

GRB afterglows with hard spectrum

Dipankar Bhattacharya

GRB afterglow evolution

Dynamics: $E, n \Rightarrow \Gamma(t), R(t)$

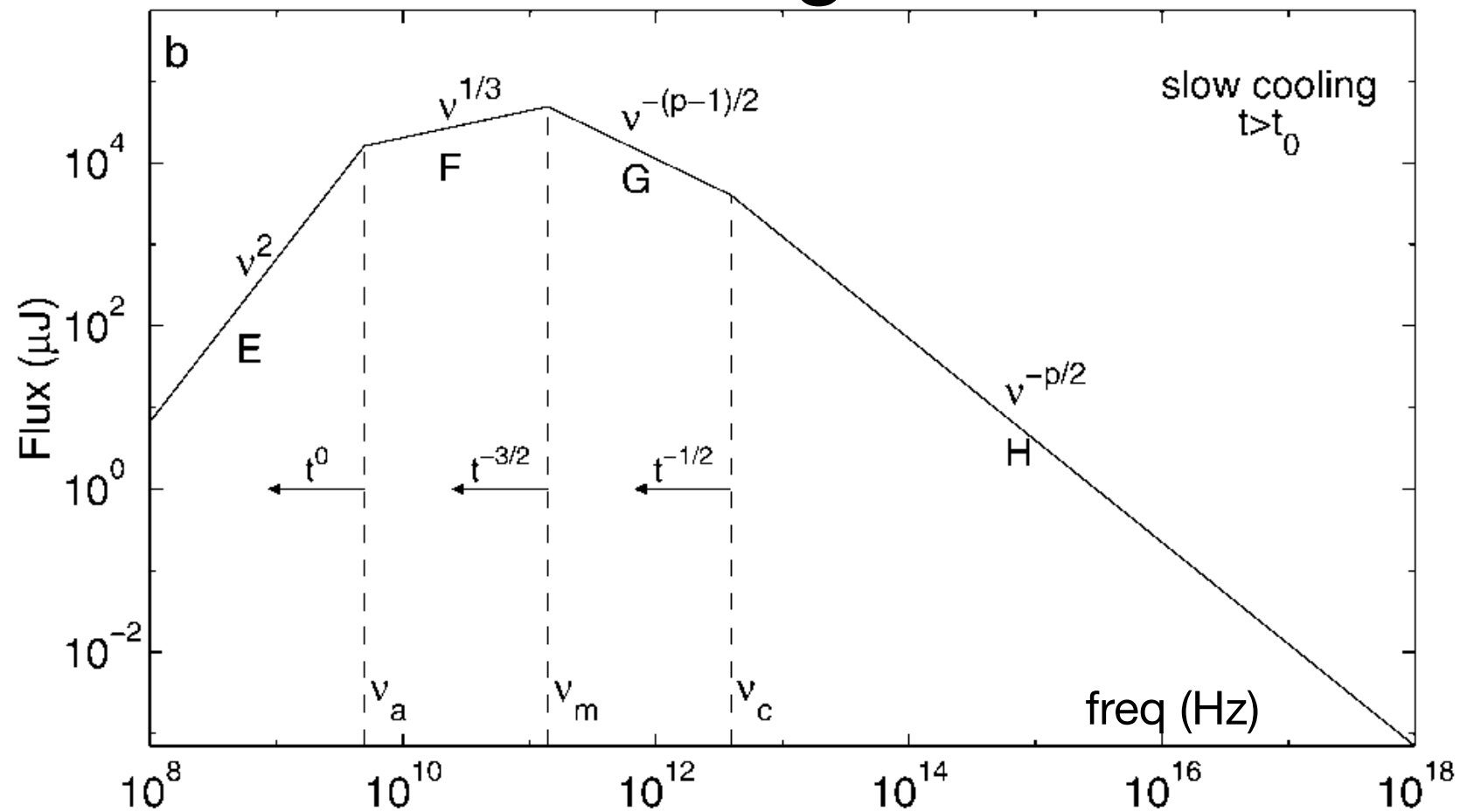
Magnetic field $B(t)$: **assume** $B^2/8\pi = \epsilon_B u_{\text{th}} = \epsilon_B 4\Gamma^2 n m_p c^2$

