM)  $\sim 500 - 1200$  pc cm<sup>-3</sup>

- Many of them seen at high Galactic latitudes; **FRB 131104** ( $E_{rad} \sim 4 \times 10^{41}$  erg) has been identified with a GRB ( $E_{\gamma} \sim 4 \times 10^{50}$  erg; DeLauney et al. 2016; Murase et al. 2017)
- If the measured DM is attributed to IGM then FRBs have  $z \sim 0.45 - 1 \Rightarrow$  Radio luminosity  $\sim 10^{41} - 10^{43}$  erg s<sup>-1</sup> and radio energy  $\sim 10^{38} - 10^{42}$  erg
- Only one FRB so far exhibits repeated bursts
  - **FRB 121102.**
- **FRB 121102** is localized within a dwarf galaxy at  $z \cong 0.193$  that contains a persistent compact radio-source (Chatterjee et al. 2017; Tendulkar et al. 2017)

- The persistent radio-source ( $S_\nu \sim 200 \mu\text{Jy}$ ) and FRB 121102 (flux densities at 1.7 GHz on different occasions range from  $\sim 0.1 \text{ Jy}$  to  $\sim 4 \text{ Jy}$ ) are separated by a projected distance less than  $\sim 40 \text{ pc}$  (Marcote et al. 2017)
- Exploiting  $t_{FF} \sim 1/\sqrt{G\rho_{nuc}} \sim 10^{-3} \text{ s}$ , Falcke and Rezzolla (2014) have proposed a natural model for FRBs invoking collapse of initially rapidly rotating supra-neutron stars that get spun down due to magnetic braking:
  - \* The supra-NS collapses into a black hole leaving its high magnetic field ‘hair’ and the associated magnetosphere outside the event horizon
  - \* Curvature radio-emission due to bunched electrons (positrons) flowing out along the magnetic field lines:

$$L_{curv} = \frac{2\gamma^4 N_{bunch}^2 e^2 c}{3R^2}$$

$$\approx 10^{42} \left( \frac{N_{bunch}}{1.5 \times 10^{27}} \right)^2 \left( \frac{\gamma}{10^2} \right)^4 \left( \frac{R}{10 \text{ km}} \right)^{-2} \text{ erg s}^{-1}$$

\* Characteristic frequency:

$$\nu_{curv} = \frac{3\gamma^3 c}{4\pi R} \approx 7.2 \left( \frac{\gamma}{10^2} \right)^3 \left( \frac{R}{10 \text{ km}} \right)^{-1} \text{ GHz}$$

- Estimated FRB rate  $\sim 0.25 \text{ deg}^{-2} \text{ day}^{-1}$  (Thorn-ton et al. 2013)

All sky rate  $\sim 2100 \text{ day}^{-1}$  for FRBs brighter than  $\sim 2 \text{ Jy}$  (Champion et al. 2016)

⇒ FRB rate per volume  $\sim 10^4 - 10^5 \text{ Gpc}^{-3} \text{ yr}^{-1}$

While long GRB rate per volume  $\sim 10^2 - 10^3 \text{ Gpc}^{-3} \text{ yr}^{-1}$

- Zhang (2013), invoking Falcke-Rezzolla model, has proposed that some FRBs are physically

## associated with GRBs

- In this work, we explore a scenario in which all FRBs and majority of long GRBs are associated with collapse of the central iron core of initial size  $\sim 10^8$  cm of massive, rotating Wolf-Rayet stars that leads to a supra-massive neutron star with large kick velocity, high B and rapid rotation, which eventually collapses to form a black hole after  $10^3 - 10^4$  s
- Motivation:
  - \* Anomalous X-Ray pulsars (AXPs) as well as Soft Gamma Repeaters (SGRs) are widely believed to be part of unified class (Kaspi, 2003; Woods and Thompson, 2006; Turolla, Zane and Watts, 2015)  $\Rightarrow$  Magnetars (Duncan and Thompson, 1992)

- \* X-Ray plateau followed by steep decay is naturally explained by magnetic braking of a rapidly spinning magnetar (Metzger et al., 2011; Granot et al. 2015)
- \* Can magnetars be the basis for all long GRBs? (For critical analyses, see Granot et al., 2015, Kumar and Zhang, 2015)
- \* SN Ib/c rates and FRB rates are comparable

• Basic Picture:

- \* Progenitor of long GRBs and FRBs are massive, rotating WR stars
- \* A rapidly rotating, unstable Fe core of mass

