

Rare leptonic B decays

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on behalf of the LHCb collaboration



UNIVERSITY OF
CAMBRIDGE



SUSY
Mumbai 2017

A broad and versatile physics programme

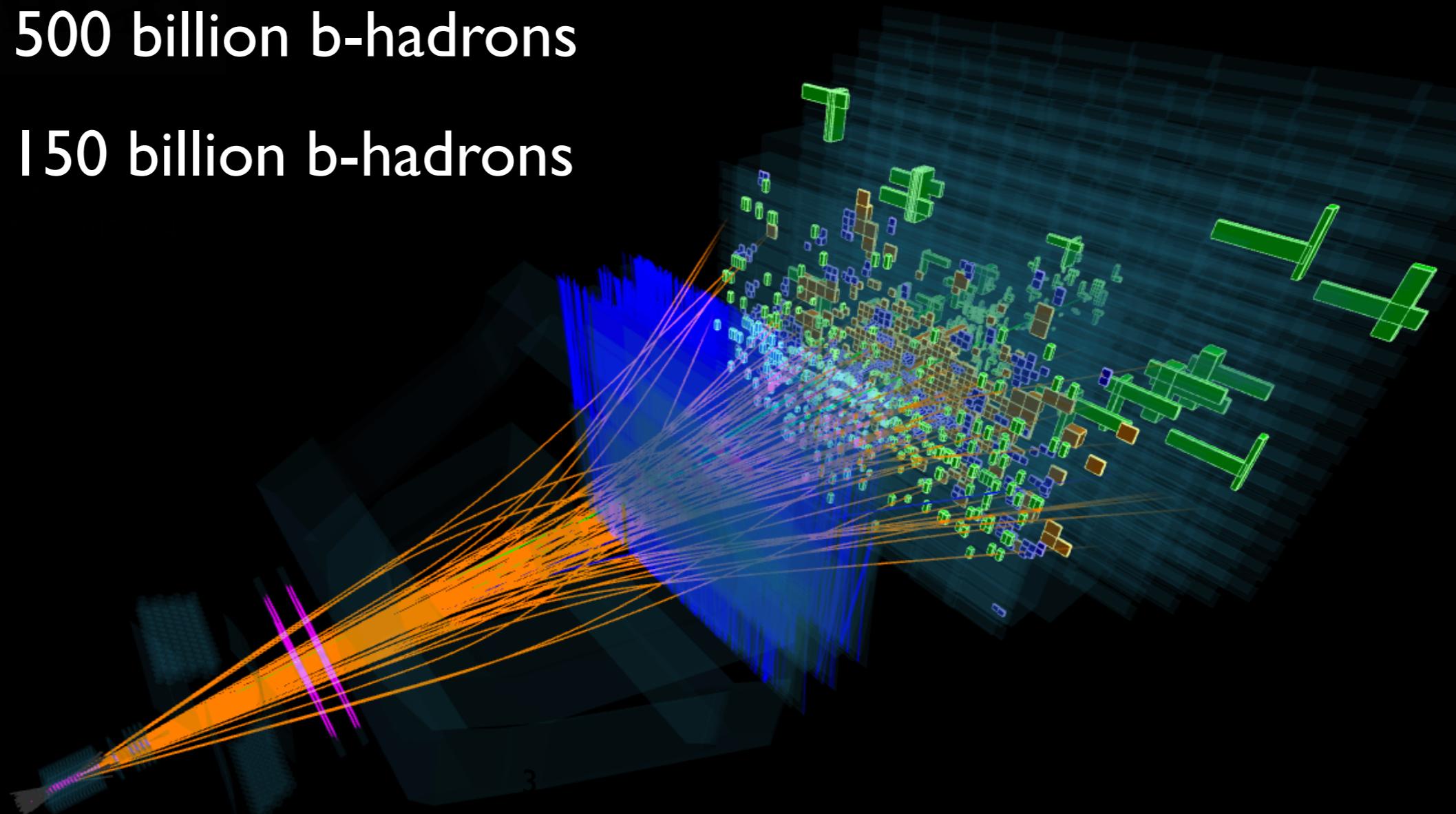
- CP violation in B decays
- New Physics searches at high energy scales
 - In rare beauty and charm decays
- Understanding QCD
 - Heavy flavour production, hadron spectroscopy (pentaquark states, bc states), unique fixed target programme
- Quark Gluon Plasma studies:
 - Rich heavy ion programs (production at p-Pb/Pb-p, fixed target p/pB-Ne)

LHCb is designed for B-physics

- Built in the high b-hadron production cross section region $2 < \eta < 5$

[PRL 118, 052002 (2017)]

- $\sigma(p p \rightarrow b\bar{b})^{\text{LHCb}} @ 13\text{TeV} \sim 155\mu\text{b}$
- Run I: 500 billion b-hadrons
- Run II: 1150 billion b-hadrons

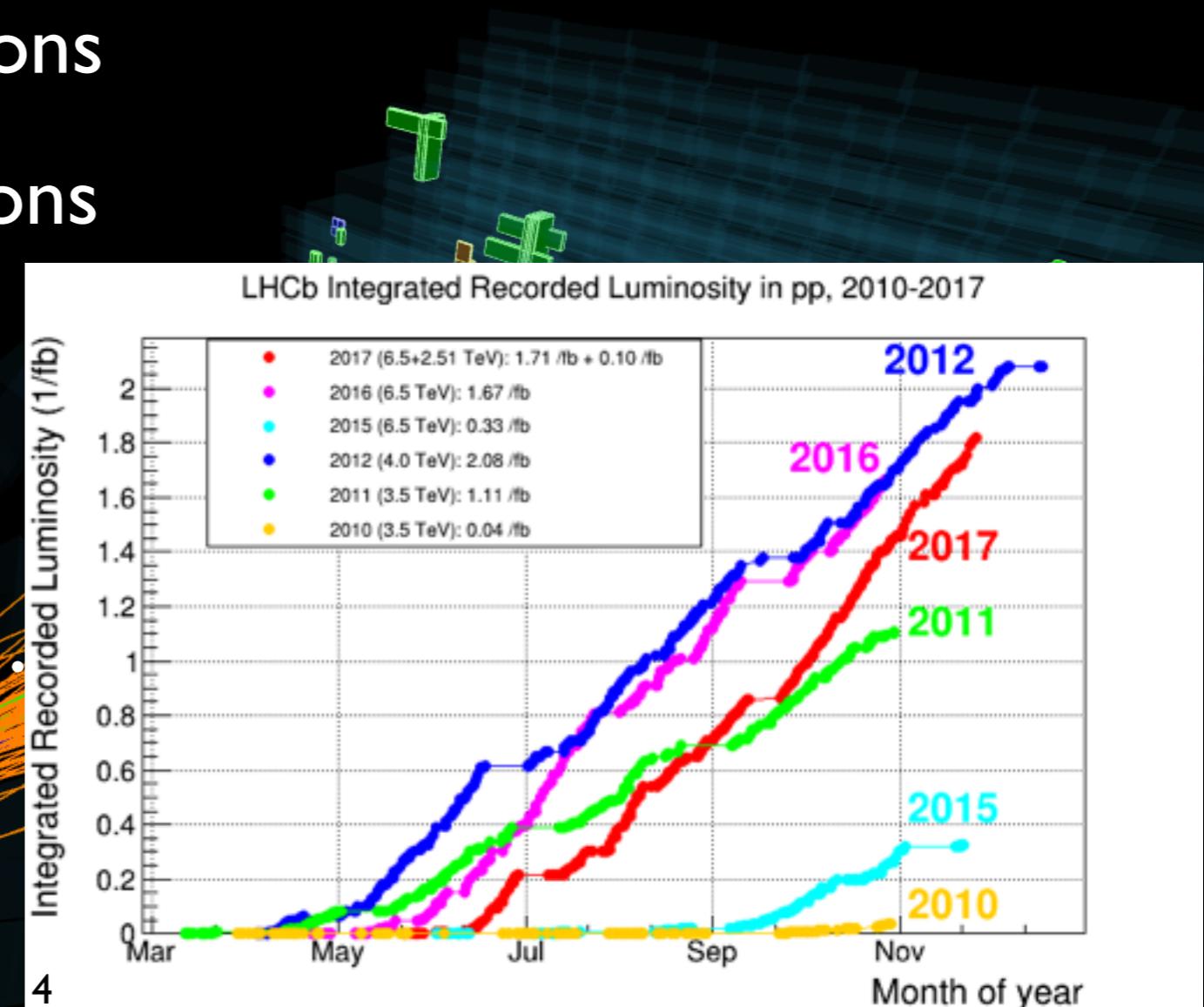


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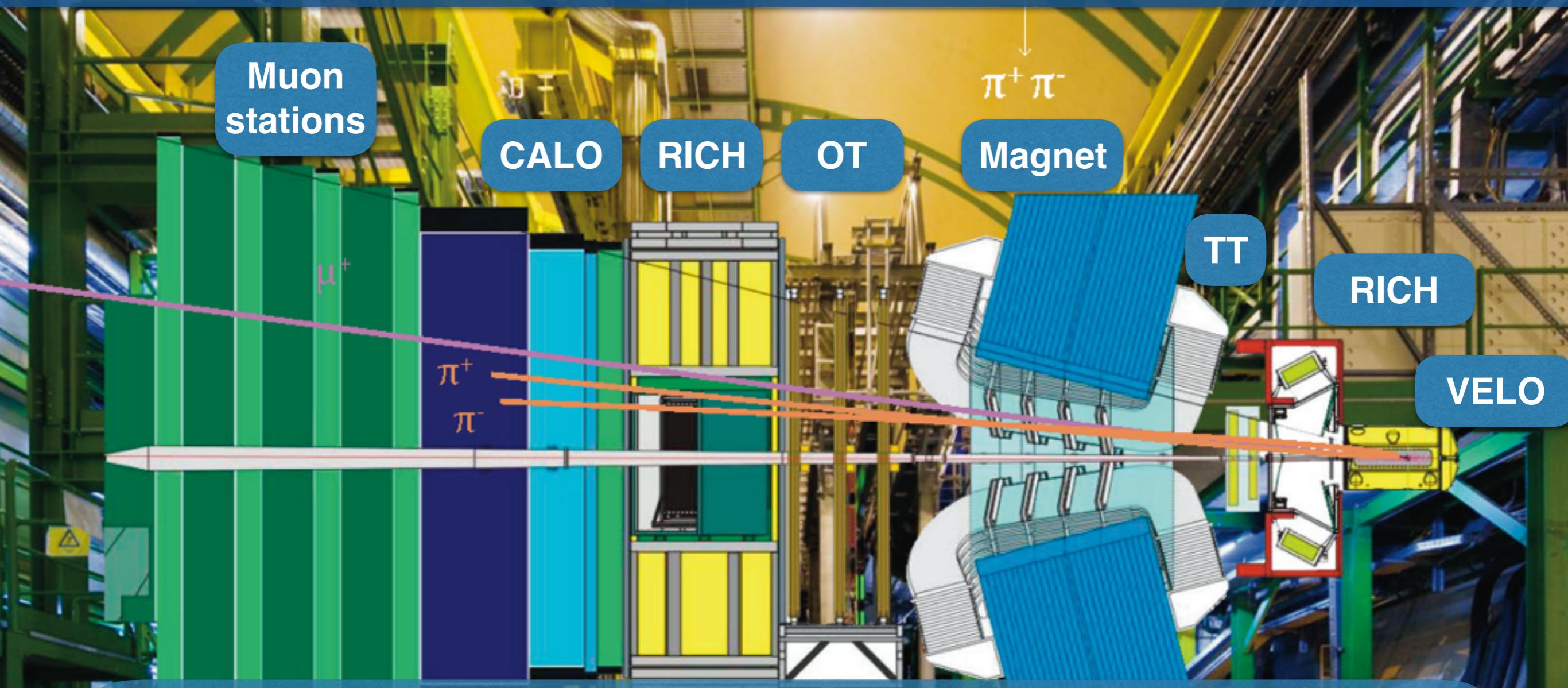
[PRL 118, 052002 (2017)]

- $\sigma(pp \rightarrow bb)^{\text{LHCb}} @ 13\text{TeV} \sim 155\mu\text{b}$
- Run I: 500 billion b-hadrons
- Run II: 1150 billion b-hadrons



- LHCb recorded 3fb^{-1} in Run I and 3.7fb^{-1} in Run II.
- High efficiency in 2017 (~91.4%)

LHCb detector @ LHC



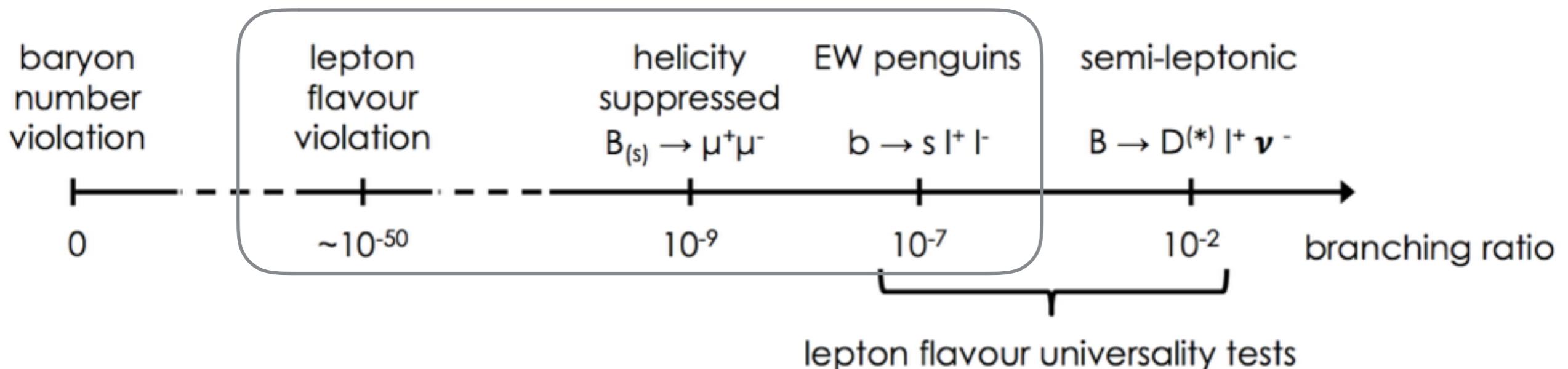
- Clean collision environment ($\mu \sim 1.6$) and high boost ($\gamma \sim 20$)
- Good mass resolution (~ 23 MeV for $B \rightarrow \mu^+ \mu^-$)

Excellent charged hadron identification, vertexing, high trigger and tracking efficiencies ($>\sim 90\%$) also in the low p_T range.

The large sample of precisely reconstructed B-decays is a true **goldmine** for New Physics searches.

Expose New Physics effects where the Standard Model is suppressed

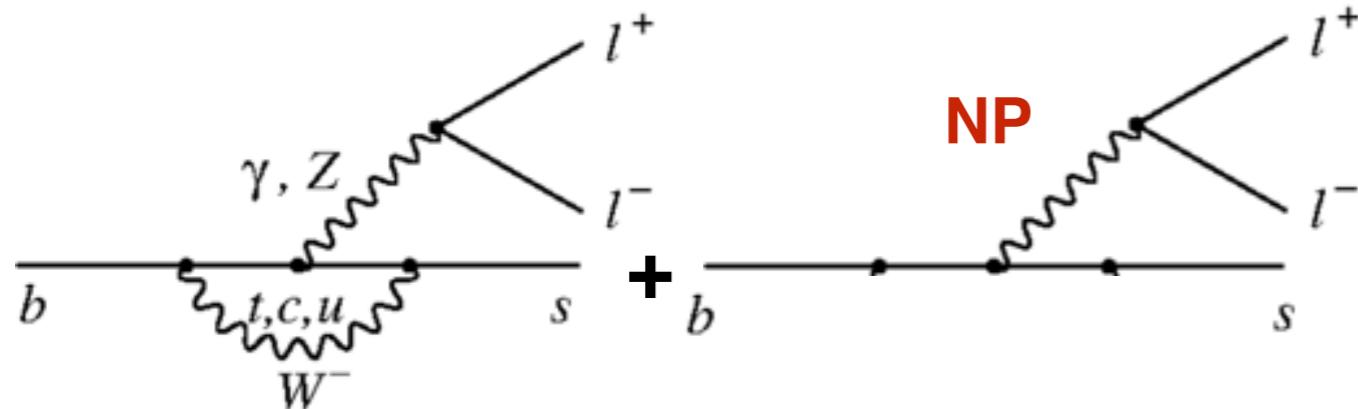
- $b \rightarrow s l l$ and $b \rightarrow d l l$ transitions are rare in the SM
No tree level contributions
(GIM, CKM, possibly helicity suppressed)



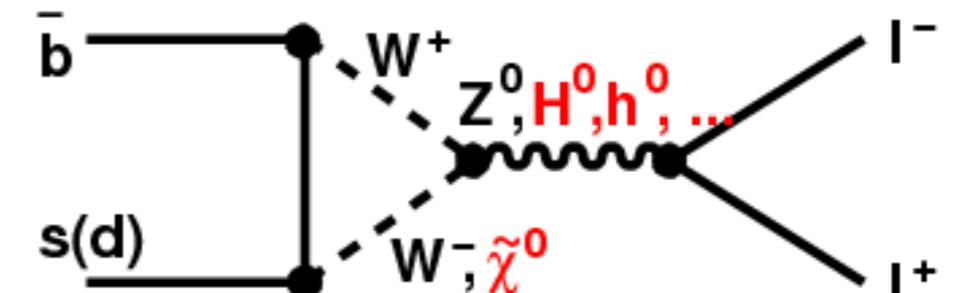
Expose New Physics effects where the Standard Model is suppressed

- New Physics can (in principle) enter at both tree and loop level:

NP at tree level



NP at loop level



$B_s \rightarrow \mu^+ \mu^-$ sensitive to Z 's up to
 $\sim 150 \text{TeV}$ or new scalars up to
 1000TeV