Electrons: $N_e(\gamma_e) d\gamma_e = K \gamma_e^{-p} d\gamma_e$

$$\int_{\gamma_m}^{\gamma_u} N_e(\gamma_e) d\gamma_e = 4\Gamma n$$

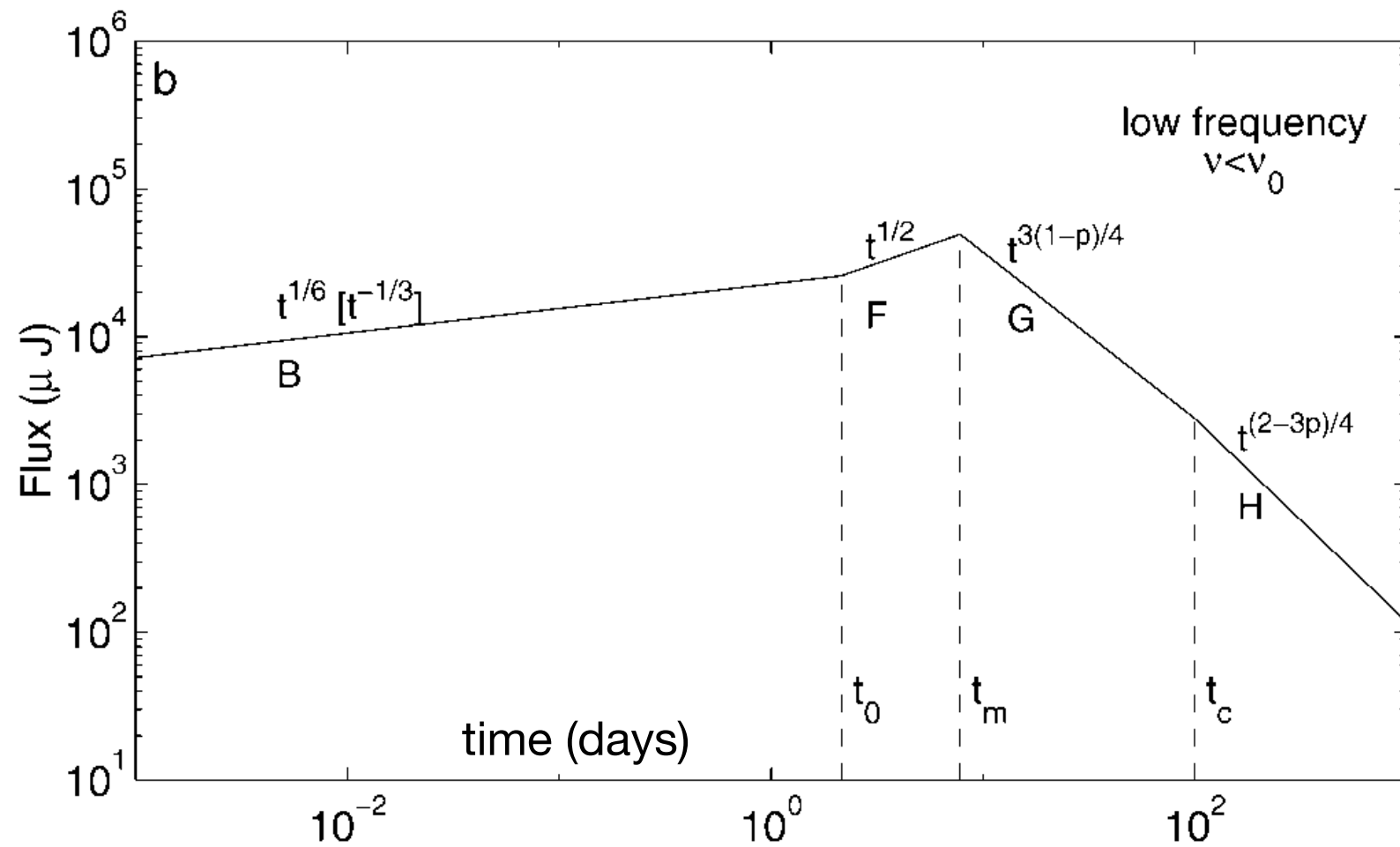
$$\int_{\gamma_m}^{\gamma_u} \gamma_e m_e c^2 N_e(\gamma_e) d\gamma_e = \epsilon_e 4\Gamma^2 n m_p c^2$$

Standard afterglow evolution



$$p > 2$$

$$\gamma_u \rightarrow \infty$$



Sari et al 1998

If $p < 2$ then γ_u cannot be ignored

$$p > 2$$

$$\gamma_m = \epsilon_e \left(\frac{p-2}{p-1} \right) \frac{m_p}{m_e} \Gamma$$

Panaiteescu 2000:

Hard spectrum in GRB000301c

Keep $\gamma_m \propto \Gamma$

Allow ϵ_e to determine γ_* , the upper cutoff

[equivalent to $q = 1$]

$$1 < p < 2$$

$$\gamma_m = \left[\epsilon_e \left(\frac{2-p}{p-1} \right) \frac{m_p}{m_e} \Gamma \gamma_u^{p-2} \right]^{1/(p-1)}$$

$$\gamma_u \propto \Gamma^q$$

DB 2001

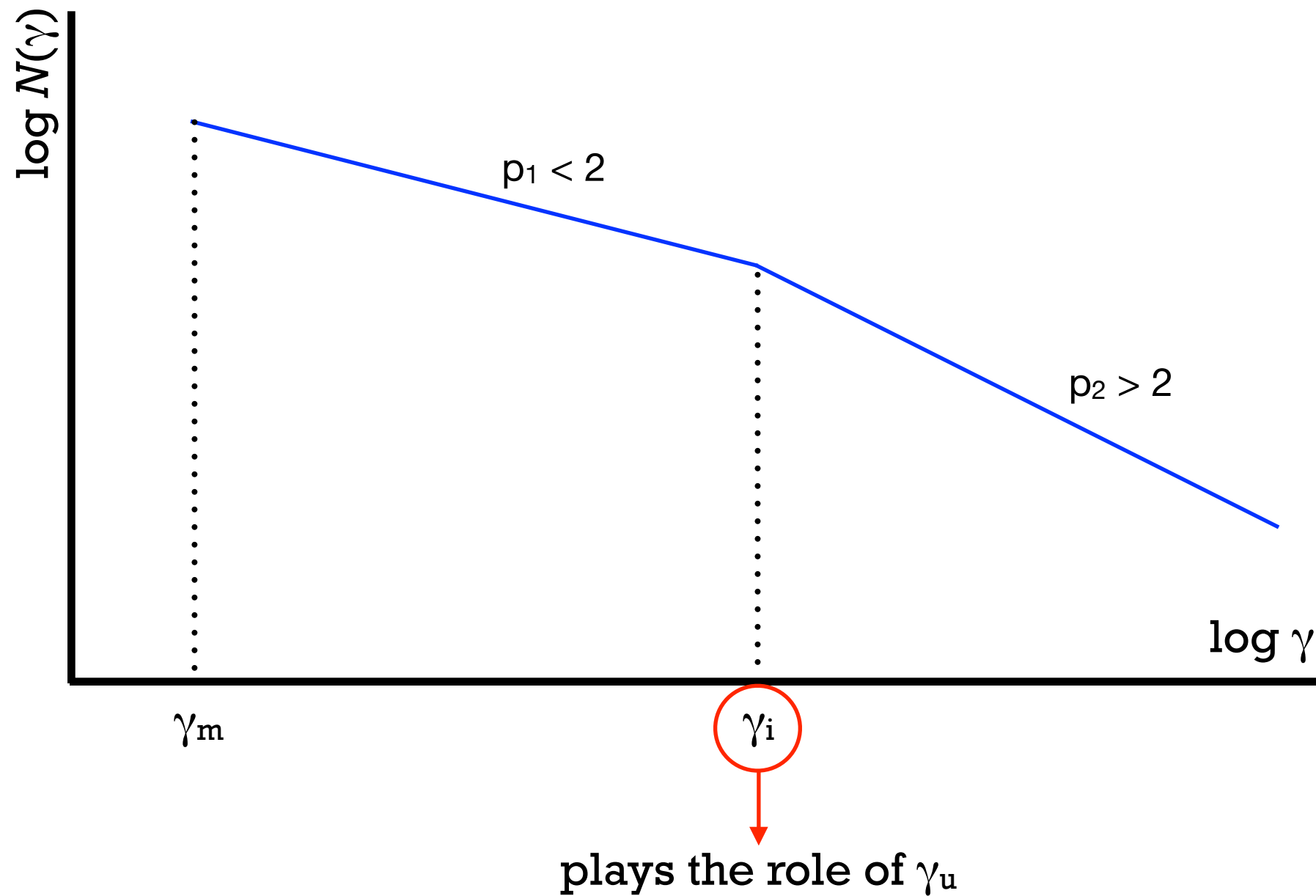
$$\gamma_u = \gamma_c \propto \Gamma^{-1/2}$$