$2 - 3 M_{\odot}$  collapses on a time scale of  $\sim 1$  s to form a fast spinning supra-massive proto-neutron star (SPNS) with kick velocity ranging from 0 to  $\sim 1000$  km/s

- \* Because of the rotation and core collapse a spherical region of size  $\sim 10^8$  cm along with two narrow funnel shaped regions around the spin axis straddling the spherical region are essentially cleared out of baryonic stellar matter of the WR star
- \* If the kick velocity direction of the SPNS lies within the funnel shaped openings, there is no baryon loading problem  $\Rightarrow$  gamma ray jet can break out of the He envelope giving rise to a long GRB

If the opening angle  $\theta_F$  of the funnel shaped

region of the WR star is also  $\sim 0.1$  corresponding to  $\Delta\Omega_F \sim 0.01$  then the probability that the prompt gamma rays are not quenched is,

$$\approx 2 \frac{\Delta\Omega_F}{4\pi} \approx 5 \times 10^{-3}$$

- \* If the SPNS moves in any other direction it will encounter the stellar material, and due to baryon loading the  $\gamma$ -rays resulting from electron-positron pairs generated by the neutrino wind would get degraded to softer photons, and there will be no prompt gamma-emission
- \* The SPNS cools and contracts to form the supra-massive neutron star (NS) in  $\sim 5 - 10$  s
- \* If  $v_{kick} \sim 100$  km/s then the supra-massive NS crosses the spherical evacuated region of size  $\sim 1000$  km in  $\sim 10$  s, before the SPNS becomes

transparent to the neutrinos

\* Magnetars with high kick velocities have been observed

Example: For the magnetar Swift J 1834.9-0846, the kick velocity component perpendicular to the line of sight is  $\sim 580$  km/s if it is at a distance 15 kpc (Granot et al. 2006; Granot et al., 2016)

\* The supra-massive magnetar collapses due to the spin down after about  $10^3 - 10^4$  s and forms a black hole giving rise to a transient radio-burst

- Magnetar spin down:

Dipole Radiation implies (Granot et al. 2015),

$$P_{em}(t) = \frac{E}{t_{sd}(1 + t/t_{sd})^2}$$

where,

$$E = \frac{1}{2} I \omega_0^2, \quad t_{sd} = \frac{3c^3 I}{(B_p \omega R^3 \sin \chi)^2}$$

If  $M = 2.5 M_\odot$ ,

$$E = 10^{53} (P/1 \text{ ms})^{-2} (M/2.5 M_\odot)^{3/2} \text{ erg}$$

where one has used (Lattimer and Schutz, 2005),

$$R = 15(M/2.5 M_\odot)^{1/4} \text{ km} \quad I = 2 \times 10^{45} (M/2.5 M_\odot)^{3/2}$$

and

$$t_{sd} = \frac{3.6 \times 10^2}{\sin^2 \chi} (B_p/10^{15} \text{ G})^{-2} (P/1 \text{ ms})^2 \text{ s}$$

- But Falcke-Rezzolla model, as it stands, cannot explain repeating FRBs. Can we salvage the model for repeating FRBs?
- We explore two scenarios to salvage the above model for sources like FRB 121102

## Scenario I:

Sporadic accretion onto a fast spinning Kerr BH resulting from the collapse of a supra-massive magnetar

- Blandford-Znajek mechanism:
  - Potential difference developed due to a rotating horizon of a Kerr BH embedded in an external magnetic field  $B$ ,

$$V_{el} \sim \frac{1}{c} (\Omega_H/2\pi) (B \cdot \pi R_{BH}^2)$$

where  $\Omega_H$  is the angular speed of the horizon,

$$\Omega_H = \frac{J}{MR_s R_{BH}}$$

$$R_s = \frac{2GM}{c^2}$$

$$R_{BH} = \frac{R_s}{2} + \sqrt{\left(\frac{R_s}{2}\right)^2 - \left(\frac{J}{Mc}\right)^2}$$

- Mining of the rotational energy of the BH

via B-Z process leads to radiated power,

$$L_{B-Z} \approx \text{current} \times V_{el} \sim \sim \frac{V_{el}^2}{\mathcal{R}} \sim \frac{c}{4} \frac{V_{el}^2}{\mathcal{R}}$$