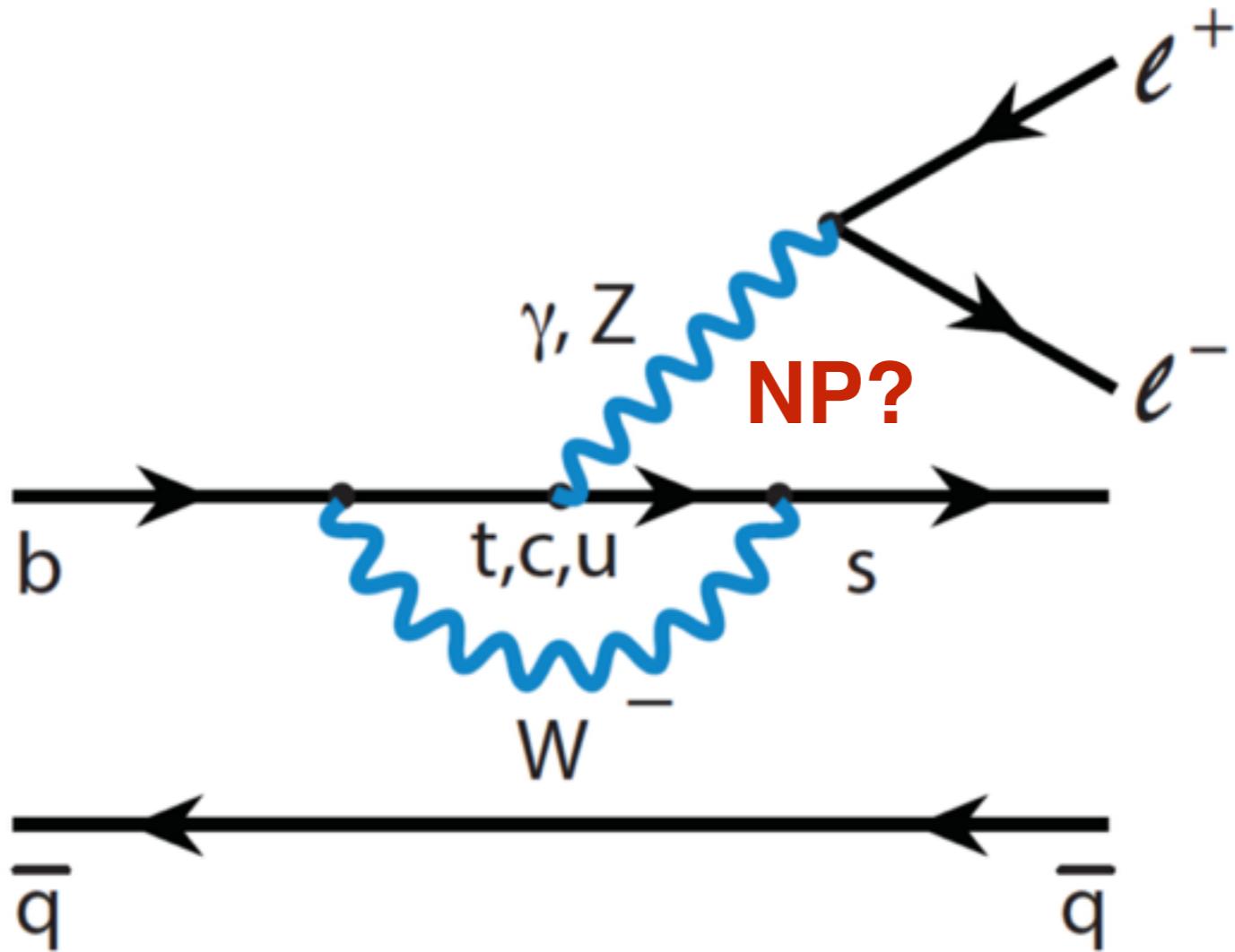
[A.Buras et al,
JHEP 1411 (2014) 121] 8

In $B_s \rightarrow \mu^+ \mu^-$ (pseudo)scalars can
bypass the helicity suppression

A strong case for indirect searches

- Indirect searches are sensitive to higher energy scales ($\sim 100\text{TeV}$)
- Historically, indirect searches have led the way in shaping the Standard Model (e.g. charm predicted 4 years before the direct proof)
- Complementary to (but no substitute for) the comprehensive direct NP search programmes



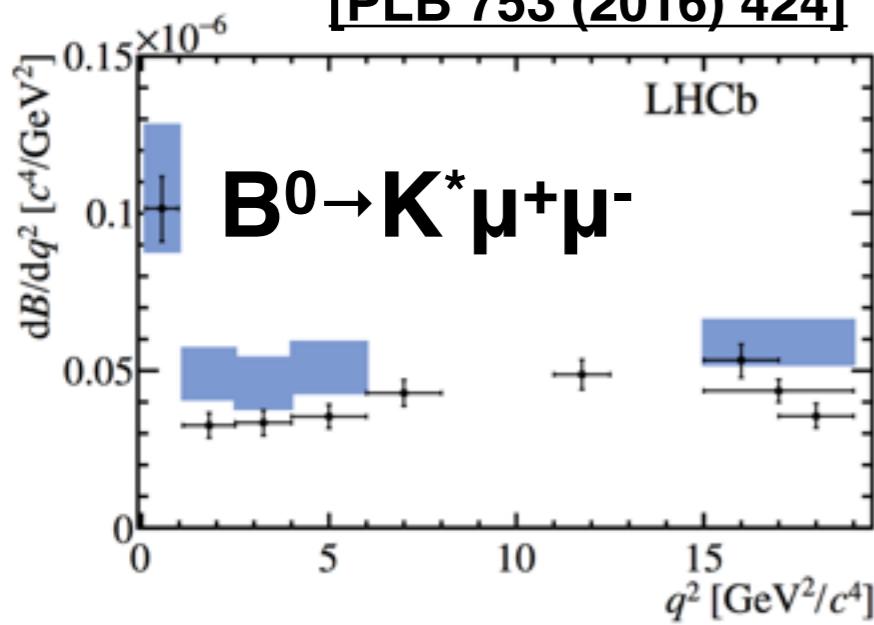


- For several reasons, rare decays involving $b \rightarrow sll$ transitions have emerged as possibly the most interesting phenomena in particle physics..

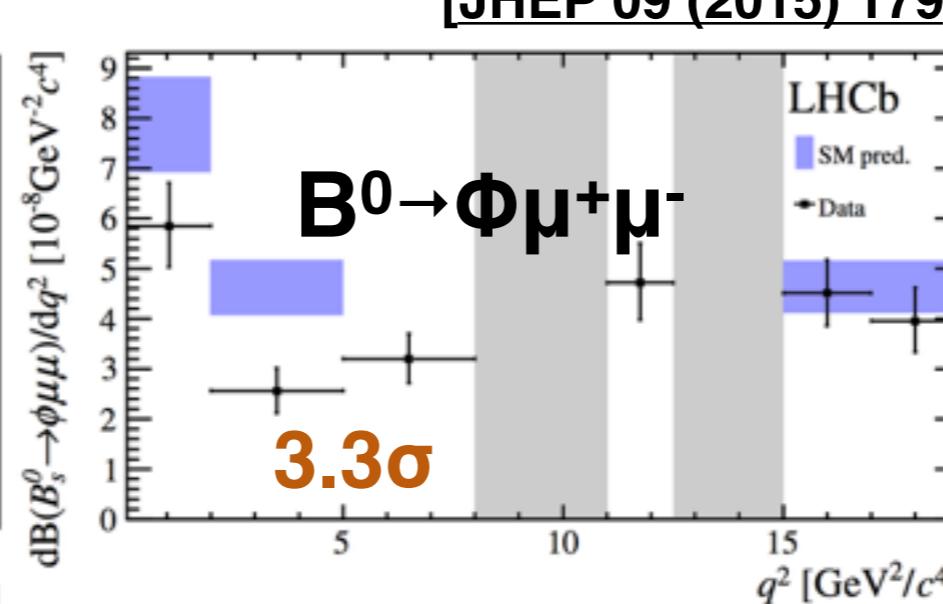
First: exclusive $b \rightarrow s \mu^+ \mu^-$ branching fractions

[JHEP 04 (2017) 142]

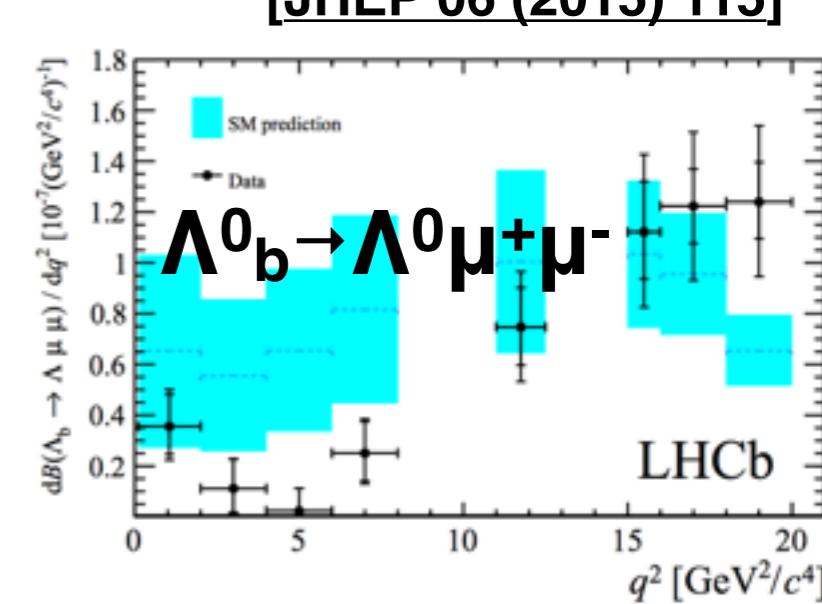
[PLB 753 (2016) 424]



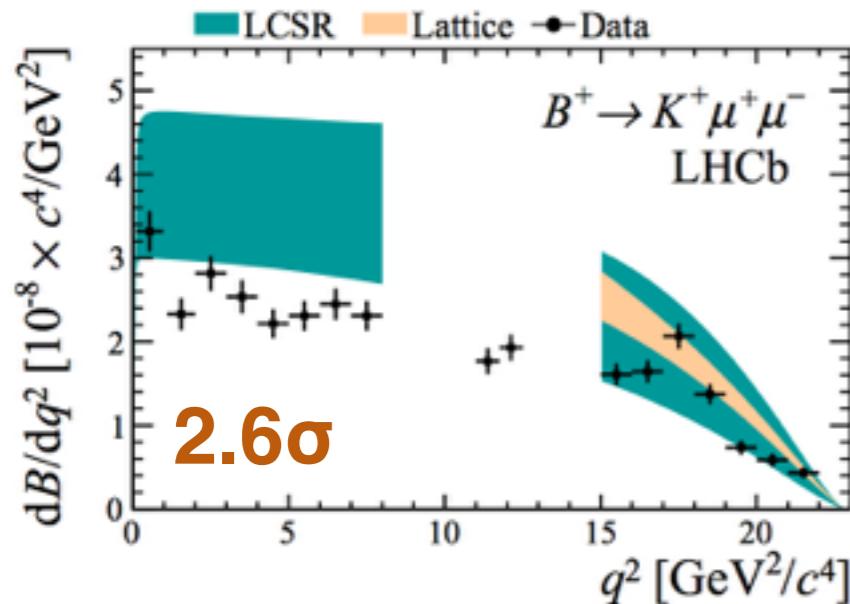
[JHEP 09 (2015) 179]



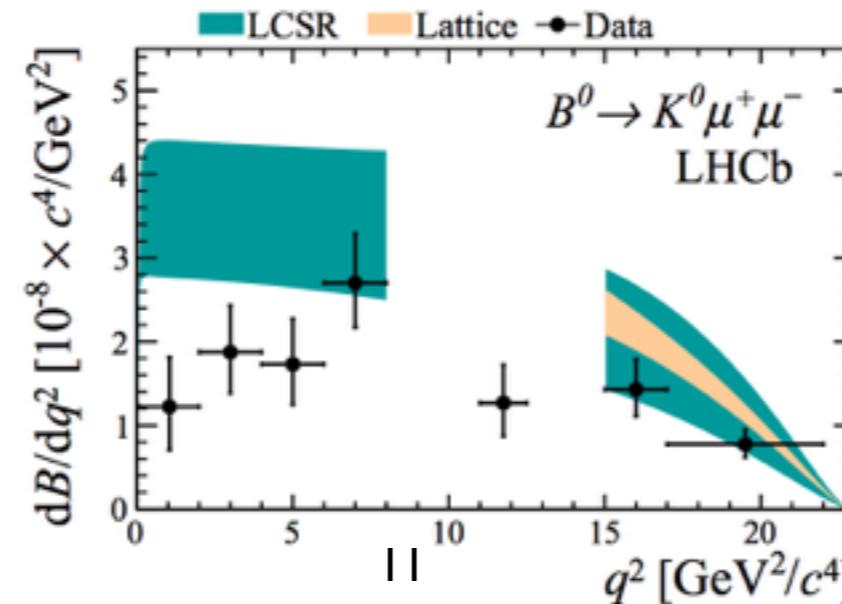
[JHEP 06 (2015) 115]



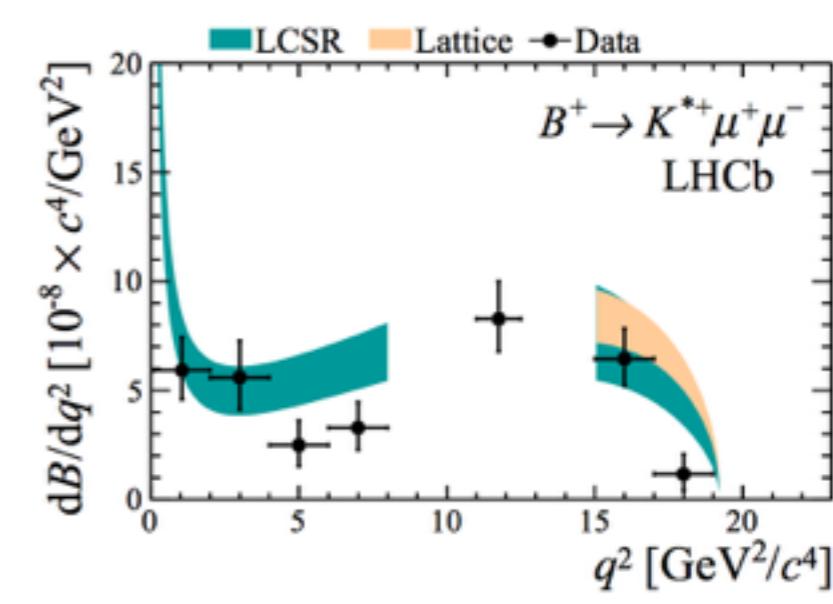
[JHEP 06 (2014) 133]



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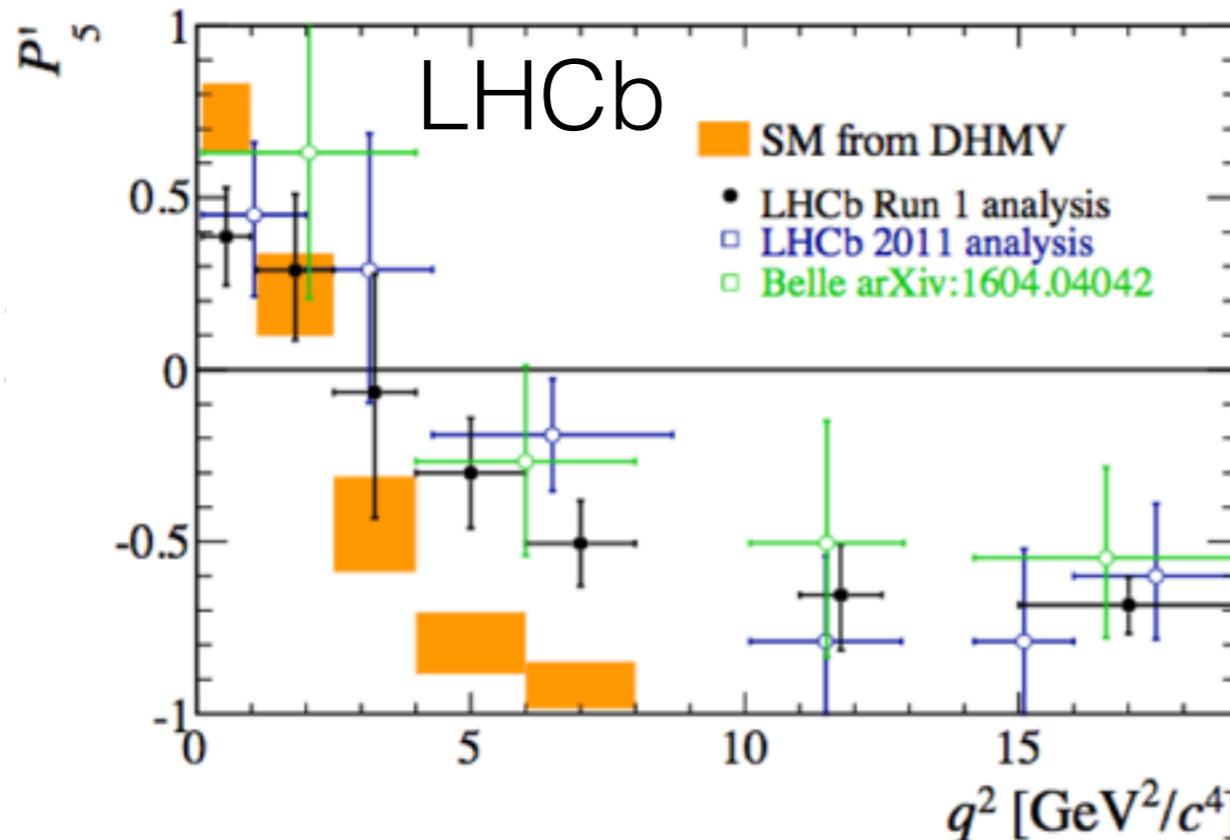
[JHEP 06 (2014) 133]



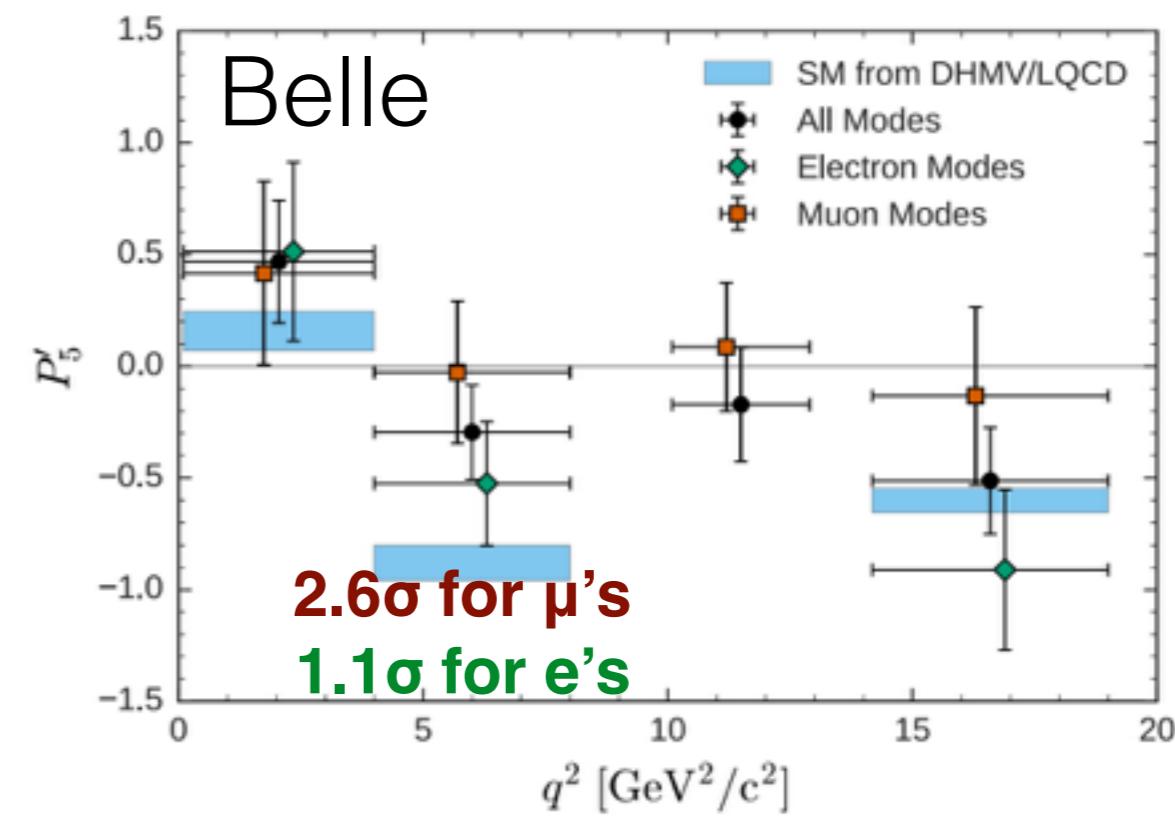
Second: tensions in $b \rightarrow s l^+ l^-$ angular observables

$B^0 \rightarrow K^* \mu^+ \mu^-$

[JHEP 02 (2016) 104]