Dai & Cheng 2001

Application to GRB 010222

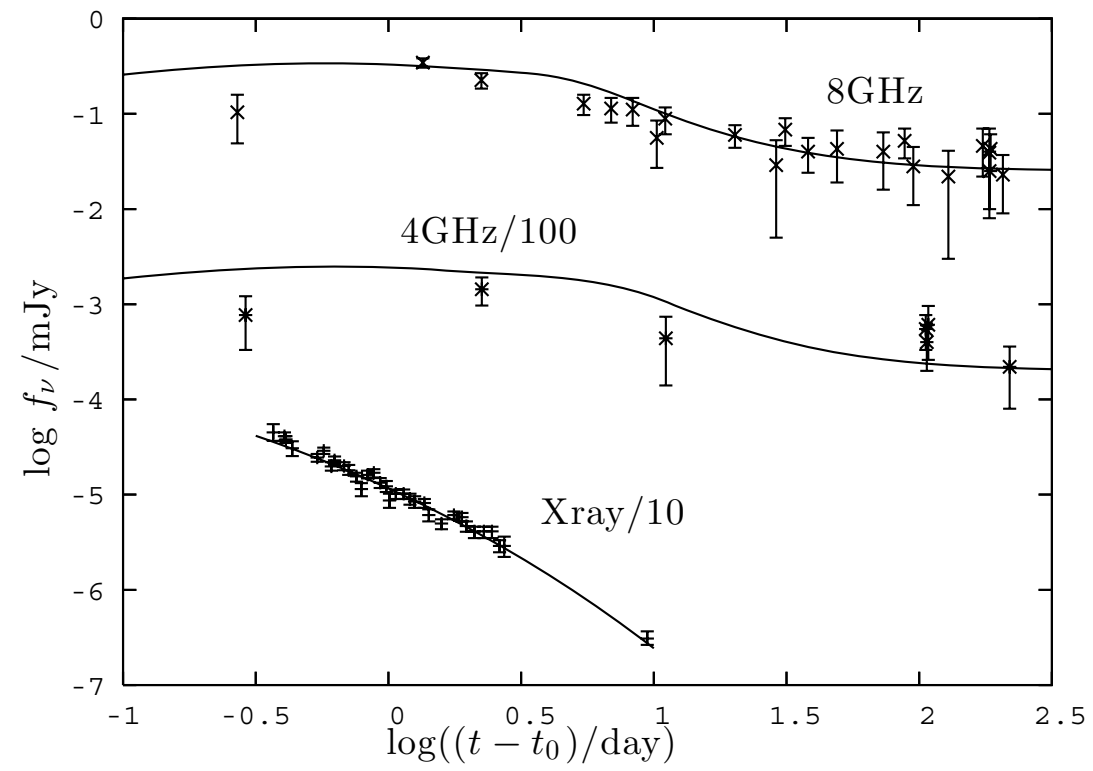
Sagar et al 2001, Cowsik et al 2001, Dai & Cheng 2001
Stanek et al 2001, Jha et al 2001