- For extremal BHs,

$$\begin{aligned} J = cMR_s/2 \Rightarrow R_{BH} = R_s/2 \Rightarrow \Omega_H = \frac{c}{R_s} \Rightarrow V_{el} \sim R_s B/8 \\ \Rightarrow L_{B-Z} \approx \frac{cB^2 R_s^2}{256} \\ = 5.58 \times 10^{42} (B/3.2 \times 10^{11} \text{ G})^2 (M/2.3 M_\odot)^2 \text{ erg s}^{-1} \end{aligned}$$

- Sporadic relativistic electron wind towards FRB 121102 by the persistent radio-source  $< 40$  pc far can cause radio-bursts arising out of B-Z mechanism

Caveats:

- \* Requires large  $B \sim 10^{11}$  G to be still present near the event horizon of the Kerr BH. Question is whether when a magnetar with polar B field  $\sim 10^{14} - 10^{15}$  G collapses to form a BH,

a vestigial plasma with field  $\sim 10^{11}$  is retained near the event horizon (In the context of GRB modeling, Contopoulos et al 2017 claim that  $B \sim 10^4$  G can hover near the horizon)

\* Accretion of plasma cannot generate such high B field since the Eddington limit for B is,

$$B_{Edd} = \sqrt{\frac{8\pi c^4 m_p}{\sigma_T G M}} \cong 2 \times 10^8 (M/2.3 M_\odot)^{-1/2} G$$

### Scenario II:

The core of the Magnetar that collapses has angular momentum too large to form a Black hole

- $R_{BH} = \frac{R_s}{2} + \sqrt{(\frac{R_s}{2})^2 - (\frac{J}{Mc})^2}$
- Initial angular momentum of the supra-massive magnetar,

$$J_0 \sim M_0 R_0^2 \Omega_0$$

with,

$$\Omega_0 < \Omega_{Break-up} = \sqrt{\frac{GM_0}{R_0^3}}$$

As it spins down due to magnetic dipole radiation, it starts collapsing on time scales  $1/\sqrt{G\rho_{nuc}}$  satisfying,

$$M_0 R^2(t) \Omega(t) \sim \beta J_0$$

where  $\beta < 1$ .

- The equatorial region forms a disc-like structure while the core of mass  $M_c$  and angular momentum  $J_c$  collapses

$$M_c = M_0 - M_{disc}$$

$$J_c = \beta J_0 - J_{disc}$$

- Assuming the disc to be thin so that angular momentum per unit mass is  $\sqrt{GM_c r}$ , one gets:

$$J_c \approx \beta J_0 \left[ 1 - \frac{8}{5} \left( 1 - M_c/M_0 \right) (M_c/M_0)^{1/2} \right]$$

- **No black hole formation if**

$$J_c > \frac{GM_c^2}{c} \Rightarrow J_0 > \frac{GM_c^2}{c\beta[1 - \frac{8}{5}(1 - M_c/M_0)(M_c/M_0)^{1/2}]}$$

- **For  $\beta \sim 0.8$ ,  $M_0 = 2.3 M_\odot$  and  $M_c \sim 1.4 M_\odot$ :**

$$\Omega_0 > 9 \times 10^3 \text{ rad s}^{-1}$$

**for no black hole formation, while for  $M_0 = 2.3 M_\odot$ ,**

$$\Omega_{Break-up} = 1.75 \times 10^4 \text{ rad s}^{-1}$$

- **What happens to the collapsed core? It becomes a strange star when the density becomes greater than  $5 \times 10^{14} gm cm^{-3}$  (Witten 1984; Alcock et al. 1986)**
- **Signatures: Emission of thermal photons and neutrinos in a burst**
- **The strange star will have an outward electric field  $\approx 5 \times 10^{17} - 10^{18} \text{ V/cm}$  that manages to**

hold on to a layer of electrons few fm thick  
(Alcock et al. 1986)

- Mannarelli et al. 2014 have shown that torsional oscillation of the thin electron cloud relative to the positively charged strange star can cause emission of GHz radiowaves with luminosity  $\sim 10^{45}$  erg/s.
- Torsional oscillations can be excited by relativistic wind from the persistent radio-source near FRB 121102

## CONCLUSION

- Collapse of spun down supra-NS is a natural framework to describe both GRBs and FRBs if pre-natal kicks are included
- Repeating bursts from FRB 121102 may also be explained either by (a) invoking intermittent Blandford-Znajek processes around the collapsed black hole or by (a) torsional oscillations of electrons close to the surface of a bare strange star

**THANK YOU**