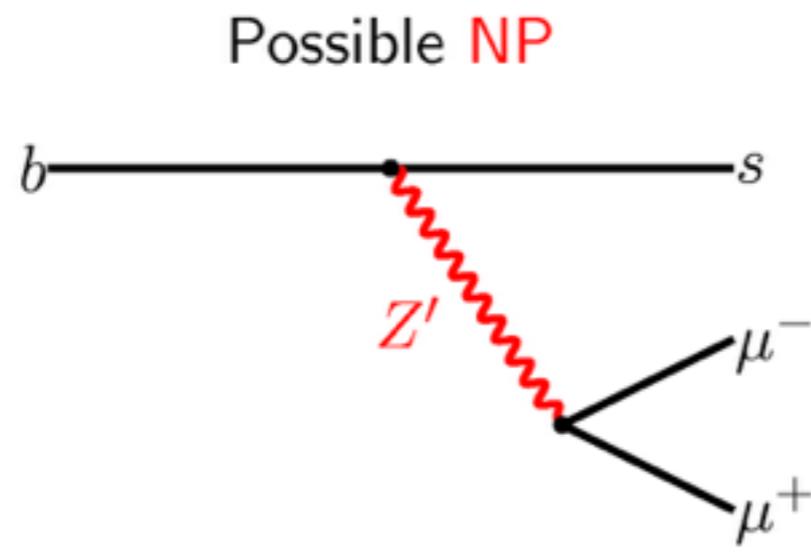
[PRL 118 (2017) 111801]



- Theoretically clean angular parameter P_5' diverges from the predictions (3.4σ)
- The tension is larger for muons

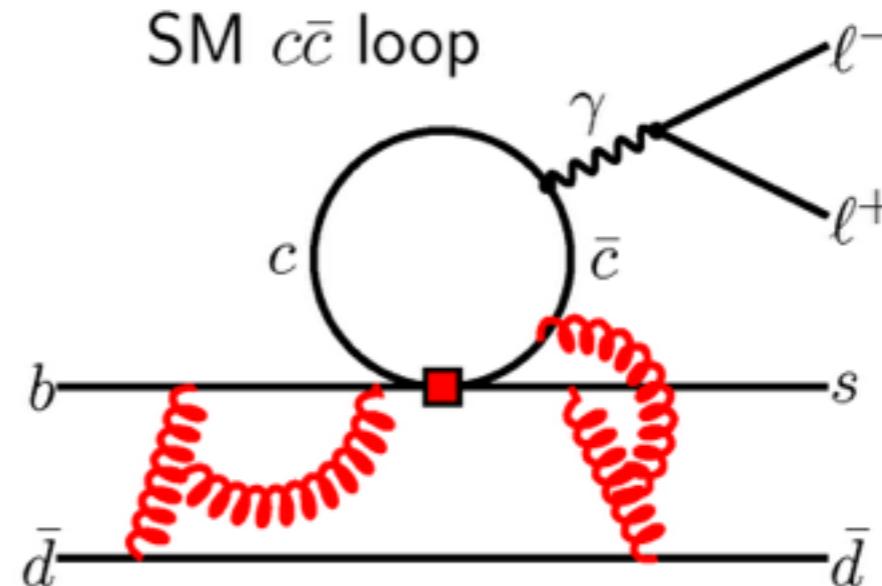
New Physics is not the only possible explanation to these effects:

Z', leptoquarks,...



$$C_9 + C_9^{NP}$$

Hadronic SM effects



$$C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{res}(q^2)$$

Long-distance charm resonance effects far from the resonances on the q^2 plane.

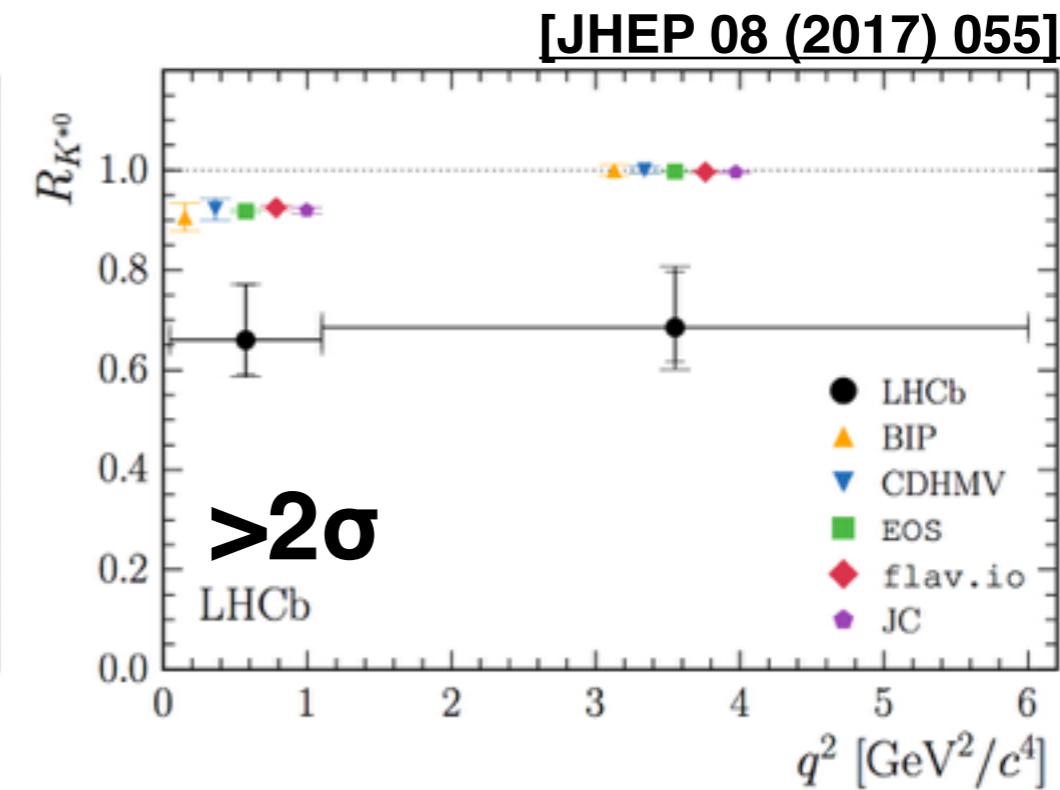
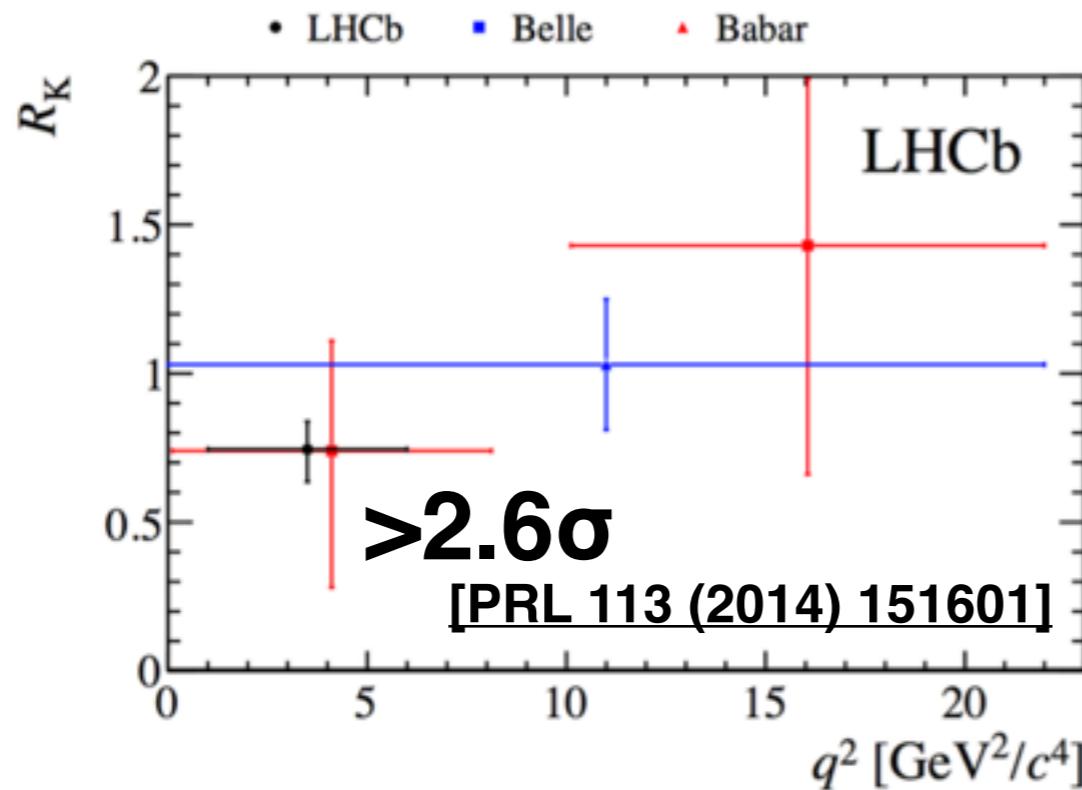
But...if it were due to hadronic effects..

..then we should see no deviations from the SM in the ratios of $b \rightarrow sll$ branching fraction.

Third: tensions in ratios:

$$b \rightarrow s \mu^+ \mu^- / b \rightarrow s e^+ e^-$$

- The measured muon and electron mode ratios are lower than predicted in the SM (LFU)

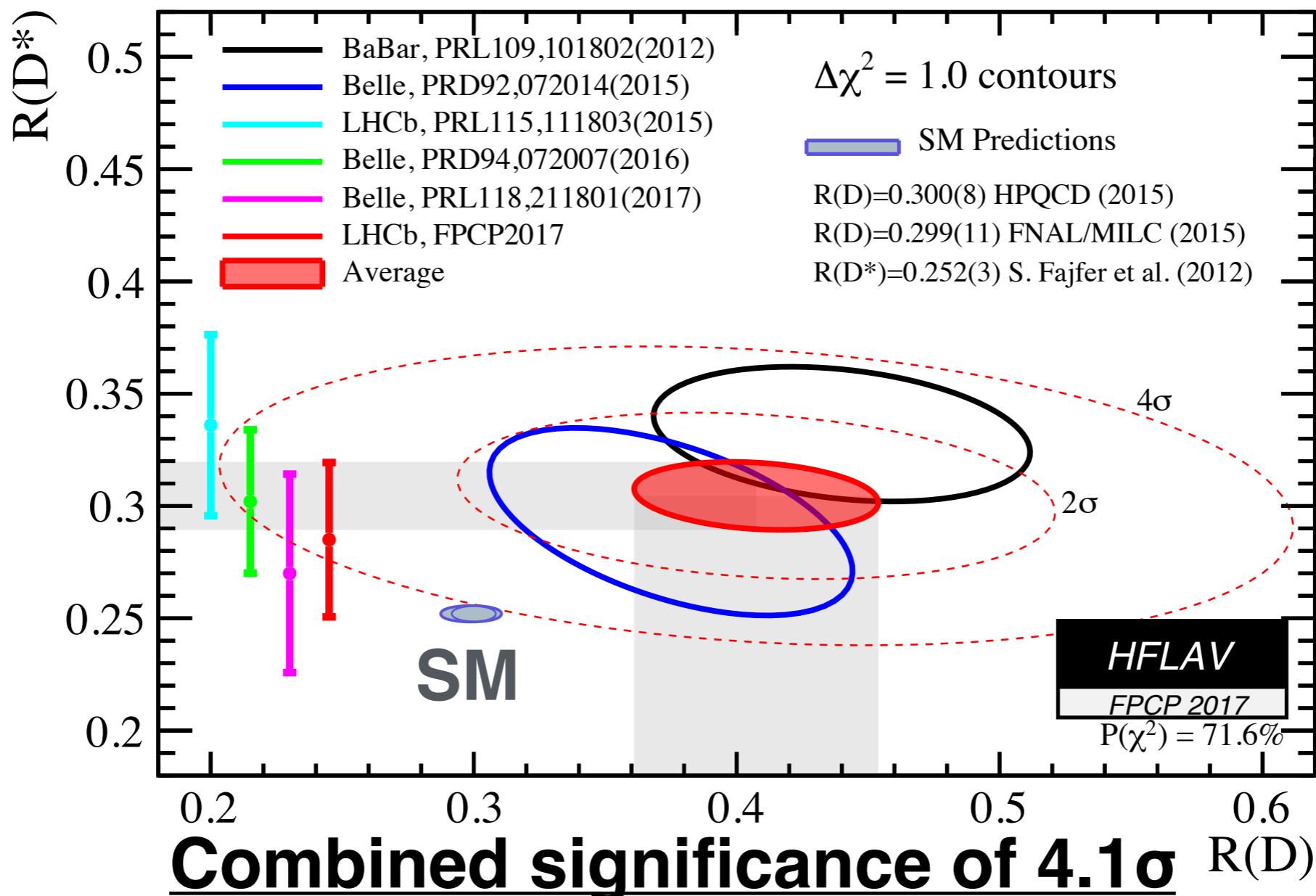


$$\mathcal{R}(K) \equiv \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}$$

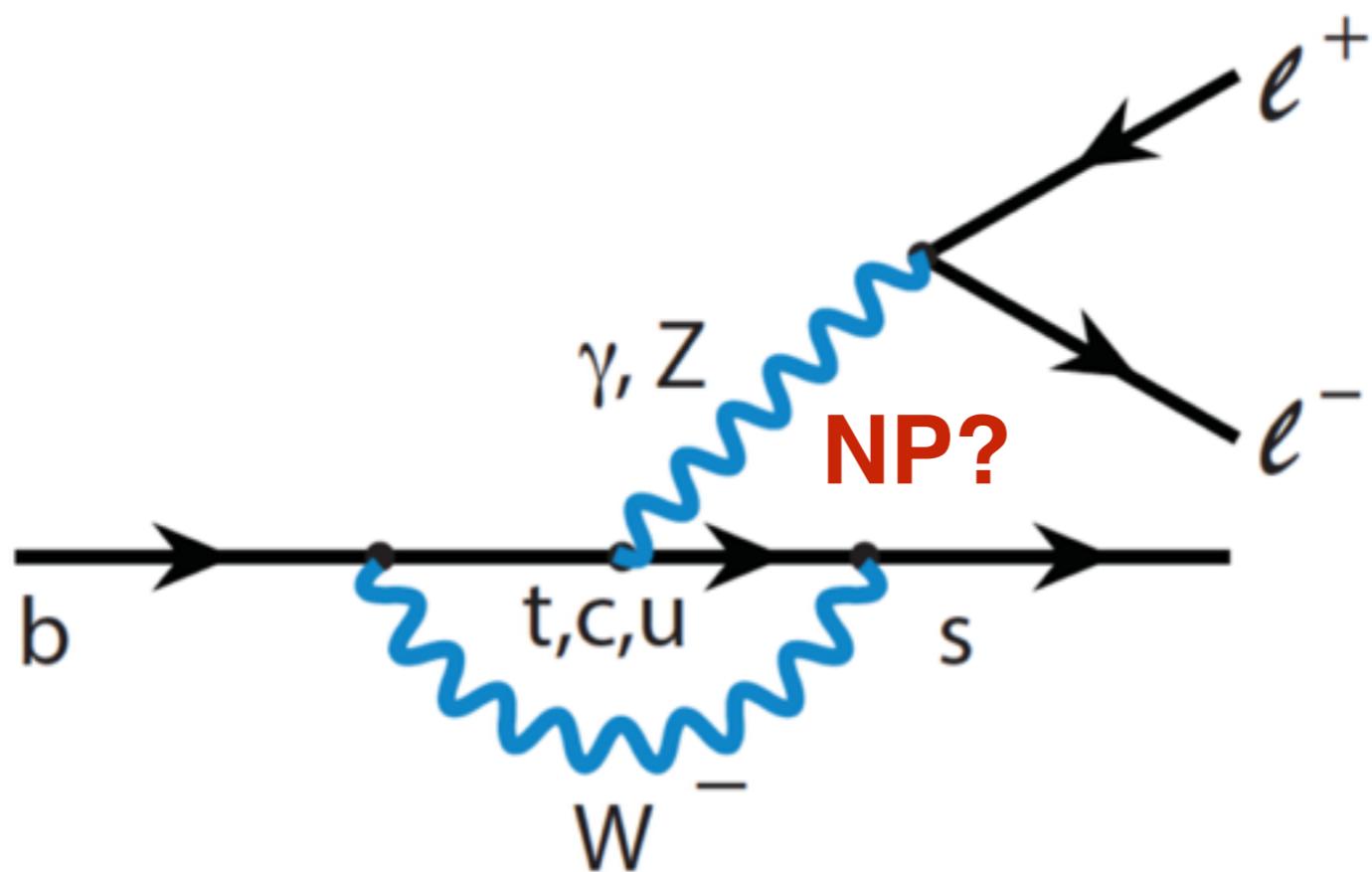
$$\mathcal{R}(K^*) \equiv \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)}$$

... a footnote: LFU divergencies are also seen in the semi-leptonic B decays via $b \rightarrow cl^+l^-$ transitions:

$$\mathcal{R}(D^{(*)}) \equiv \frac{\mathcal{B}(B^0 \rightarrow D^{(*)-} \tau^+ \nu_\tau^-)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \mu^+ \nu_\mu^-)}$$



What can fully leptonic B-decays add?



All B-decays include processes over a wide energy range:

0.2GeV.....4GeV.....80GeV.....~ 100 TeV ?