Injection Break

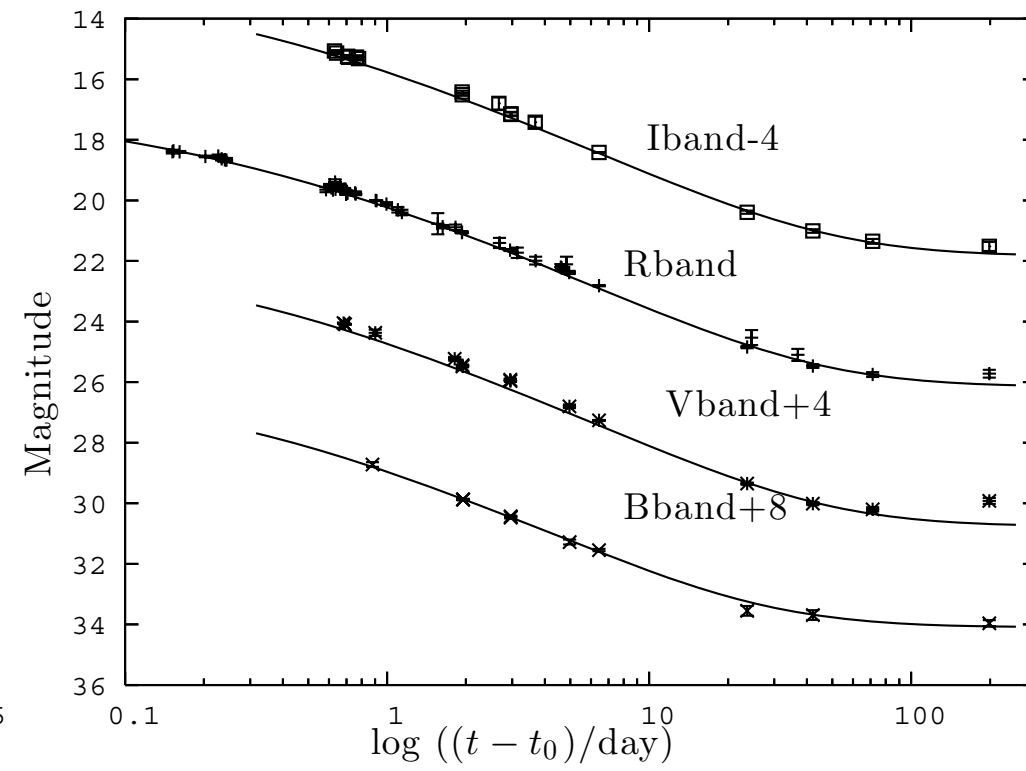


Panaiteescu 2000
Panaiteescu & Kumar 2001
Resmi & DB 2008

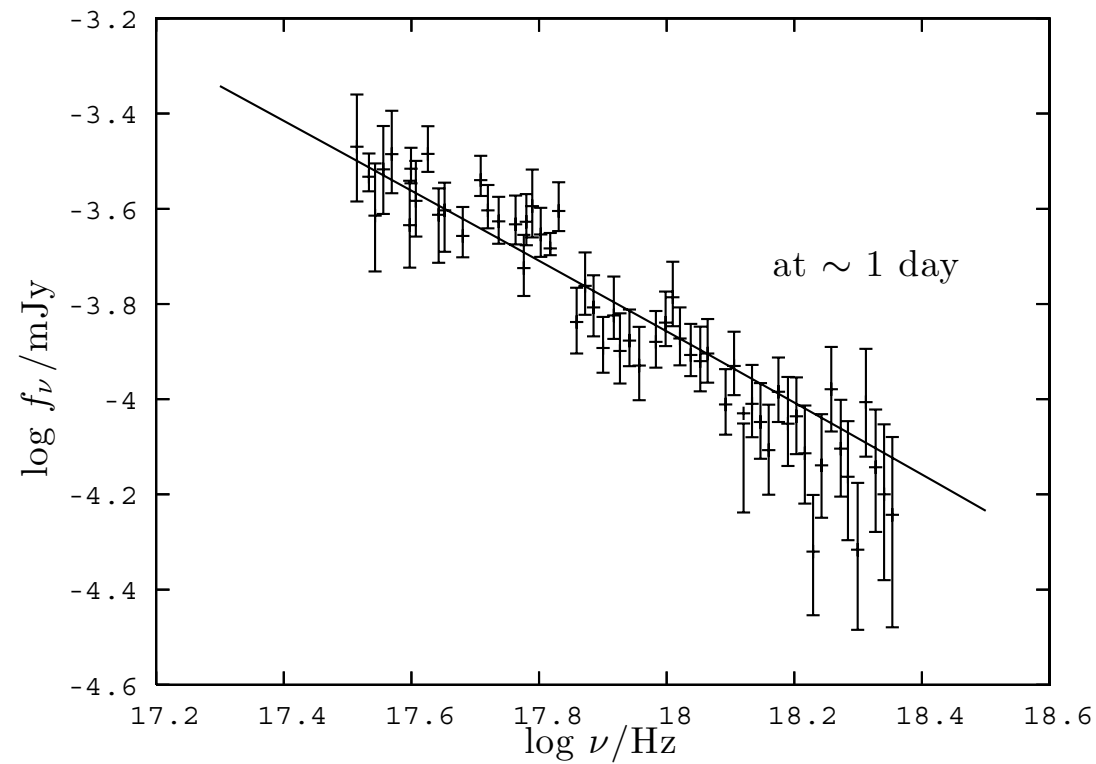
GRB 010222



(a)

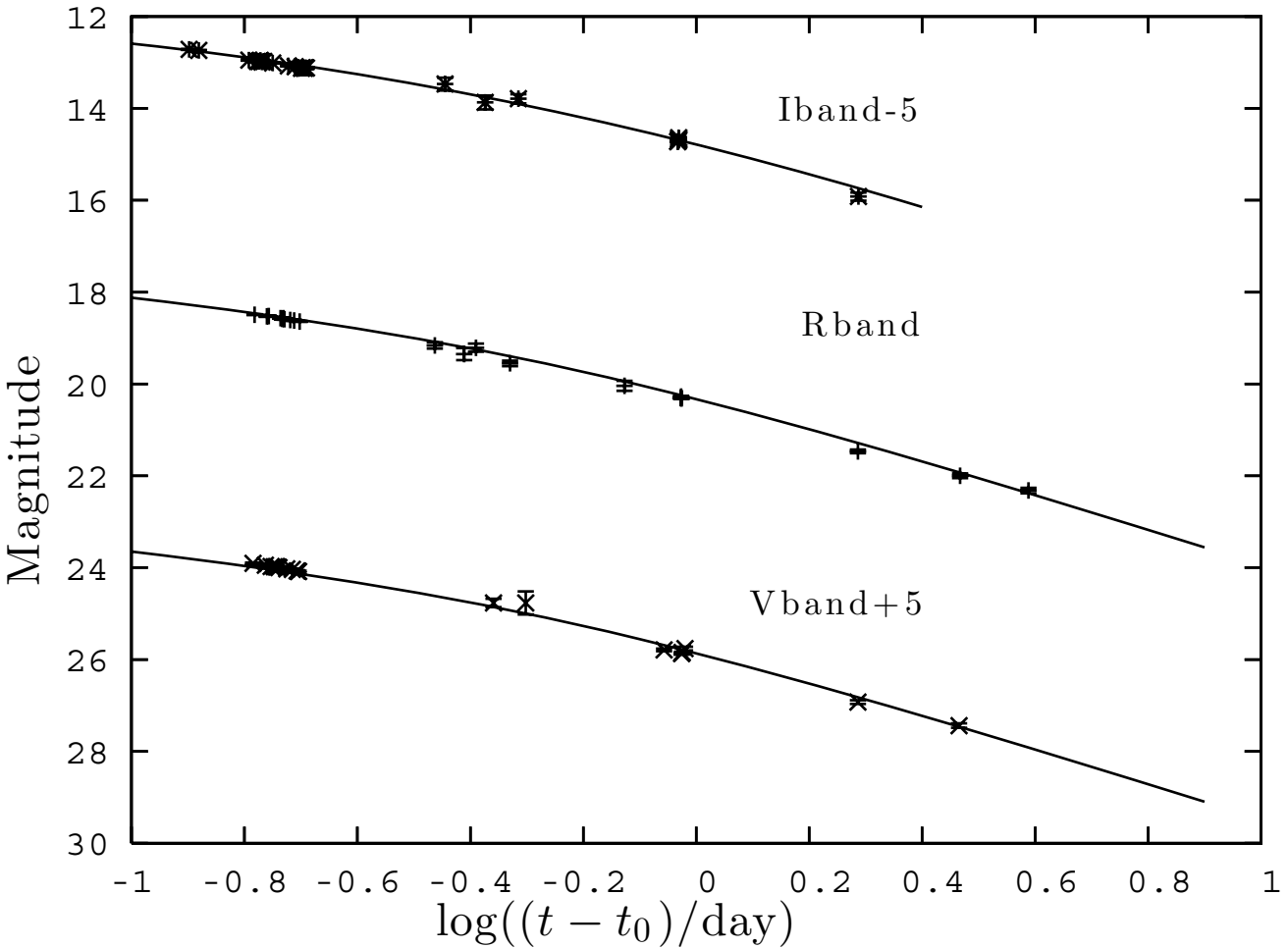
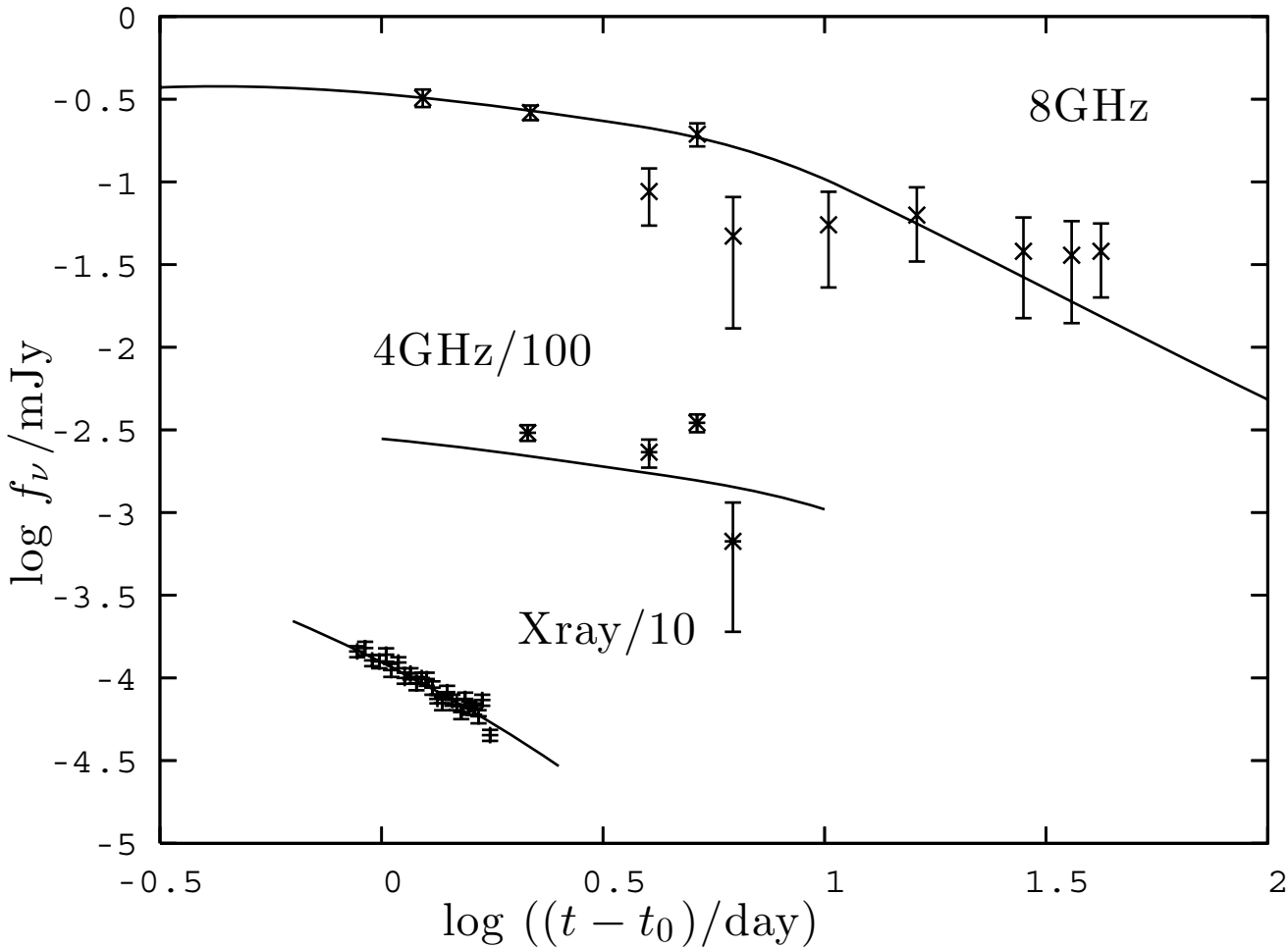