Λ_{QCD}	Λ_b	Λ_{EW}	Λ_{NP}
(non-perturbative regime)	(b mass)	(W mass)	(new physics scale)

and can be described by the **effective field theory** and **operator product expansion** by splitting the scale at b mass (μ_b):

$$A(B \rightarrow f) = \langle f | \mathcal{H}_{\text{eff}} | B \rangle = \frac{G_F}{\sqrt{2}} \sum_i \lambda_{CKM} \underbrace{C_i(\mu_b)}_{\text{Wilson coefficients}} \underbrace{\langle f | \mathcal{Q}_i(\mu_b) | B \rangle}_{\text{Hadronic matrix el.}}$$

Wilson coefficients **Hadronic matrix el.**
(perturbative) (include non-perturbative QCD)

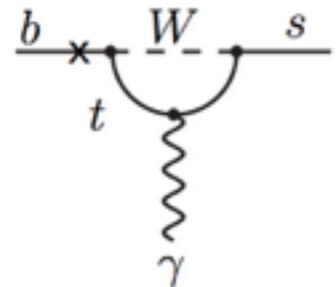
Leptonic modes

$$\langle ll | j_{ll} \cdot j_{qq} | B_q \rangle = \langle ll | j_{ll} | 0 \rangle \cdot \underbrace{f_{Bq}}_{\text{Lattice QCD}}$$

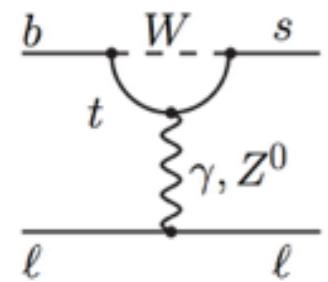
Semi-leptonic modes:

$$\langle llM | j_{ll} \cdot j_{qq} | B \rangle = \langle ll | j_{ll} | 0 \rangle \cdot \underbrace{F(q^2)}_{\text{Lattice QCD (large } q^2 \text{)}} + \underbrace{C_{\text{non-fact}}}_{\text{Light Cone Sum Rules (small } q^2 \text{)}} + \underbrace{\text{corrections}}_{\text{}} \text{ corrections}$$

The A-V semi-leptonic current (O_{10}) contributes to both semi-leptonic and fully leptonic B-decays:

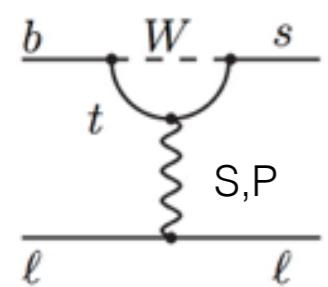


Electromagnetic penguin



Semi-leptonic vector current

Semi-leptonic A-V current



Scalar

Pseudo-scalar

$$Q_7^{(')} = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_{R(L)} b) F^{\mu\nu}$$

$$Q_9^{(')} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{l} \gamma^\mu l)$$

$$Q_{10}^{(')} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{l} \gamma^\mu \gamma_5 l)$$

$b \rightarrow s l^+ l^-$

$B_{(s)}^0 \rightarrow l^+ l^-$

$$Q_S^{(')} = \frac{e^2}{16\pi^2} (\bar{s}_{L(R)} b_{R(L)}) (\bar{l} l)$$

$$Q_P^{(')} = \frac{e^2}{16\pi^2} (\bar{s}_{L(R)} b_{R(L)}) (\bar{l} \gamma_5 l)$$

*In SM only O_{10} contributes to the leptonic modes, Higgs contribution via O_S is negligible

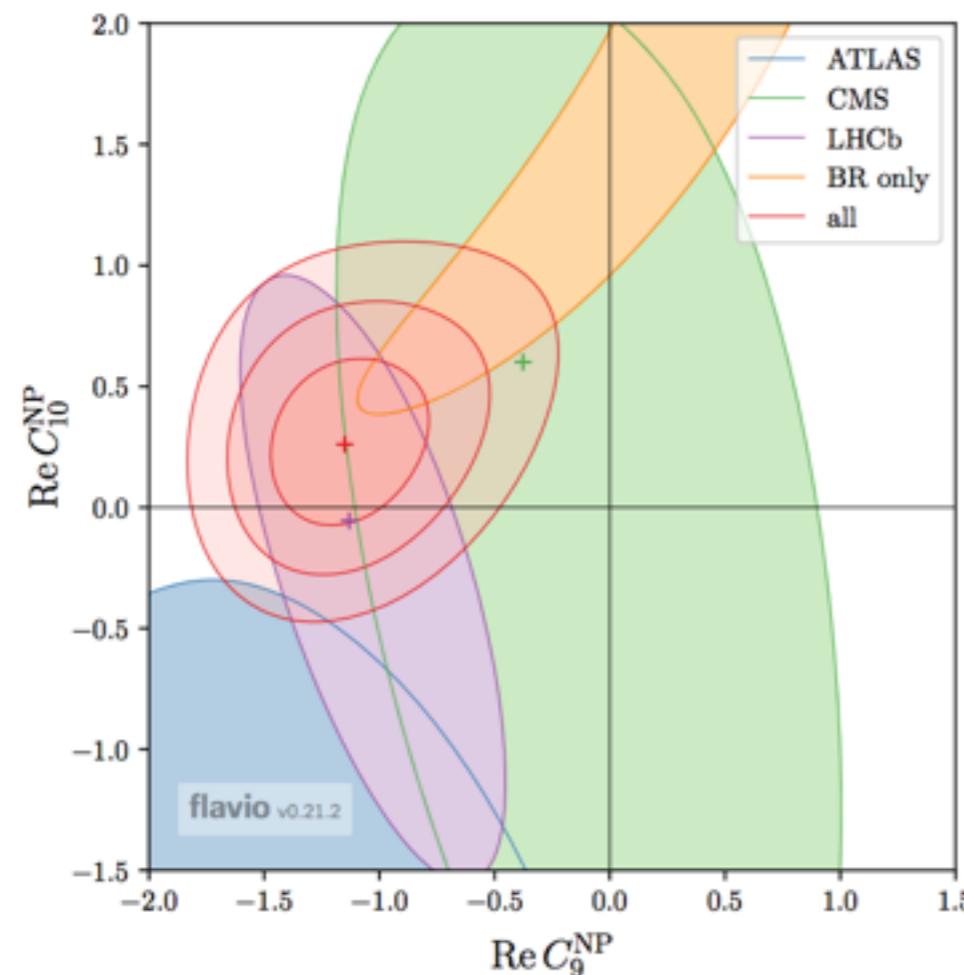
► **New Physics** can

- alter the SM operator contributions (Wilson coefficients)
- enter through new operators (right-handed Q's, $Q_{S,P}$)

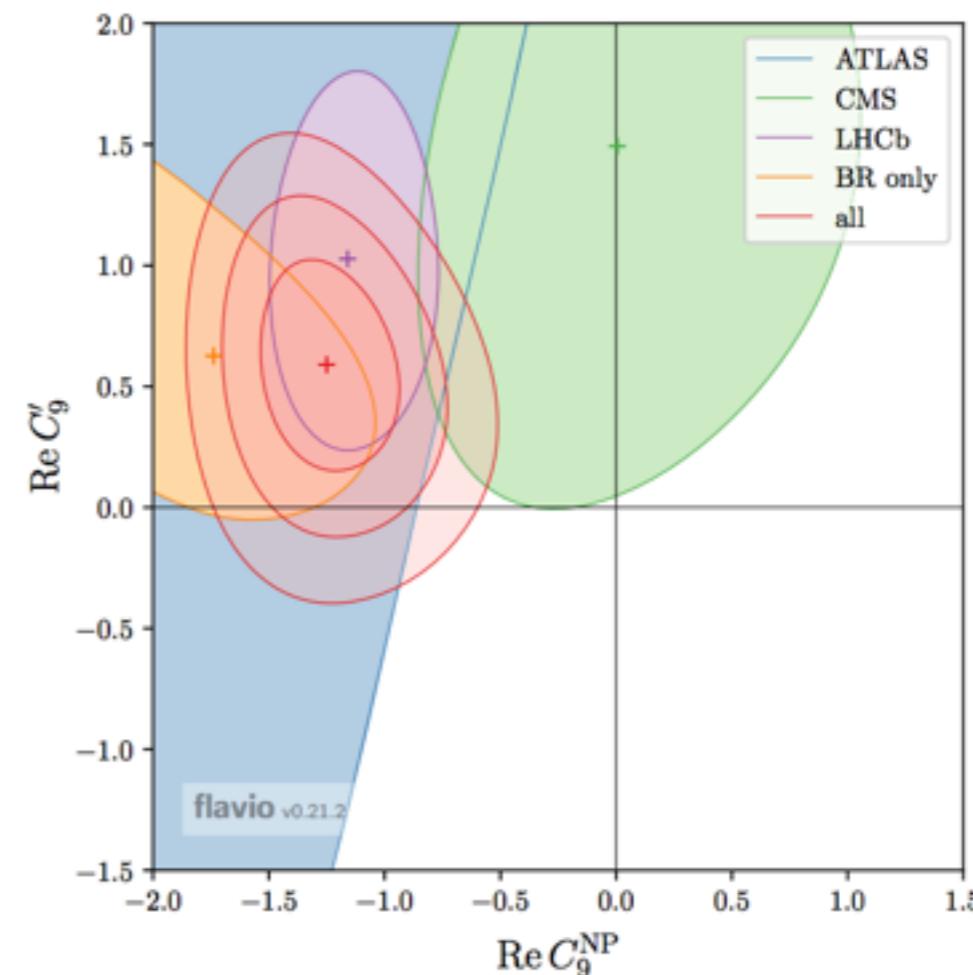
The Wilson coefficients are determined from global $b \rightarrow s l^+ l^- (\gamma)$ analysis, which point to

- tensions at $4-5\sigma$ level w.r.t SM in left-handed muon couplings
- two favoured (model independent) solutions to the tensions:

a) $C_9^{\text{NP}} = -C_{10}^{\text{NP}}$



b) $C_9^{\text{NP}} < 0$



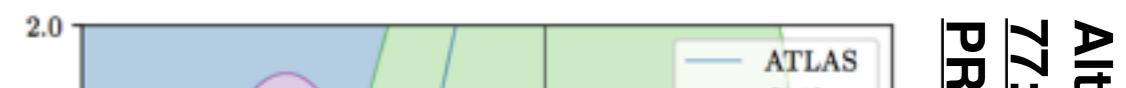
Altmannshofer et al [EPJC (2017) 77:377], Capdevila et al [PSI-PR-17-05]

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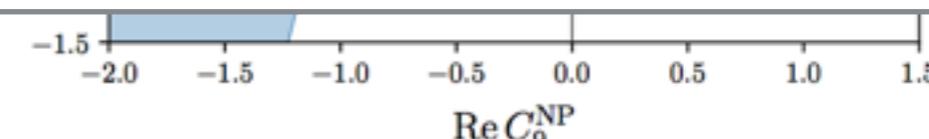
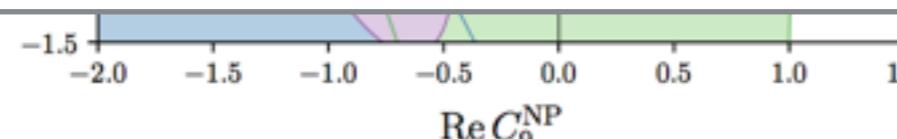
$$a) C_9^{\text{NP}} = -C_{10}^{\text{NP}}$$

$$b) C_9^{\text{NP}} < 0$$



Rare fully leptonic B decays provide:

- a clean, reliable and complementary way to determine the axial-vector contribution (C_{10}^{NP})
- also sensitive to new (pseudo-)scalar contributions ($C_{P,S}$ free from helicity suppression)



(~90 measurements e.g. in Descotes-Genon, Hofer, Matias, Virto [[JHEP 06 \(2016\) 092](#)],
Altmannshofer, Straub [[EPJC 75\(8\) \(2015\) 382](#)], Hurth, Mahmoudi, Neshatpour [[arXiv:1603.00865](#)])

The experimental success story of

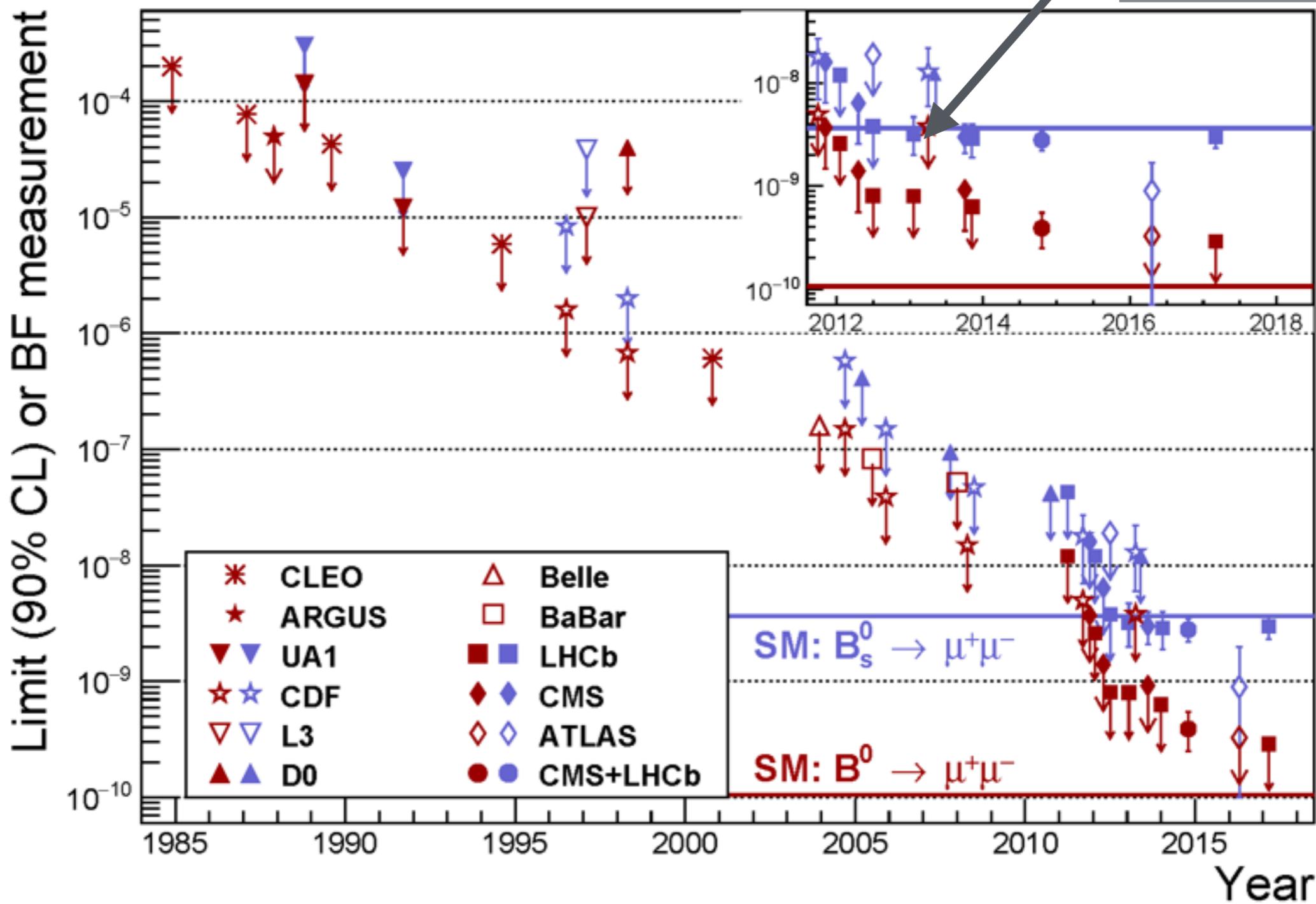
$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

One of the most important indirect
New Physics probes at the LHC.

Persistence that paid off after 30 years

[PRL 110, 021801 (2013)]

2013: first evidence
seen by LHCb

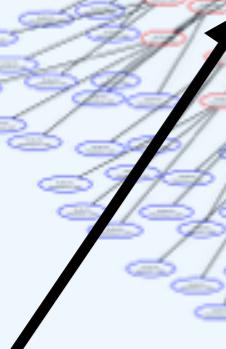
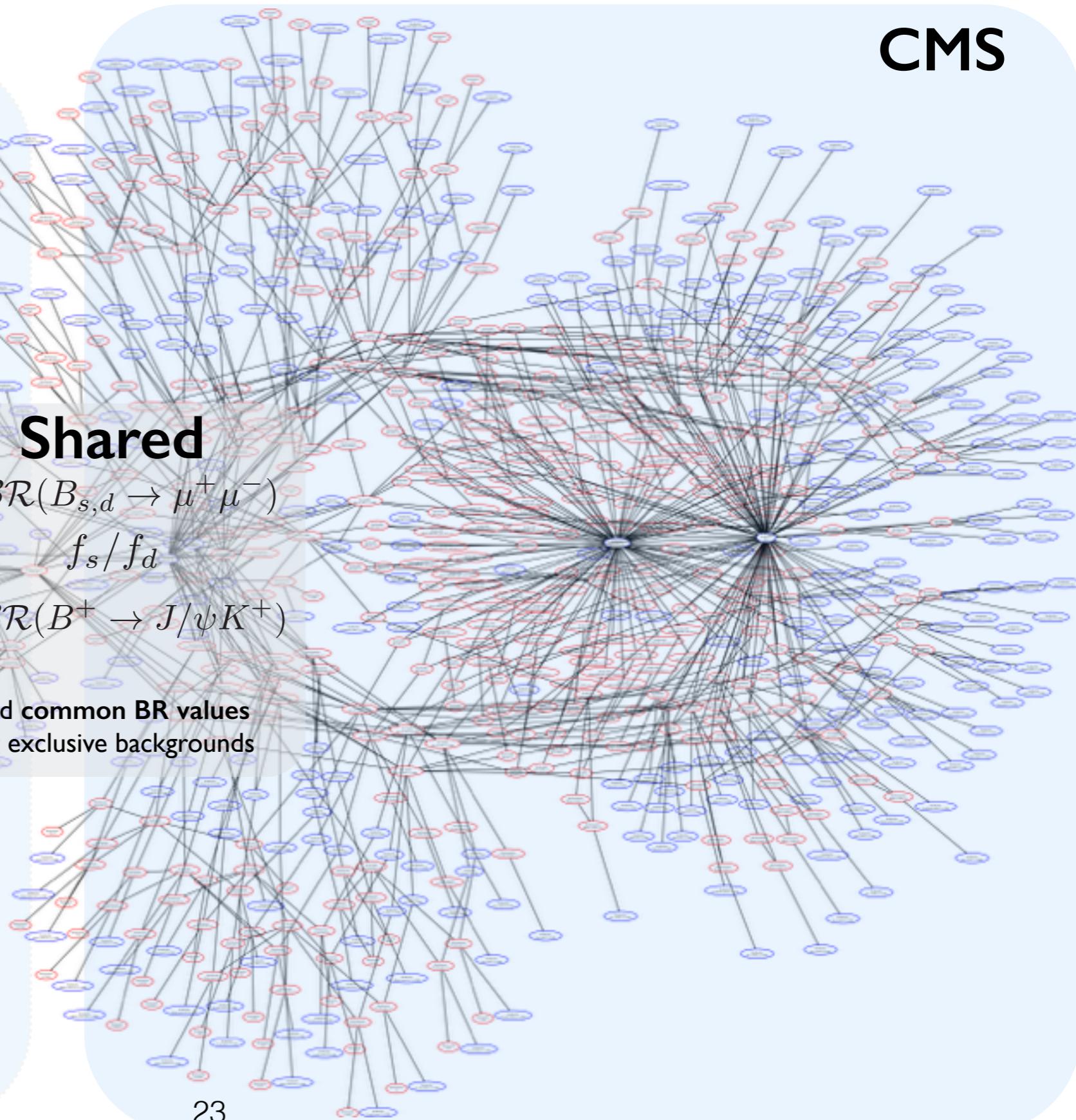


The combined Run I $B^0_{(s)} \rightarrow \mu^+ \mu^-$ analysis models

CMS

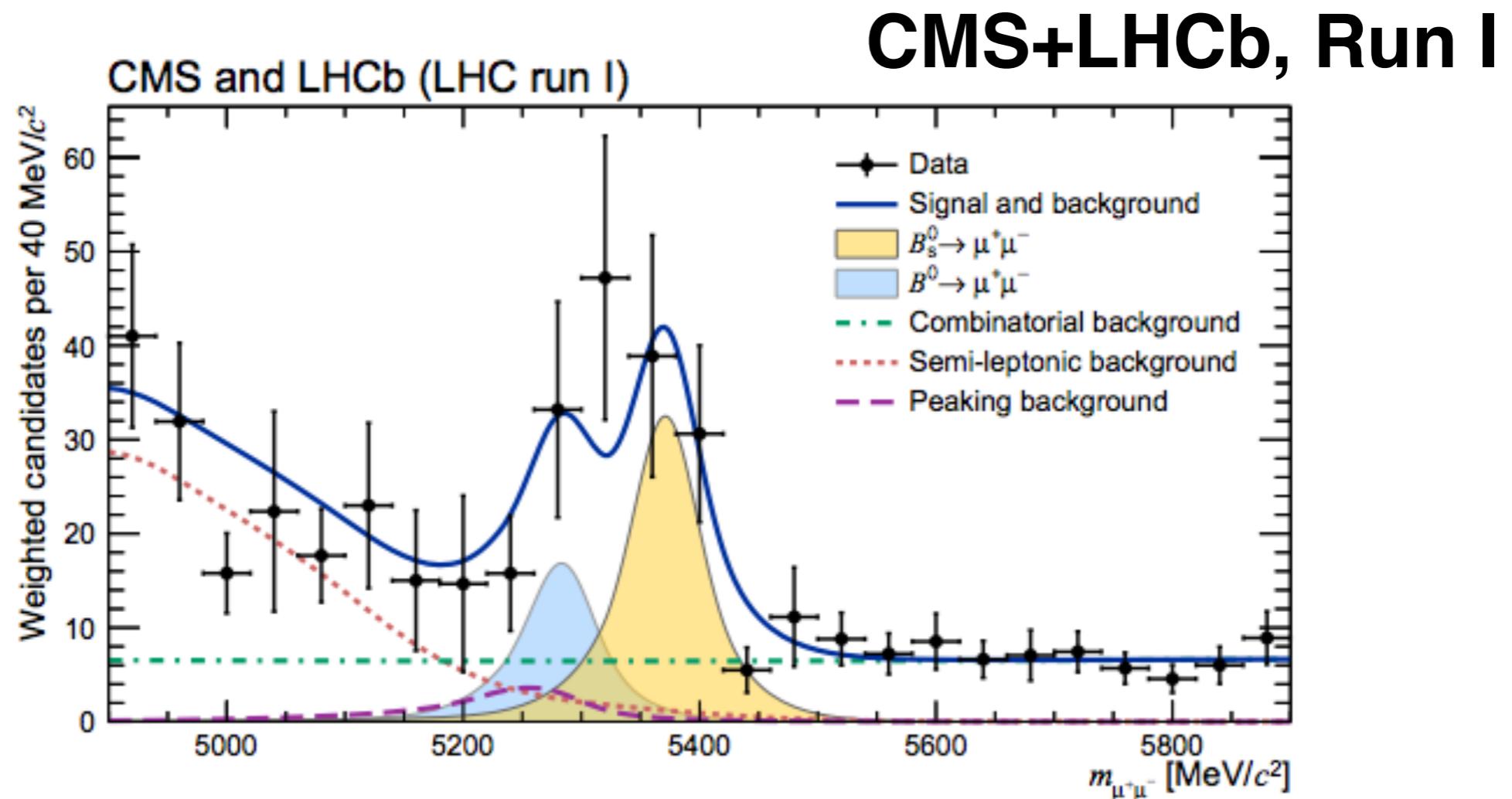
LHCb

MisID

Peaking bkg
shape pars.Mass and signal shape
parameters

2015

The first observation of $B_s \rightarrow \mu\mu$ decay and the first evidence of $B_d \rightarrow \mu\mu$:



► The fitted central BF values

$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-) = 2.8_{-0.6}^{+0.7} \times 10^{-9}$$

6.2 σ obs. (expected 7.2 σ in SM)

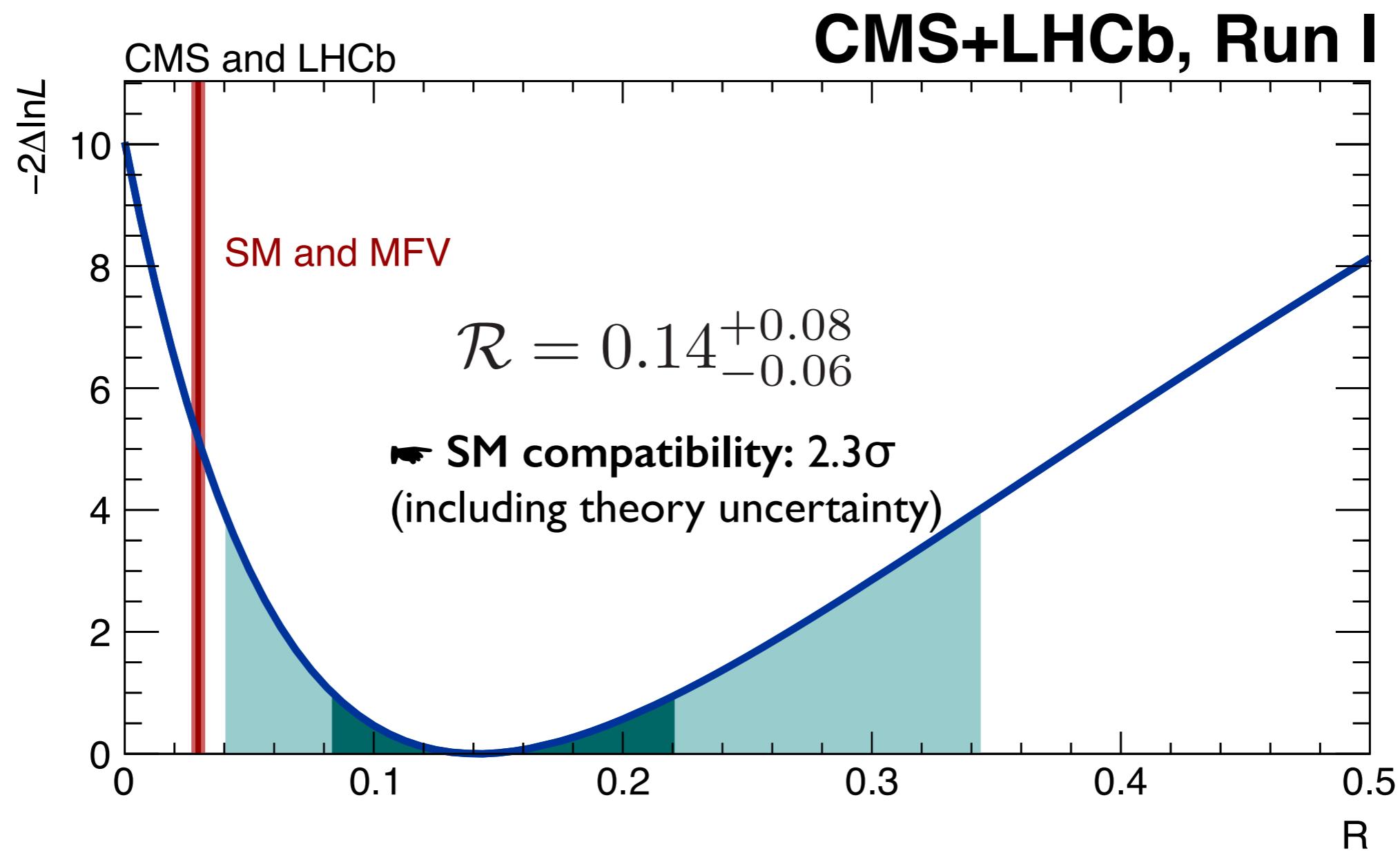
$$\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-) = 3.9_{-1.4}^{+1.6} \times 10^{-10}$$

3.2 σ obs. (expected 0.8 σ in SM)

*Cross-checked with Feldman-Cousins:
3.0 σ (official significance)

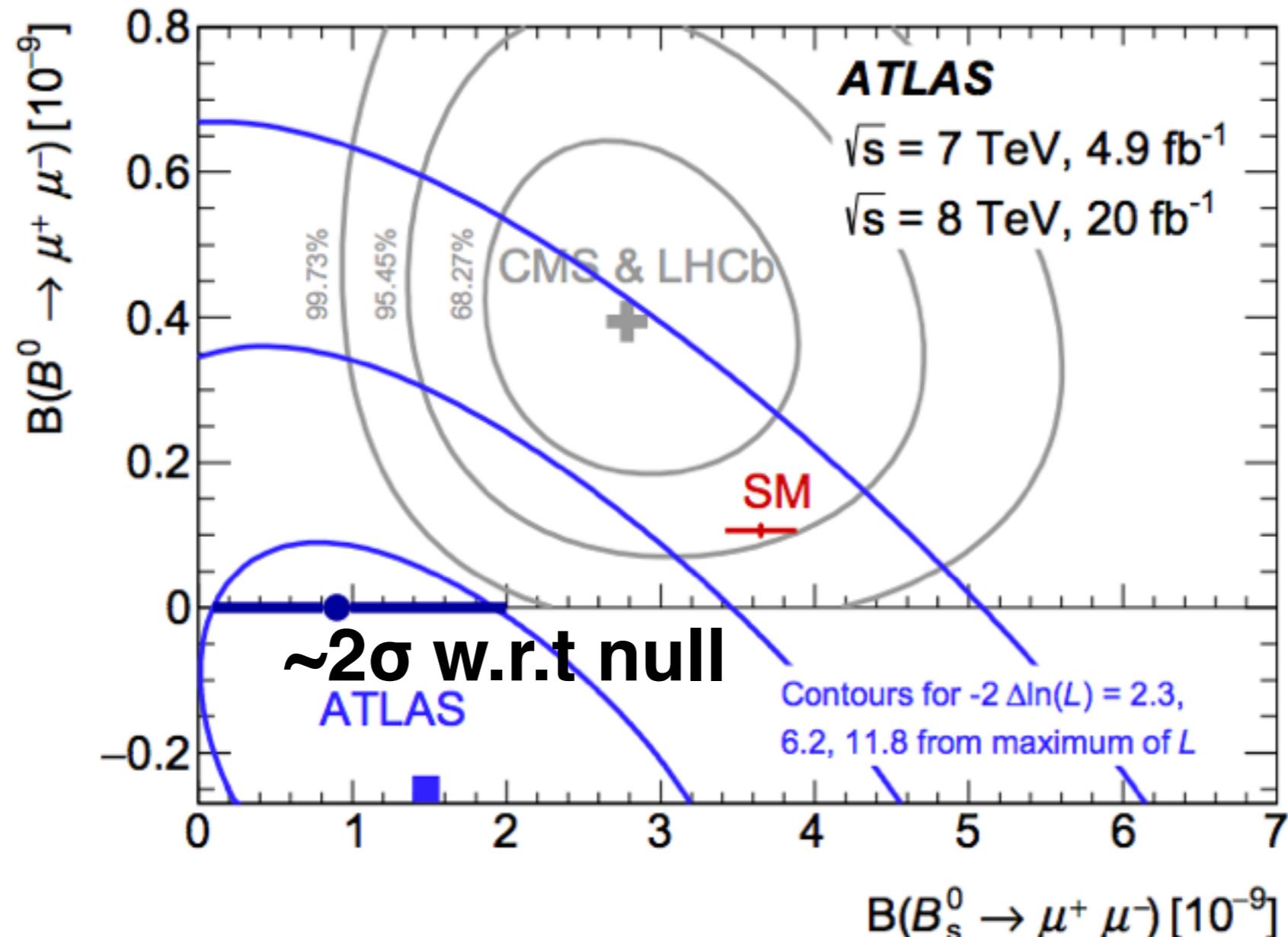
2015

The ratio $R = \text{BF}(B_d \rightarrow \mu\mu) / \text{BF}(B_s \rightarrow \mu\mu)$ is a precise test of minimal flavour violation (MFV):



Run I results from ATLAS are in agreement.

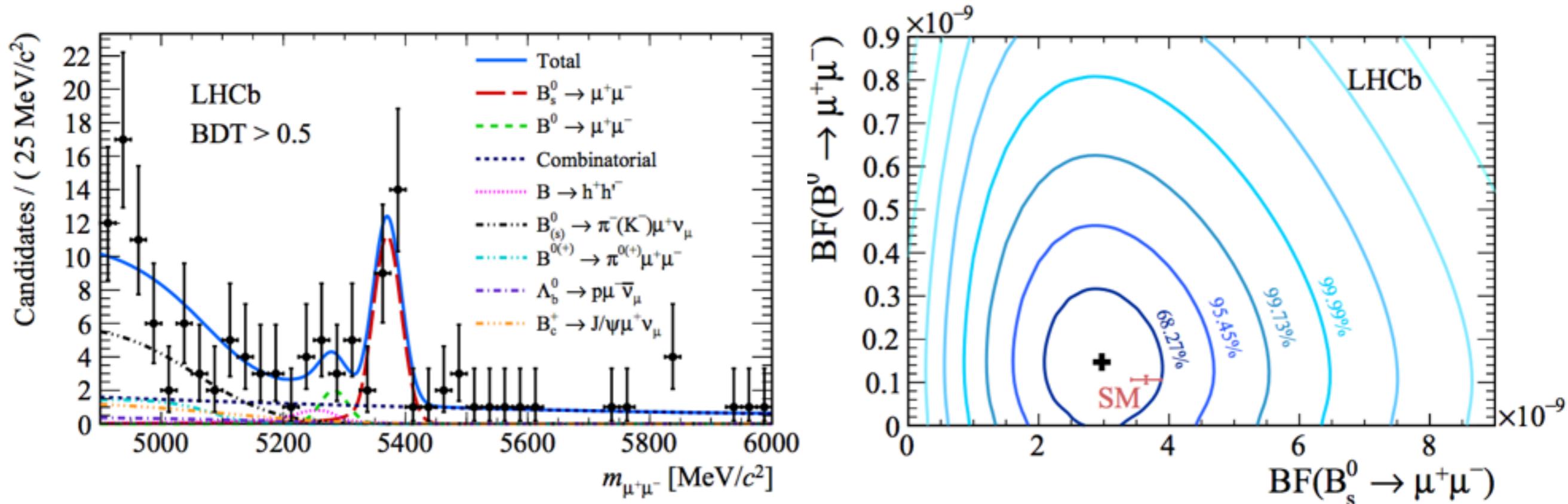
$B_s \rightarrow \mu^+ \mu^-$ excess at 2σ :



$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-) = 0.9_{-0.8}^{+1.1} \times 10^{-9} \ (2\sigma)$$

$$\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-) < 4.2 \times 10^{-10} (95\% CL)$$

In Run II, LHCb observes $B_s \rightarrow \mu^+ \mu^-$ independently with 7.8σ :



- » LHCb Run I data (3fb^{-1}) + 2015 (0.33fb^{-1}) + 2016 (1.4fb^{-1})
- » Several improvements compared to the old analysis:
 - » better di-hadron background rejection (50%)
 - » exclusive background estimates validated on data
 - » new isolation variables improve BDT
- » The most precise results up to date, first single experiment $B_s \rightarrow \mu \mu$ observation.

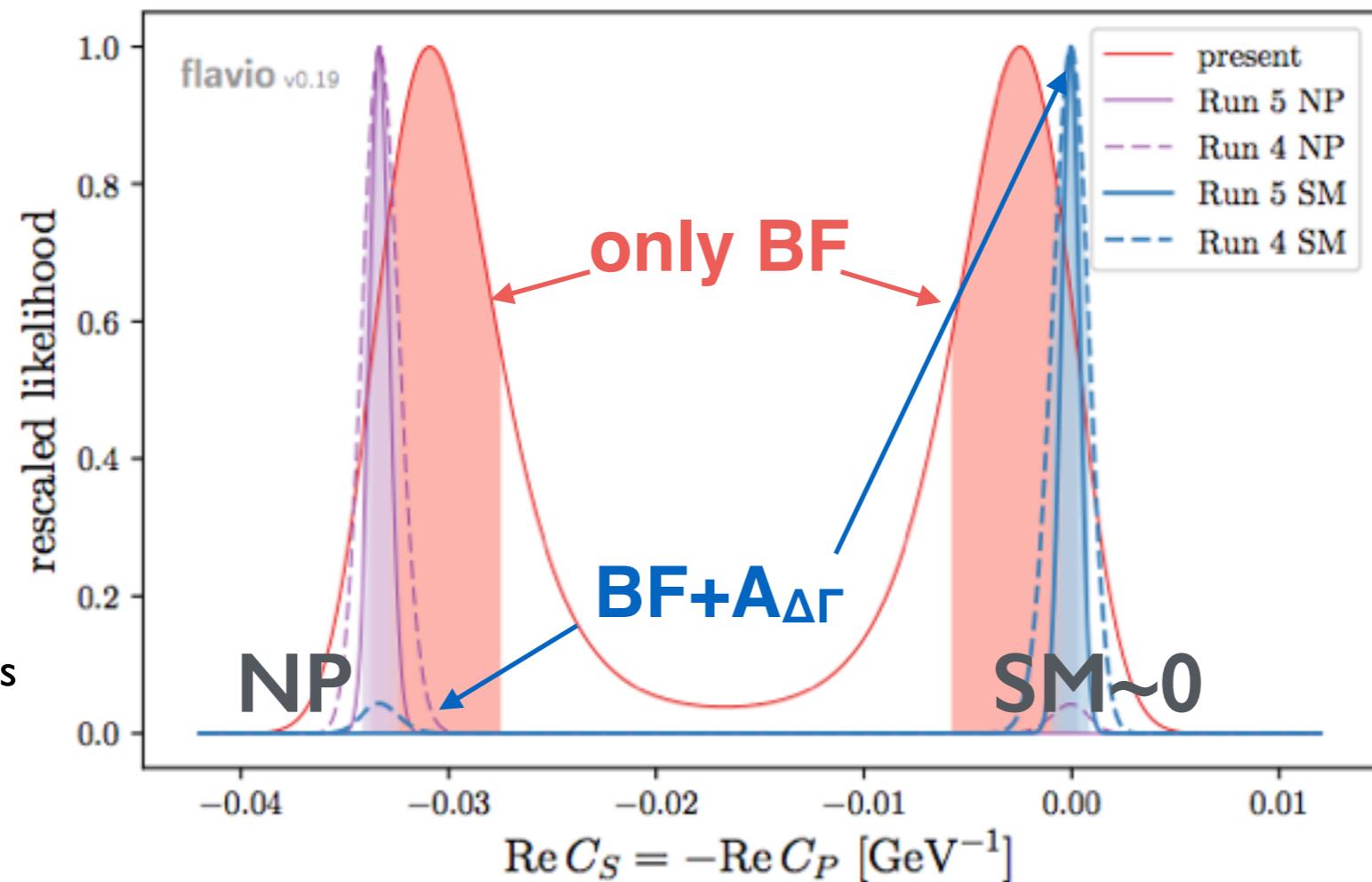
$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9}$$

$$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) < 3.4 \times 10^{-10}$$

$B_s \rightarrow \mu \mu$ (7.8σ) and $B_d \rightarrow \mu \mu$ (1.6σ)

$B_s \rightarrow \mu^+ \mu^-$ is sensitive to new physics even if its branching ratio is not.

for example..