(b)



(c)

GRB 041006



Misra et al 2004
Resmi & DB 2008

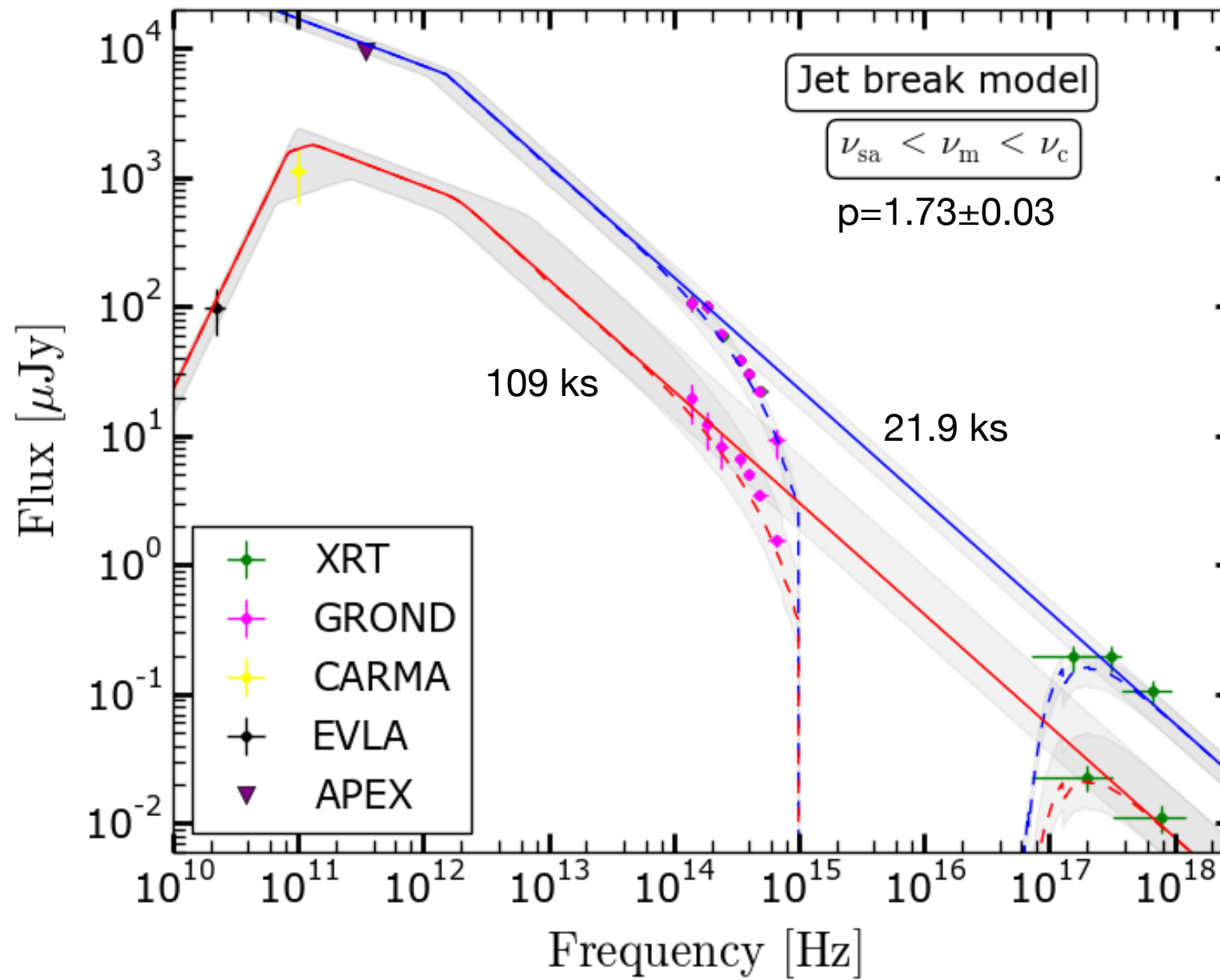
Fit parameters	GRB010222	GRB020813	GRB041006
p_1	$1.47^{+0.004}_{-0.003}$	$1.40^{+0.007}_{-0.004}$	1.29–1.32
p_2	$2.04^{-0.01}_{+1.76}$	~ 2.1	> 2.2
q	1.3 ± 0.06	1.3 ± 0.05	0.95–1.14

GRB	Density (cm ⁻³)	p	ϵ_e	ϵ_B
970228		2.44 ⁸		
970508	0.75 ²	2.29 ^{2, 3, 8}	0.19 ^{1, 2, 3}	0.1685 ^{1, 2, 3, 6}
971214		2.2 ⁸		
980329		2.69 ^{3, 8}	0.12 ³	0.17 ³
980519	0.14 ²	2.87 ^{2, 8}	0.11 ²	0.000 035 ²
980703		2.64 ^{3, 8}	0.27 ³	0.0018 ³
990123	0.0019 ⁴	2.135 ^{2, 8}	0.13 ²	0.000 74 ²
990510	0.29 ⁴	1.945 ^{2, 8}	0.025 ²	0.0052 ²
991208	18 ²	1.53 ²	0.056 ²	0.035 ²
991216	4.7 ²	1.36 ²	0.014 ²	0.018 ²
000301C	27 ⁴	1.43 ²	0.062 ²	0.072 ²
000418	27 ²	2.04 ²	0.076 ²	0.0066 ²
000926	22 ⁴	2.58 ^{2, 3, 8}	0.125 ^{2, 3}	0.0435 ^{2, 3}
010222	1.7 ²	1.695 ^{2, 8}	0.43 ²	0.000 067 ²
011121		2.5 ⁵		0.5 ⁵
011211	3 ⁵	2.4 ⁵	0.0025 ⁵	0.01 ⁵
050801		2.64 ⁹		
050802		2.62 ⁹		
050904			0.0309 ⁷	
051109A		2.08 ⁹		
060124		2.02 ⁹		
060729		2.22 ⁹		
061121		1.88 ⁹		
090323			0.07 ¹⁰	0.0089 ¹⁰
090328		2.26 ¹⁰	0.11 ¹⁰	0.0019 ¹⁰
090902B	0.000 56 ¹⁰	2.21 ¹⁰	0.13 ¹⁰	0.33 ¹⁰
090926A		2.13 ¹⁰	0.33 ¹⁰	0.081 ¹⁰

Compilation of observationally derived microphysical parameters of GRBs

- 1: [Wijers & Galama \(1999\)](#)
- 2: [Panaitescu & Kumar \(2002\)](#)
- 3: [Yost et al. \(2003\)](#)
- 4: [Chevalier & Li \(2004\)](#)
- 5: [Piro et al. \(2005\)](#)
- 6: [van der Horst, Wijers & Rol \(2005\)](#)
- 7: [Gou, Fox & Mészáros \(2007\)](#)
- 8: [Starling et al. \(2008\)](#)
- 9: [Curran et al. \(2009\)](#)
- 10: [Cenko et al. \(2011\)](#)