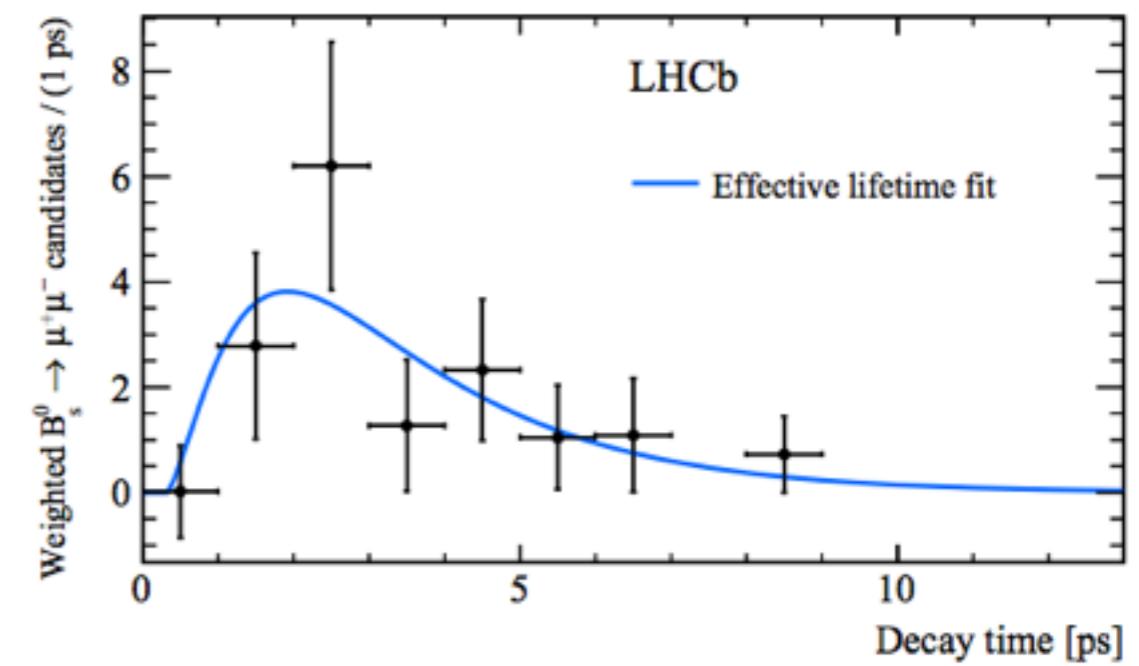
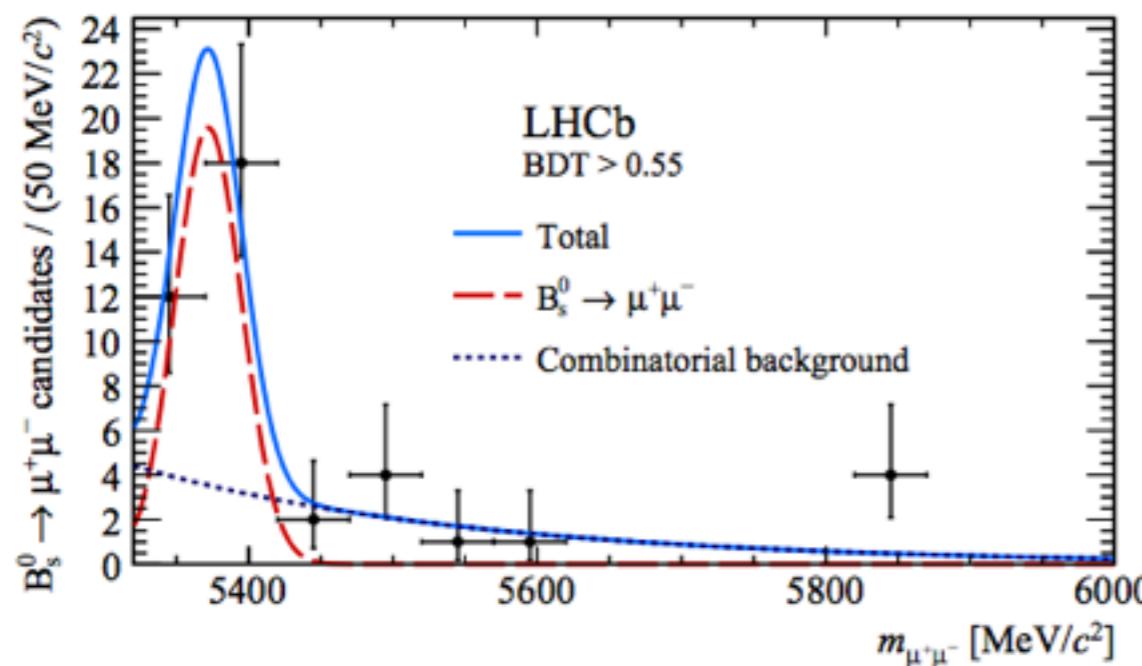
- Measured BF alone leads to ambiguity: e.g. $C_S = -C_P$ equally likely to the SM solution ($C_S = C_P = 0$)
- **Mass-eigenstate-rate asymmetry ($A_{\Delta\Gamma}$) can solve the ambiguity:**

$$A_{\Delta\Gamma} = \frac{\Gamma(B_s^H \rightarrow \mu^+ \mu^-) - \Gamma(B_s^L \rightarrow \mu^+ \mu^-)}{\Gamma(B_s^H \rightarrow \mu^+ \mu^-) + \Gamma(B_s^L \rightarrow \mu^+ \mu^-)} \quad \text{SM: } A_{\Delta\Gamma} = +1$$

LHCb goes beyond the counting: the first effective lifetime measurement

- $A_{\Delta\Gamma}$ can be determined from the effective $B_s \rightarrow \mu^+\mu^-$ lifetime:

[PRL 118, 191801 (2017)]



$$\tau(B_s \rightarrow \mu^+\mu^-) = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$$

(stat) (syst)

- » Compatible with the SM: $\tau(B_s \rightarrow \mu^+\mu^-)^{SM} = (1.615 \pm 0.010) \text{ ps}$
- » First (proof of concept) measurement (no attempt to extract $A_{\Delta\Gamma}$ yet)
- » Result consistent with the $A_{\Delta\Gamma} = +1(-1)$ at 1.0σ (1.4σ)

Goals for both before and after the upgrade(s)

2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	203+
		Run III						Run IV						Run V
LS2						LS3					LS4			
LHCb 40 MHz UPGRADE Phase I		$L = 2 \times 10^{33}$			LHCb Consolidation			$L = 2 \times 10^{33}$ 50 fb^{-1}			LHCb Ph II UPGRADE *	$L = 2 \times 10^{34}$ 300 fb^{-1}		
ATLAS Phase I Upgr	$L = 2 \times 10^{34}$			ATLAS Phase II UPGRADE			HL-LHC $L = 5 \times 10^{34}$			ATLAS	HL-LHC $L = 5 \times 10^{34}$			
CMS Phase I Upgr	300 fb^{-1}			CMS Phase II UPGRADE						CMS	3000 fb^{-1}			
Belle II	5 ab^{-1}		$L = 8 \times 10^{35}$		50 ab^{-1}									

- Improve the $\text{BF}(B_s \rightarrow \mu\mu)$ to constrain NP in $C_{10,S,P}$
- Measure $B^0 \rightarrow \mu\mu$ and test MFV in the BF ratio
 - If very lucky, could see evidence as early as 2019 (expect ~ 20 SM candidates after Run 2, ~ 60 together with Run 3)
- Determine the $A_{\Delta\Gamma}$ to probe the hidden New Physics effects in C_S and C_P
 - First discriminating $A_{\Delta\Gamma}$ measurement expected after Run 3 with $\sim 35\%$ rel. precision ($\sim 20\%, < 10\%$ uncertainty after Run 4,5)

Other $B \rightarrow l^+ l^-$ modes

Other $B \rightarrow l^+ l^-$ modes

- $B_{(s)} \rightarrow e^+ e^-$ heavily helicity suppressed ($\sim 10^{-13}$) in the SM and experimentally difficult
- $B_{(s)} \rightarrow \tau^+ \tau^-$ challenging experimentally, but also affected the least by the helicity suppression:
 - $BF_{SM}(B_s \rightarrow \tau^+ \tau^-) = 7.7(5) \times 10^{-7}$ Bobeth et al
[PRL 96:241802 (2014)]
 - previous limit only for B^0
 $BF(B^0 \rightarrow \tau^+ \tau^-) < 4.1 \times 10^{-3}$ @ 90%CL BaBar Aubert et al
[PRL 96:241802 (2006)]
 - LFU tensions $R(D)$, $R(D^*)$ could imply a $\mathcal{O}(10^3)$ Alonso et al
[1505.05164] boost (Z', leptoquarks, 2HDM,..)

$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

[PRL 118, 251802 (2017)]

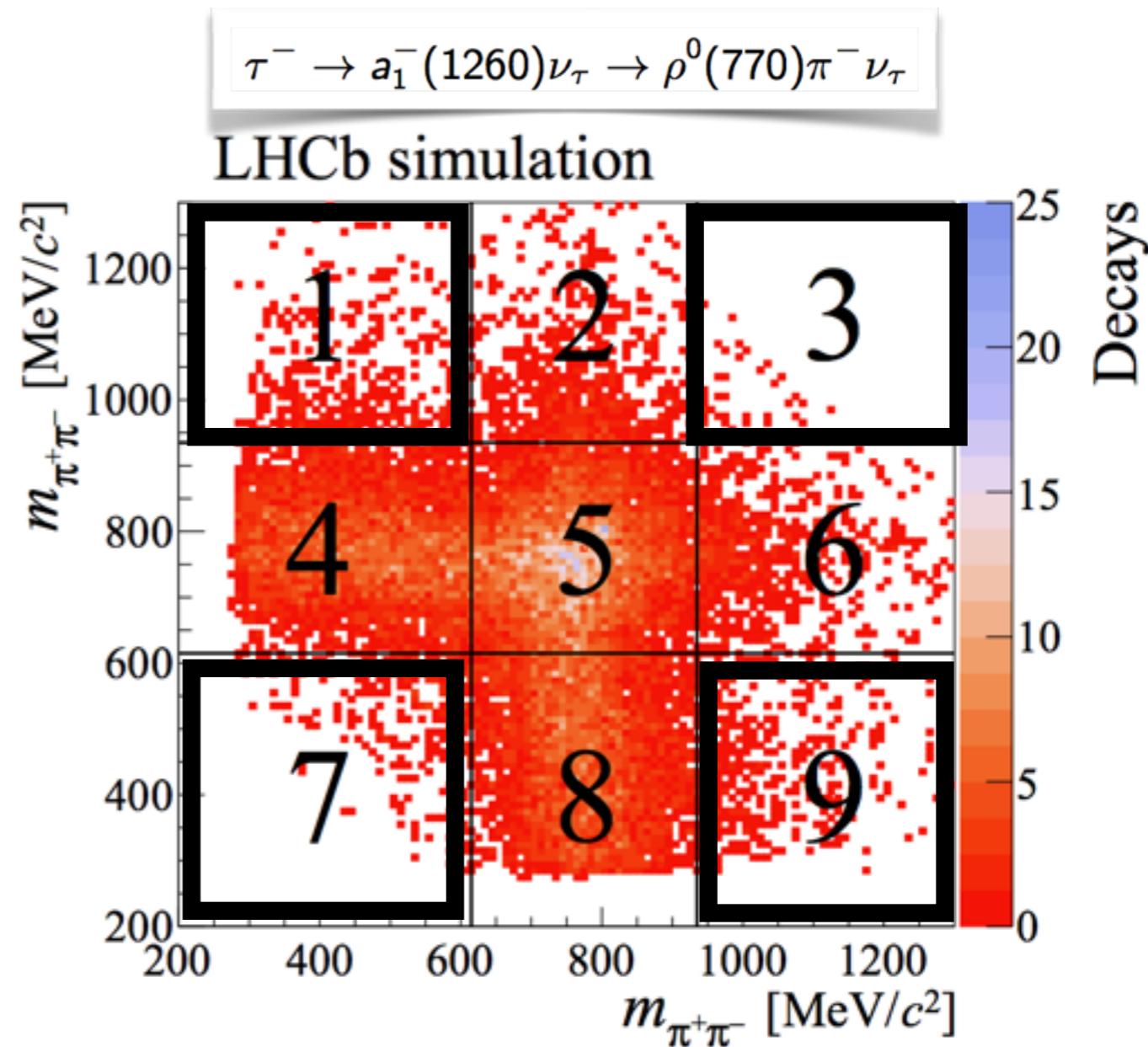
- LHCb analyses Run I data (3fb^{-1}) for the **hadronic τ -modes**: $\text{BF}(\tau \rightarrow \pi \pi \pi \nu) = 9.31(5)\%$
- Two final state neutrinos render B -mass useless for signal/background (and B^0/B_s) separation
- Instead use the intermediate $\rho^0(770) \rightarrow \pi^+ \pi^-$ resonance of the predominant decay chain:

$$\tau^- \rightarrow a_1^-(1260) \nu_\tau \rightarrow \rho^0(770) \pi^- \nu_\tau$$

$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

PRL 118, 251802 (2017)

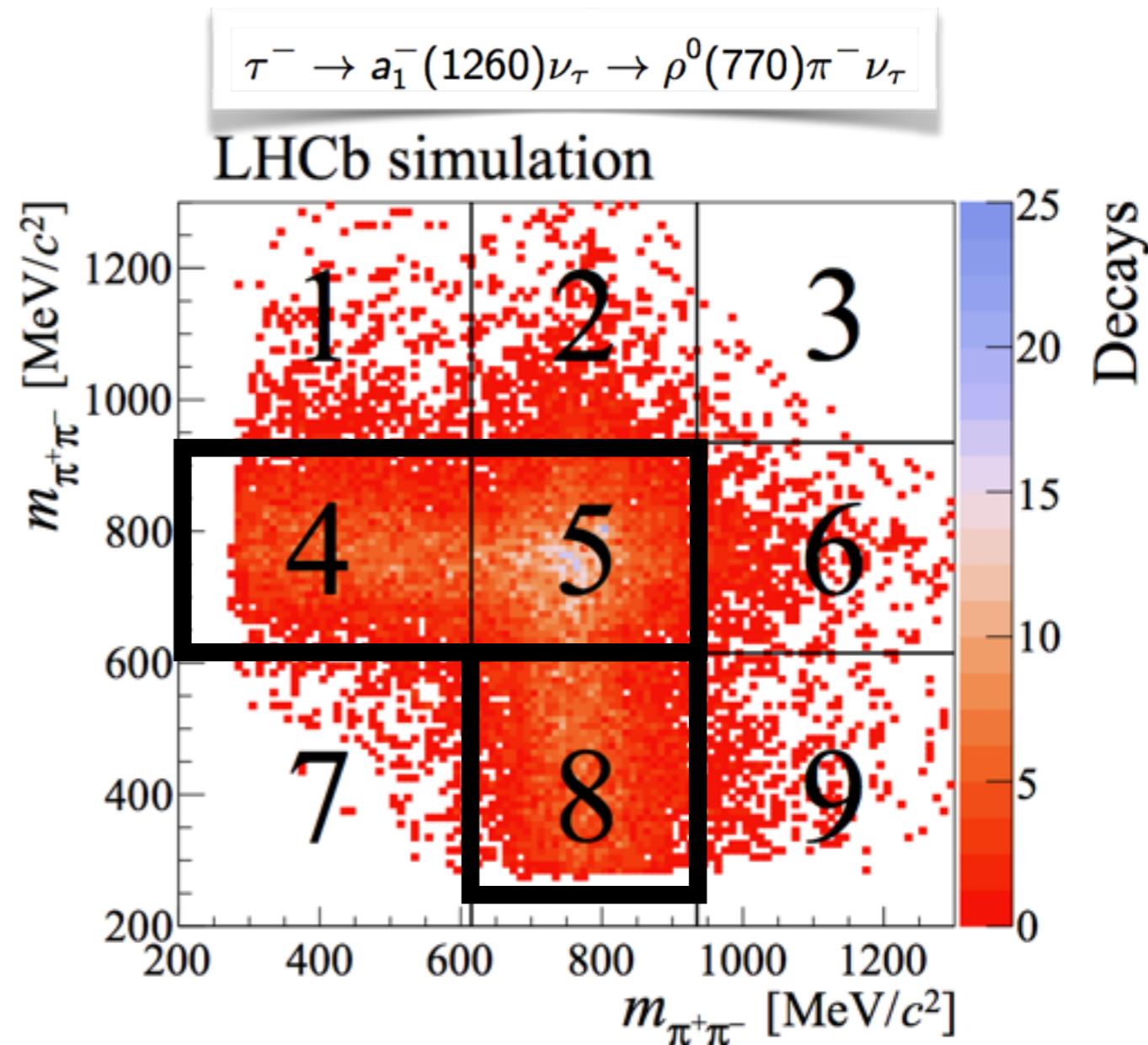
- Optimise the selection, train NN: one- τ in 1-3-7-9 (13% N_{Sig})
- Background model from: one- τ in 4-5-8 and other in one- τ 4-8 (58% N_{Sig})
- Signal region: both τ 's in 5 (16% N_{Sig})



$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

PRL 118, 251802 (2017)

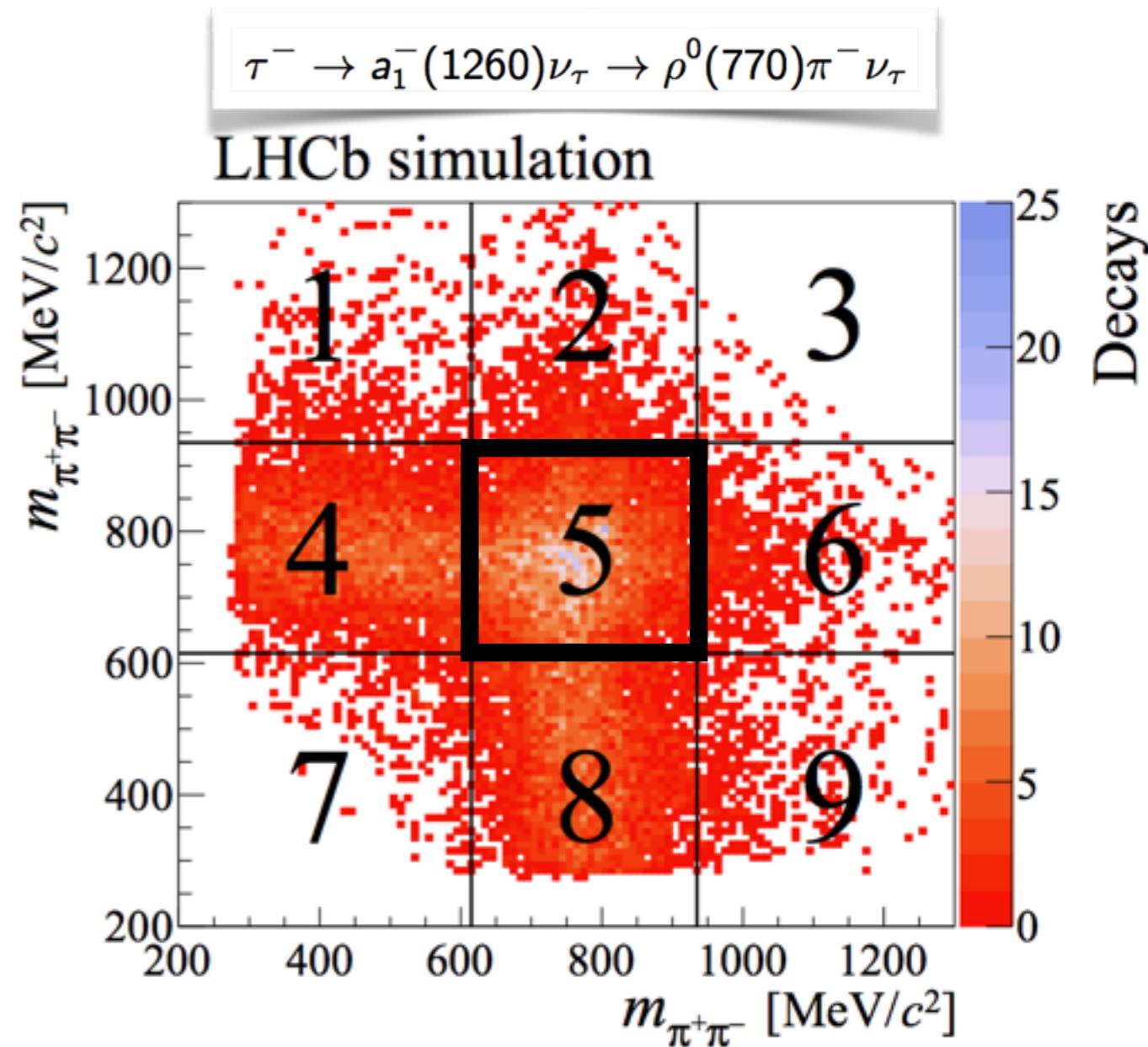
- Optimise the selection, train NN: one- τ in 1-3-7-9 (13% N_{Sig})
- Background model from: one- τ in 4-5-8 and other in one- τ 4-8 (58% N_{Sig})
- Signal region: both τ 's in 5 (16% N_{Sig})