GRB121024A



Varela et al 2016

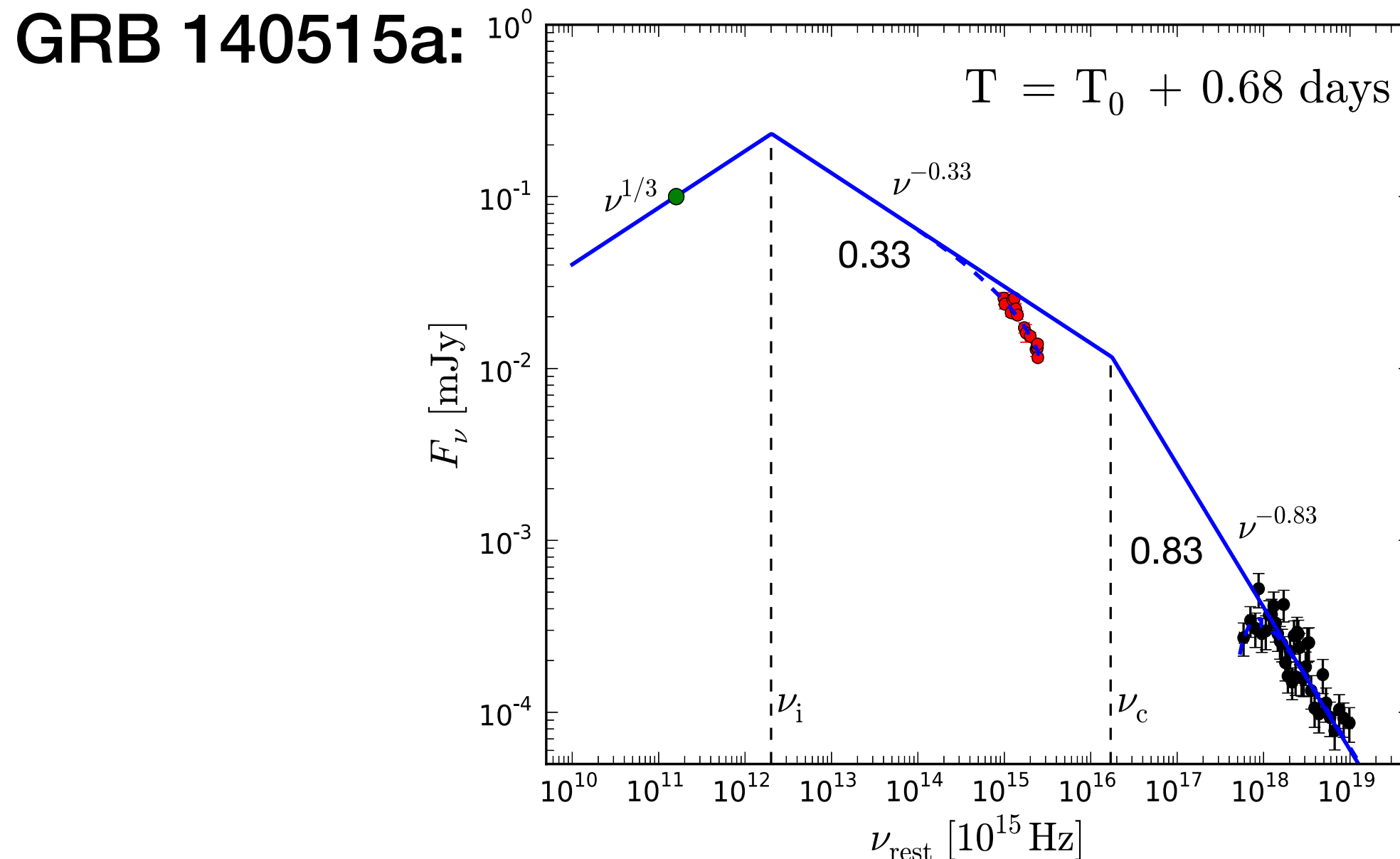
Shallow SED slope

GRB 060908: $\beta_{\text{opt}} = 0.33$

Covino et al 2010

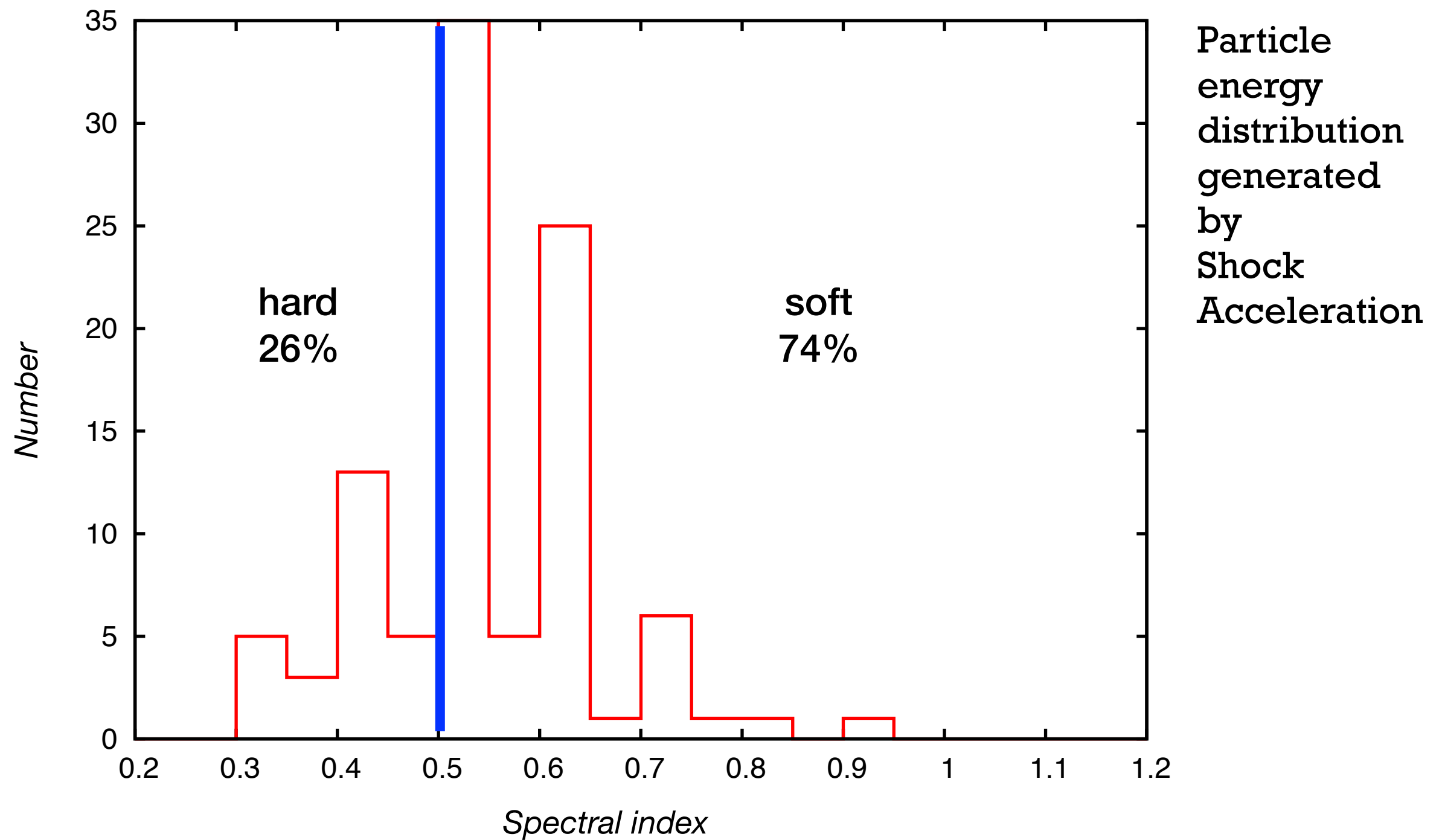
GRB 091127: $\beta_{\text{opt}} = 0.25, \beta_X = 0.75$
 $p = 1.5, q = 0.64$

Zhang et al 2015



Melandri et al 2015

Distribution of β of shell-type radio SNRs



Data from Cambridge SNR catalogue, D. Green

Summary

- Electron energy spectrum in GRB afterglows typically have $p \sim 2.2 - 2.5$, but in a minority of cases $p < 2$ have been inferred
- In case of hard energy spectrum the evolution of the upper cutoff energy affects the light curve
- Originally motivated to obtain consistency between spectral and temporal slopes of a few GRBs, the models required strong synchrotron cooling.
- More recently, cases of SED with flat spectrum below cooling frequency have been found
- What caused the diversity in energy distribution is unclear, shock acceleration theory tends to predict universal slope
- Even in shell SNRs a distribution of p is observed, with some fraction below 2