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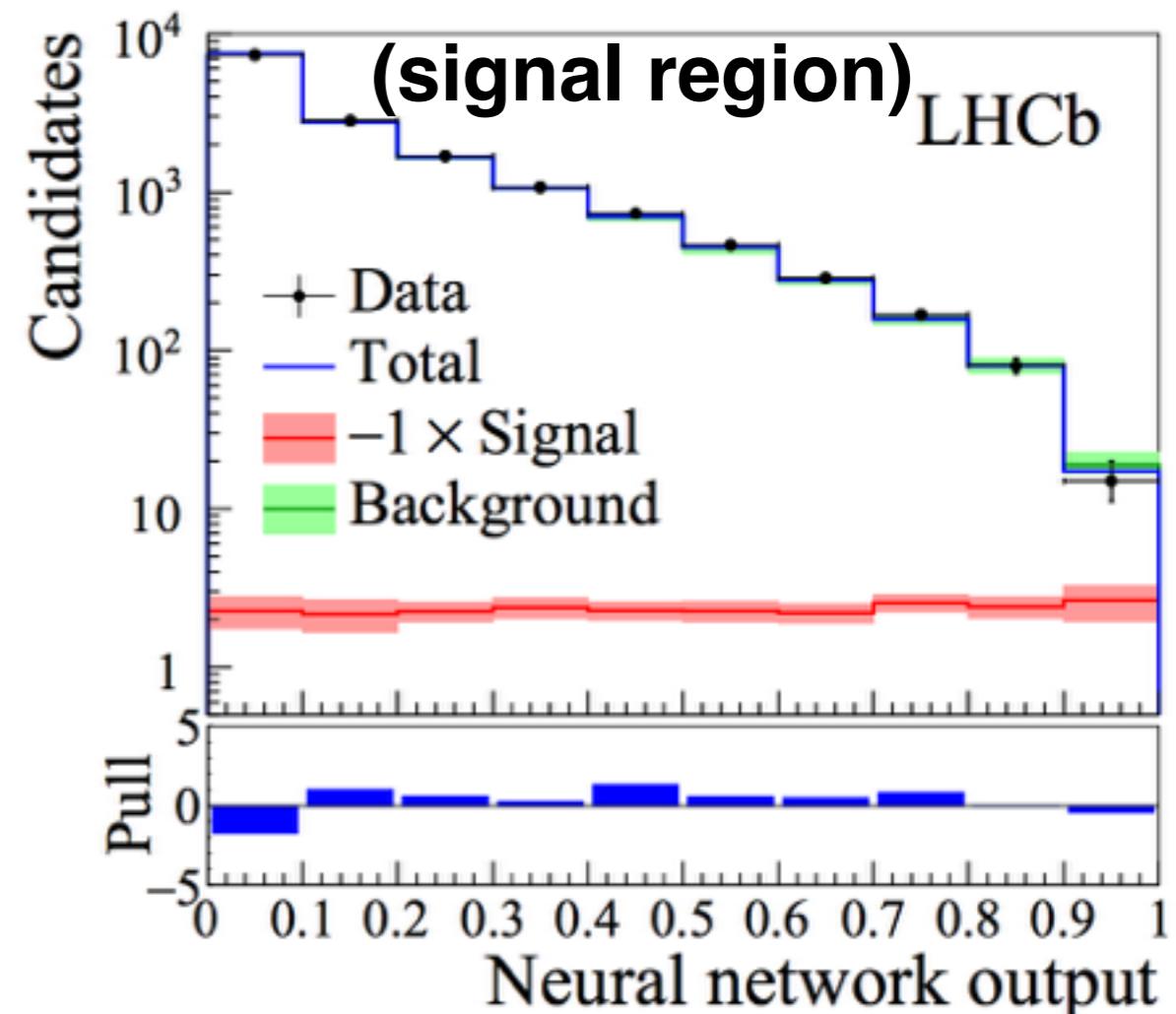
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$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

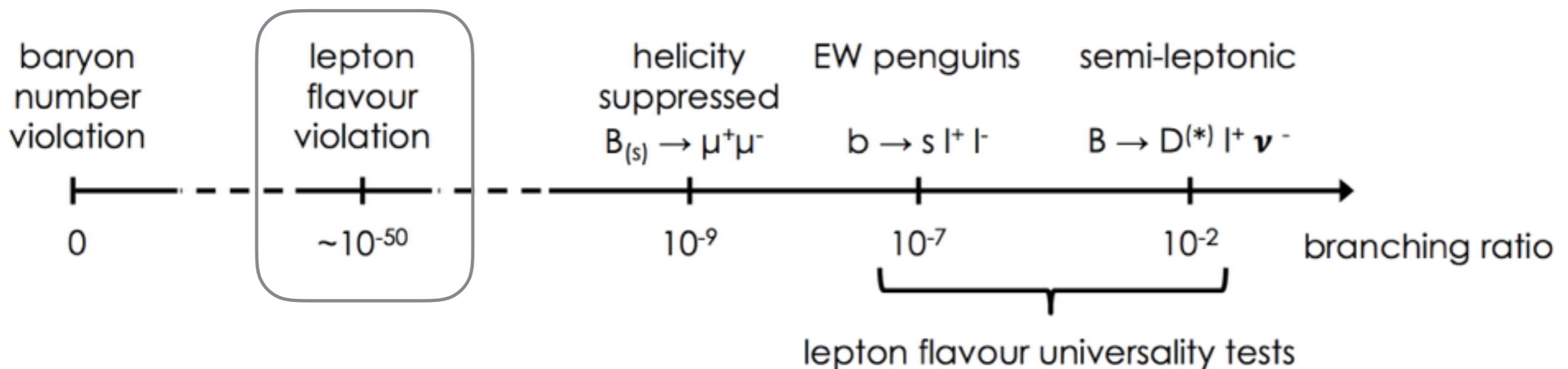
PRL 118, 251802 (2017)

- Separate signal from the background using a neural-net
 - 29 discriminating variables (geom., kin., iso., τ params.)
 - Signal MC distributions calibrated on the normalisation modes
- Normalise the BF to $B_0 \rightarrow D^- D_s^+$ (where $D \rightarrow 3h$):



$$\mathcal{B}(B^0 \rightarrow \tau^+ \tau^-) < 2.1 \times 10^{-3} \text{ @ 95\% CL}$$
$$\mathcal{B}(B_s \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3} \text{ @ 95\% CL}$$

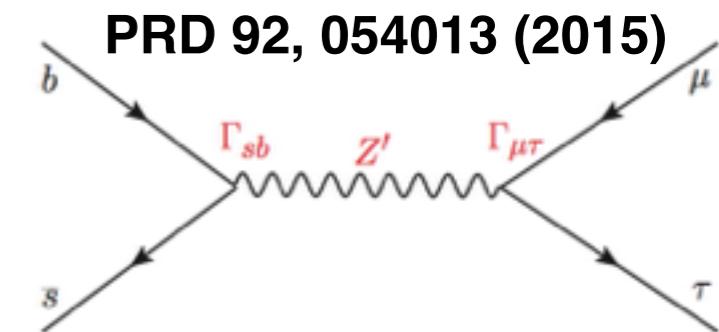
Leptonic B decays have more to offer..



Fully leptonic $B \rightarrow l_x^+ l_y^-$ decays are practically non-existent in the SM

Lepton flavour violation searches in LHCb

- Especially interesting in the light of the recent lepton non-universality hints: $R(K^{(*)})$, $R(D^{(*)})$.
- A large number of modes (SUSY, Z' , leptoquark, Pati-Salam,..) could enhance
 - $BF(B_{(s)} \rightarrow \tau^+ \mu^-) \sim \mathcal{O}(10^{-8})$ in generic Z'
 - $BF(B_{(s)} \rightarrow e^+ \mu^-) \sim \mathcal{O}(10^{-11})$
- Existing limits:
 - $BF(B^0 \rightarrow \tau^+ \mu^-) < 2.2 \times 10^{-5}$ @90% BaBar
 - $BF(B^0 \rightarrow e^+ \mu^-) < 3.7 \times 10^{-9}$ @95% LHCb 1fb^{-1}
 - $BF(B_s \rightarrow e^+ \mu^-) < 1.4 \times 10^{-8}$ @95% LHCb 1fb^{-1}



PRD 77, 091104 (2008)
PRL 111 (2013) 141801

New!

$B_{(s)} \rightarrow e^+ \mu^-$ search in Run I data

arXiv:1710.04111

submitted to JHEP

- Analyse full Run I sample (3fb^{-1}) with improved selection (esp. BDT)
- Similar to $B_{(s)} \rightarrow \mu^+ \mu^-$, yet more challenging
 - Bremsstrahlung correction to the e-momentum
- Selected $e^+ \mu^-$ candidates in $m_{e\mu} \in [4.9, 5.85]\text{GeV}/c^2$
 - contaminated by combinatorial background
 - sample split in two depending on the nr. of recovered photons: a) $e+0\gamma$ and b) $e+n\gamma$

New!

$B_{(s)} \rightarrow e^+ \mu^-$ search in Run I data

arXiv:1710.04111

submitted to JHEP

- The combinatorial is suppressed using a multivariate classifier (BDT):
 - trained on $B_{(s)} \rightarrow e^+ \mu^-$ MC and same sign $e^{+/-} \mu^{+/-}$ data
 - signal response calibrated on $B^0 \rightarrow K^+ \pi^-$ data (accounting for Bremsstrahlung)
- Simultaneous fit on 2x7 BDT bins. Model:
 - Signal+mis-identified bkg. ($B \rightarrow hh, B \rightarrow hlv$) +combinatorial bkg.
 - individual for both bremsstrahlung categories

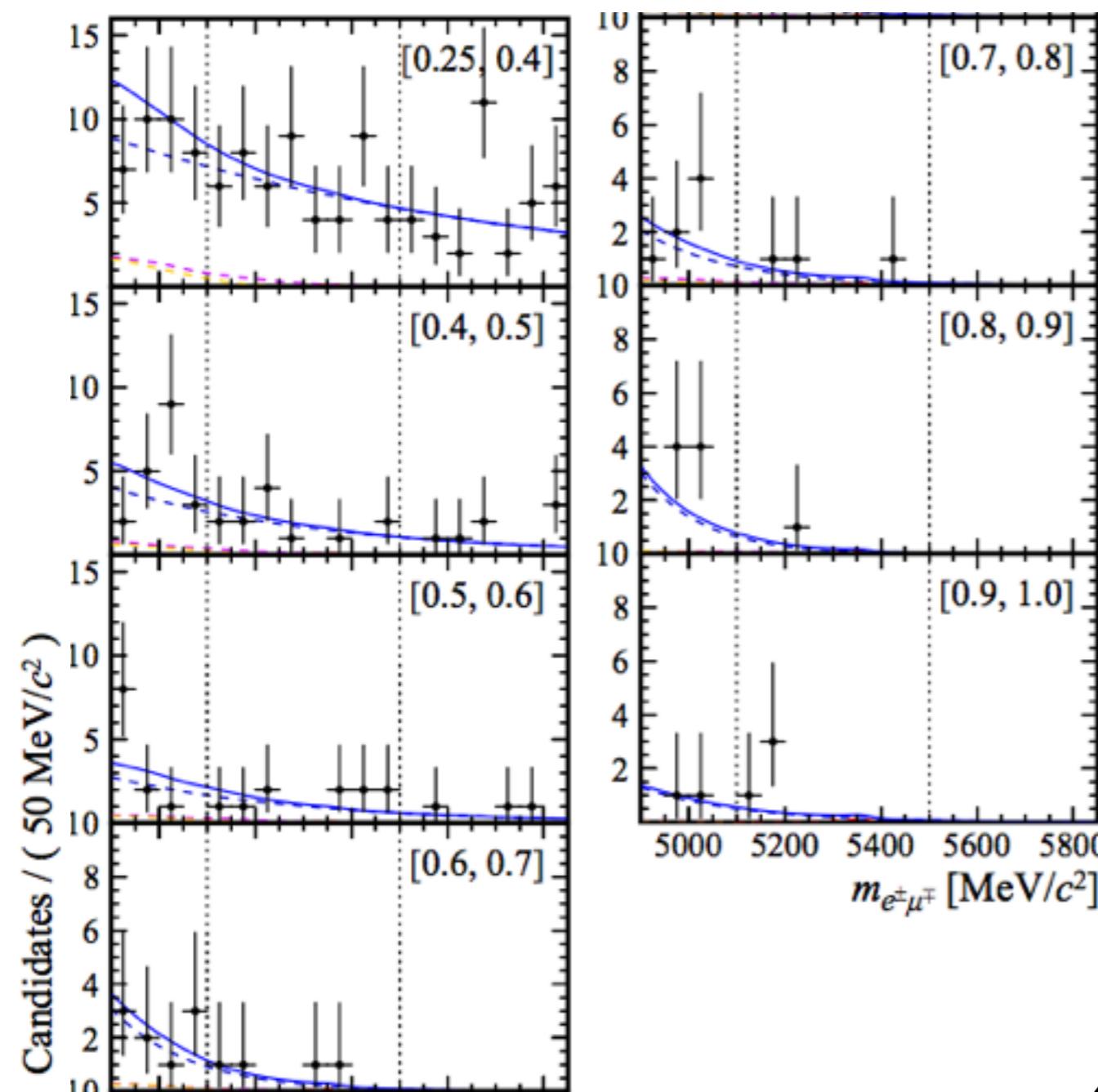
New!

No $B_{(s)} \rightarrow e^+ \mu^-$ signal in Run I data

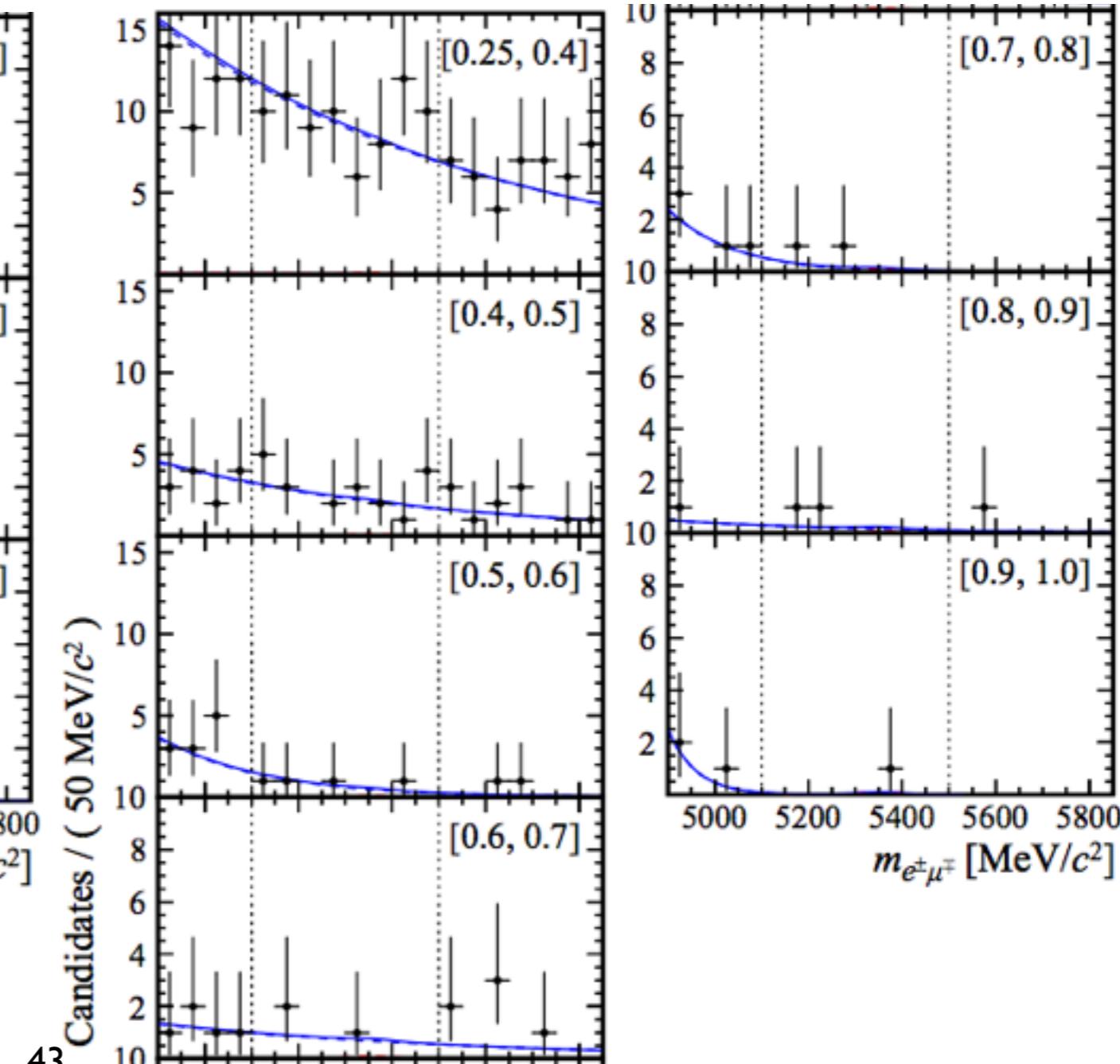
arXiv:1710.04111

submitted to JHEP

- a) No Bremsstrahlung



- b) Bremsstrahlung



New!

$B_{(s)} \rightarrow e^+ \mu^-$ search in Run I data

arXiv:1710.04111
submitted to JHEP

- LHCb sets the most stringent limits up to date:

channel	expected	observed
$\mathcal{B}(B_s^0 \rightarrow e^\pm \mu^\mp)$	$3.9 (5.0) \times 10^{-9}$	$5.4 (6.3) \times 10^{-9}$
$\mathcal{B}(B^0 \rightarrow e^\pm \mu^\mp)$	$0.9 (1.2) \times 10^{-9}$	$1.0 (1.3) \times 10^{-9}$

- The limit on $B_s \rightarrow e^+ \mu^-$ is set assuming only B_{Heavy} decays (as in SM).
- B_{Light} : $\text{BF}(B_s \rightarrow e^+ \mu^-) < 6.0(7.2) \times 10^{-9}$ @ 90(95)% CL

Rare leptonic B-decays at the end of 2017

- B-decays have provided us with some of the most interesting puzzles in particle physics:
- global W . coefficient analysis show a coherent picture
- anomalies either in **vector (C_9)** OR in both **vector and axial-vector currents (C_9, C_{10})**

- Fully leptonic B-decays can constrain the axial-vector contributions (C_{10})
 - SM like $BF(B_s \rightarrow \mu^+ \mu^-)$ excludes very large contributions to $C_{10,S,P}$, but not yet precise enough to distinguish btw. $C^{NP}_{10} + C^{NP}_9$ and C^{NP}_9 alone scenarios.
 - Only beginning to tap into $B_{(s)} \rightarrow \mu^+ \mu^-$
 - Effective $B_s \rightarrow \mu^+ \mu^-$ lifetime will help to expose/exclude $C_{S,P}$ contributions invisible to the BF alone (first LHCb results on Run 1+Run 2 are out, $A_{\Delta\Gamma}$ accessible in Run 3)
 - $B_d \rightarrow \mu^+ \mu^-$ could enter the game soon (2019? but most likely in Run 3)

- In the light of the recent LFU tensions
other leptonic B modes are as important:
 - LHCb sets best/first $B_{(s)} \rightarrow \tau^+ \tau^-$ limits on Run I data at $\mathcal{O}(10^{-3})$
 - LHCb sets best $B_{(s)} \rightarrow e^+ \mu^-$ limits on Run I data at $\mathcal{O}(10^{-9})$

Back-up

Historical success of the ‘effective’ approach

- The ‘effective’ model independent approach has historically played a crucial role in understanding the underlying theory from both direct and indirect measurements:
 - 1933: First model for the weak decays. Similar coupling in the beta decay and muon decay suggested an underlying structure (V-A)
 - 1960’s: Motivated charm prediction to make GIM work and explain missing FCNC.
 - 1970’s: In predicting lower bounds on Z and W masses from muon lifetime (motivate SPS)
 - 2010’s: **Lepton Flavour Universality Violation? Z' ? Leptoquarks?**

$B \rightarrow \mu\mu$ future in numbers

Unofficial crude back-of-the-envelope Standard Model yield estimates based on the Run I performance:

Assuming SM and Run1 performance (raw est.)	Run1	+Run 2 (2019)	+Run3 (2024)	+Run4 (2030)	+Run 5 (assume 30% have good S/B)
Lumi (fb⁻¹)	3	5,3	15	15	250
N($B_s \rightarrow \mu^+\mu^-$)	35	155	0.5k	0.9k	2.7k
N($B_d \rightarrow \mu^+\mu^-$)	4	20	60	0.1k	0.3k
$\sigma_{\text{Relative}}(\text{BF}(B_s \rightarrow \mu^+\mu^-))$	40%	20%	15%	13%	~10%
$\sigma_{\text{Relative}}(A_{\Delta\Gamma})$	-	115%	35%	20%	<10%

Rare di-lepton modes

$$B_{(s)} \rightarrow \mu^+ \mu^-$$

► Precise Standard Model predictions for individual modes:

[[Phys. Rev. Lett. 112, 101801 \(2014\)](#)]

with updated **top mass**

[<http://arxiv.org/abs/1403.4427>]

$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-)^{ < CP>} = 3.66 \pm 0.23 \times 10^{-9} \text{ (6.4% unc.)}$$

$$\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-)^{ < CP>} = 1.06 \pm 0.09 \times 10^{-10} \text{ (8.5% unc.)}$$

$B_s^0 \rightarrow \mu^+ \mu^-$	f_{B_s}	CKM	τ_H^s	M_t	α_s	other param.	non-param.	\sum
	4.0%	4.3%	1.3%	1.6%	0.1%	< 0.1%	1.5%	6.4%
$B^0 \rightarrow \mu^+ \mu^-$	f_{B_d}	CKM	τ_H^s	M_t	α_s	other param.	non-param.	\sum
	4.5%	6.9%	0.5%	1.6%	0.1%	< 0.1%	1.5%	8.5%

► Even more precise Standard Model predictions for the ratio (MVF test):

$$\mathcal{R} = \frac{\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)}{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)} = \frac{\tau_{B_d}}{1/\Gamma_H^s} \left(\frac{f_{B_d}}{f_{B_s}} \right)^2 \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{M_{B_d} \sqrt{1 - \frac{4m_\mu^2}{M_{B_d}^2}}}{M_{B_s} \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}}} = 0.0295^{+0.0028(8.7\%)}_{-0.0025(7.7\%)}$$

Error budget of \mathcal{R} :

- 8% from V_{td}/V_{ts}
- 3.7% from f_{B_d}/f_{B_s}
- 1.4% from B_s lifetime

- Top mass, Wilson coefficients, and V_{tb} cancel in theory predictions
- Experimental side: no need for the normalisation

Coefficients \mathbf{C}_{10} , \mathbf{C}_S and \mathbf{C}_P in fully leptonic B decays

$B_{(s)} \rightarrow \mu^+ \mu^-$

- Only \mathbf{C}_{10} contributes in the Standard Model
- NP sensitivity in \mathbf{C}_S and \mathbf{C}_P is larger than in \mathbf{C}_{10} (no helicity suppression)
($K^* \mu \mu$ sensitivity to \mathbf{C}_S is lower than initially expected)

$$\frac{\text{BR}(B_q \rightarrow \ell^+ \ell^-)}{\text{BR}(B_q \rightarrow \ell^+ \ell^-)_{\text{SM}}} = \frac{|S|^2 \left(1 - \frac{4m_\ell^2}{m_{B_q}^2}\right) + |P|^2}{|C_{10}^{\text{SM}}|^2} \quad \begin{array}{l} \text{SM: } S=0 \\ \text{SM: } P=1 \end{array}$$

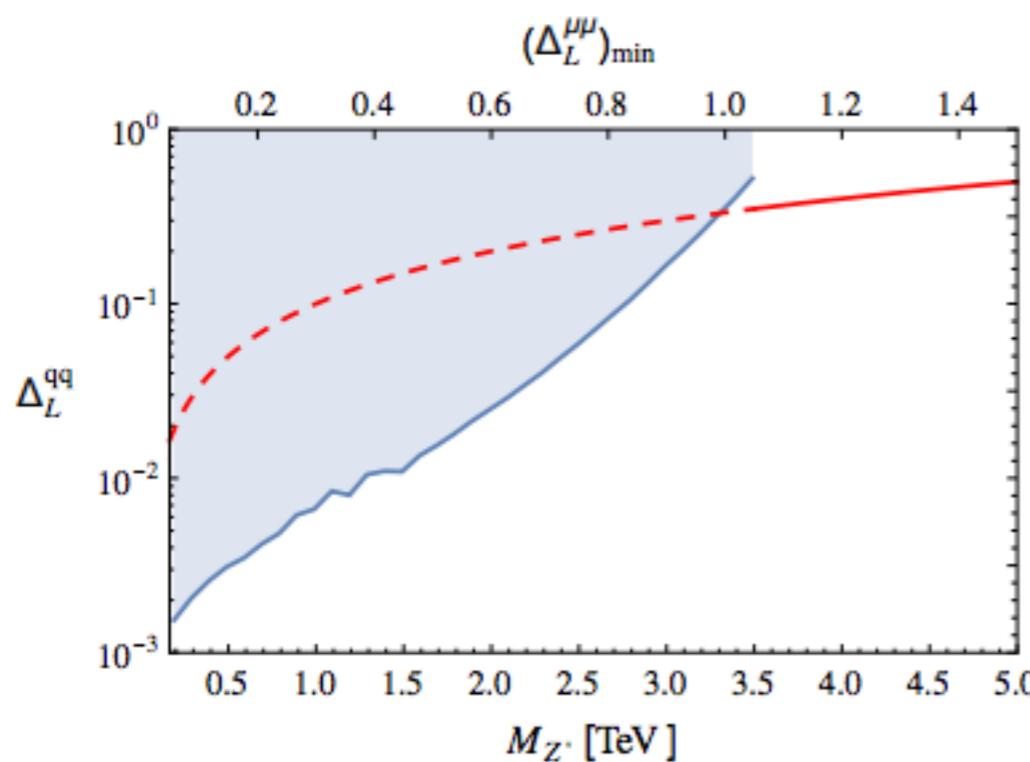
$$S = \frac{m_{B_q}^2}{2m_\ell} [(C_S)_q^\ell - (C'_S)_q^\ell] \quad P = [(C_{10})_q^\ell - (C'_{10})_q^\ell] + \frac{m_{B_q}^2}{2m_\ell} [(C_P)_q^\ell - (C'_P)_q^\ell]$$

- Very precise Standard Model predictions (limited by CKM and B decay constant):

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.59 \pm 0.18) \times 10^{-9}$$

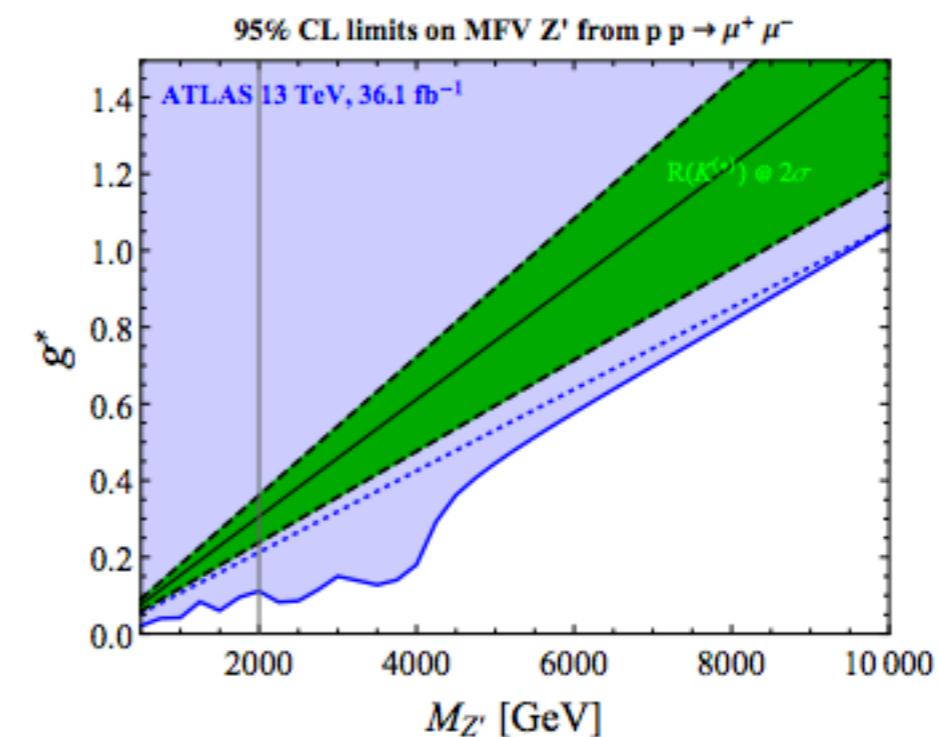
Rel. Unc. from 6.4% -> 5%
Phys. Rev. Lett. 112, 101801 (2014)
updated in arXiv:1702.05498

Dimuon constraints: two examples



Altmannshofer and Straub 1411.3161

- ▶ For $M_{Z'} \lesssim 3.5$ TeV, coupling to light quarks must be suppressed



Greljo and Marzocca 1704.09015

- ▶ MFV-like coupling to quarks is already excluded

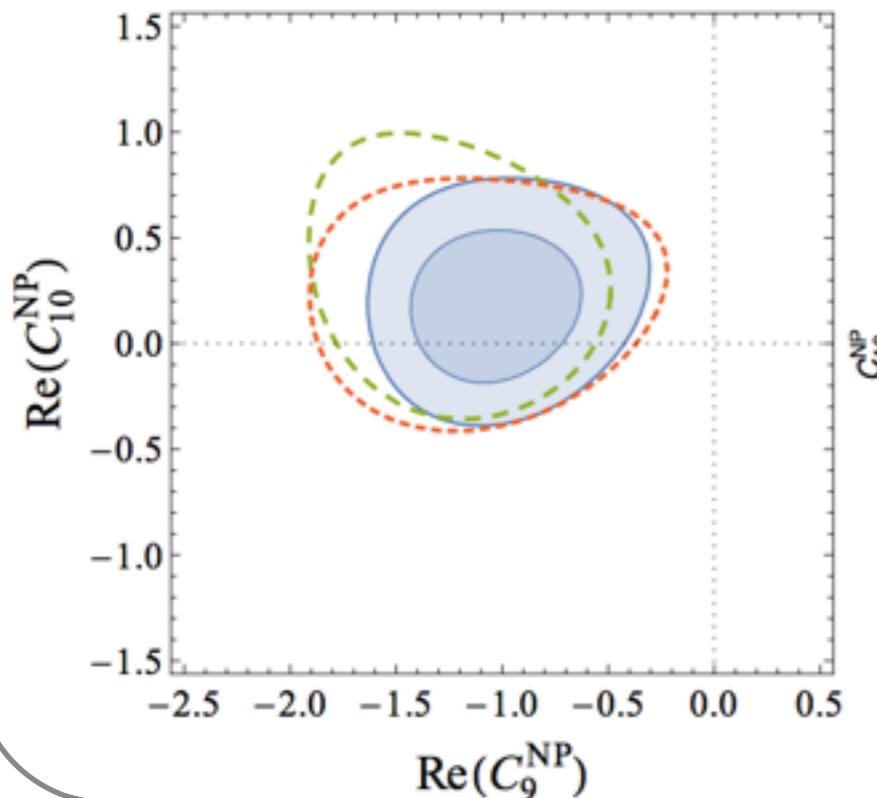
Wilson coefficients are measured in **global $b \rightarrow s l^+ l^- (\gamma)$ analysis**

- No evidence for right-handed FCNC ($C'_i = 0$) and $C_{(7,9,10)}$ signs $[-,+,-]$ agree with the predictions (pre LHC discussion)
- There are tensions w.r.t SM (up to 4σ)
- Tensions are **driven** by **$B^0 \rightarrow K^* \mu^+ \mu^-$ angular observables** and by several **exclusive $b \rightarrow s l^+ l^-$ branching fraction** measurements; supported by $R(K)$.
- **Tensions are relieved** by (NP effects?):

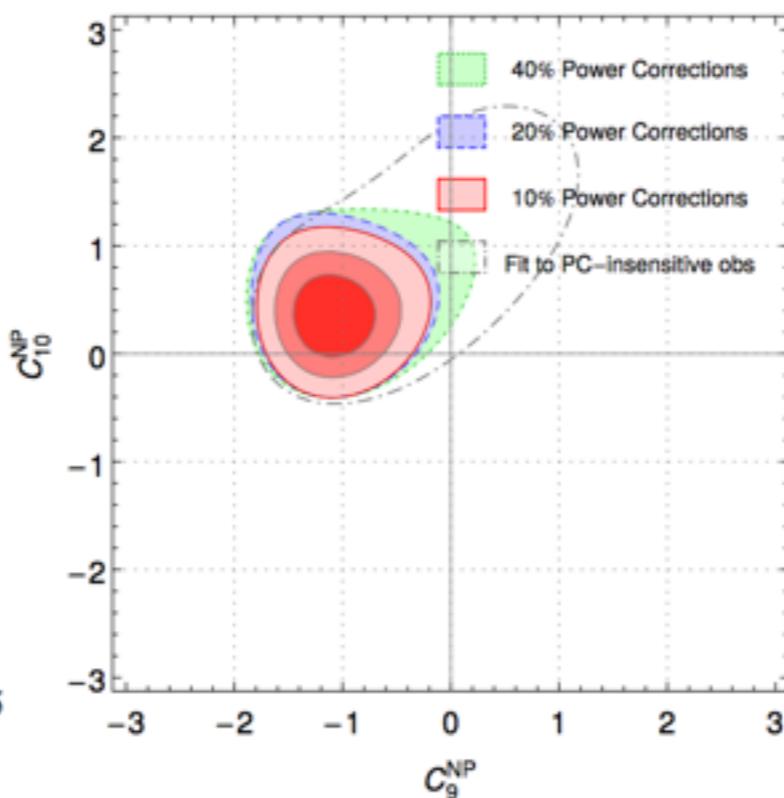
$$[(C_9)_s^\mu]^{NP} \approx -1.1 \quad \text{or} \quad [(C_9)_s^\mu]^{NP} = -[(C_{10})_s^\mu]^{NP} \approx -0.5$$

Altmannshofer, Straub

[Eur.Phys.J.C75(8)(2015)382]

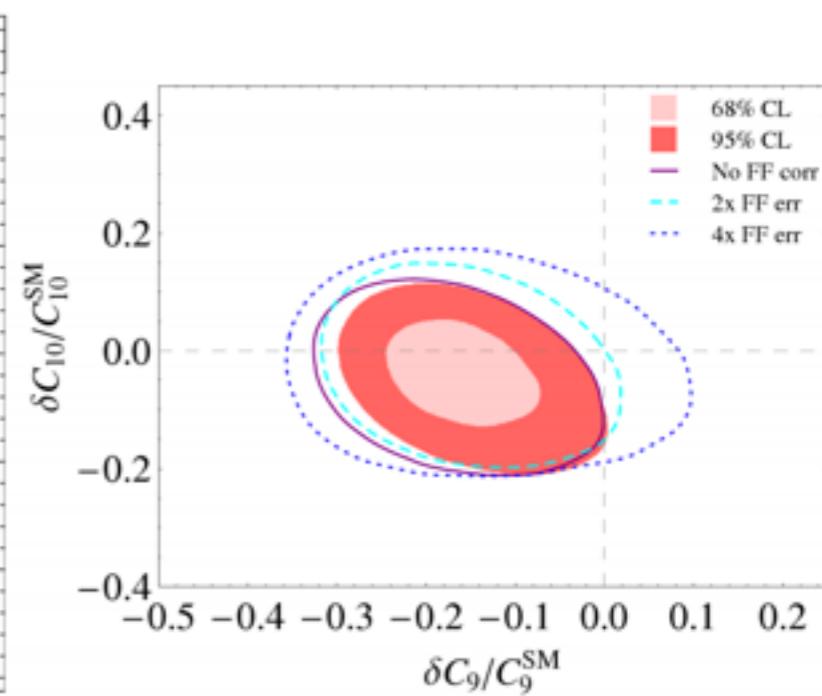


Descotes-Genon, Hofer, Matias,
Virto [JHEP 06 (2016) 092]



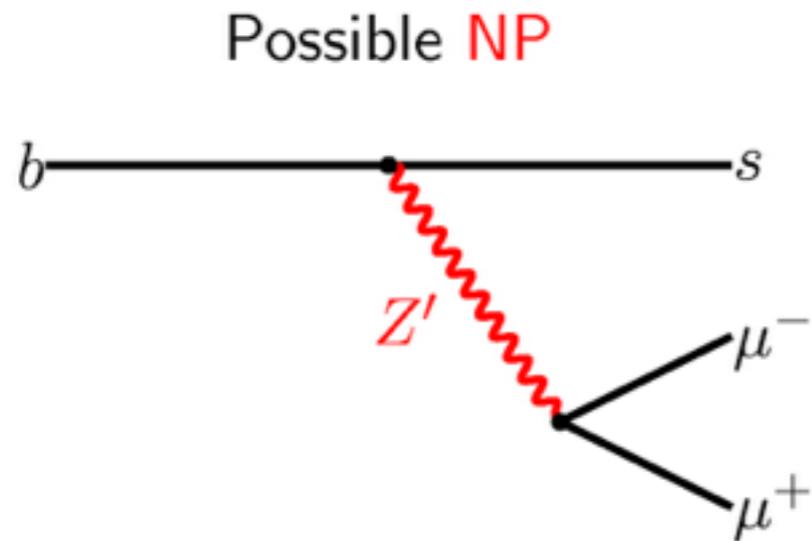
Hurth, Mahmoudi, Neshatpour

[arXiv:1603.00865]



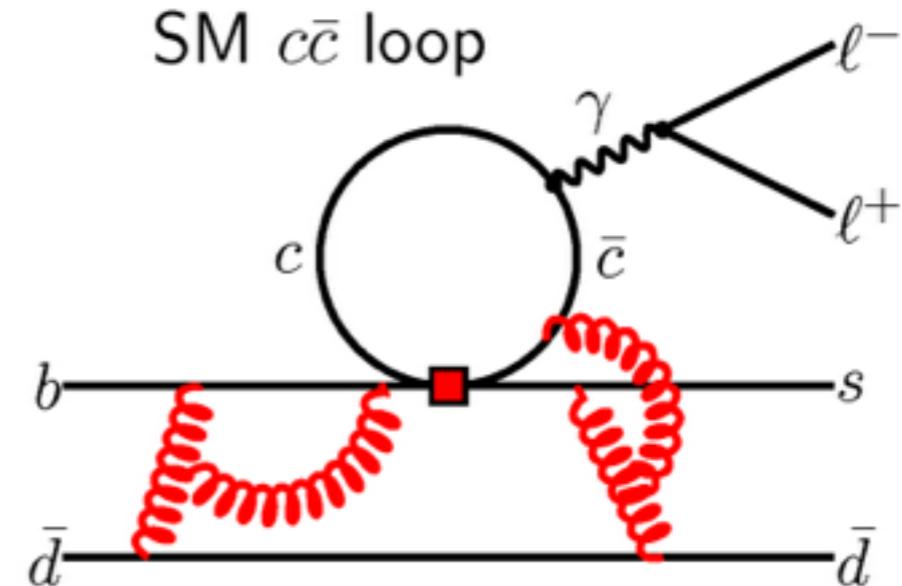
Understanding **the origin** of the tensions

Z', leptoquarks,...



or

Hadronic SM effects



$$C_9 + C_9^{NP}$$

$$C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{res}(q^2)$$

Large long-distance charm resonance effects far from the resonances on the q^2 plane.

NEW!

► Measure the resonance effects in C_9 in an inclusive analysis:

$$B^+ \rightarrow K^+ \mu^+ \mu^- + B^+ \rightarrow K^+ X_{c\bar{c}} (\rightarrow \mu^+ \mu^-)$$

$$B^+ \rightarrow K^+ \mu^+ \mu^-$$

- The differential decay rate depends on the Wilson coefficients:

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 \alpha^2 |V_{tb} V_{ts}^*|^2}{128\pi^5} |\mathbf{k}| \beta \left\{ \frac{2}{3} |\mathbf{k}|^2 \beta^2 \left| \mathcal{C}_{10} f_+(q^2) \right|^2 + \frac{4m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} \left| \mathcal{C}_{10} f_0(q^2) \right|^2 \right. \\ \left. + |\mathbf{k}|^2 \left[1 - \frac{1}{3} \beta^2 \right] \left| \mathcal{C}_9 f_+(q^2) + 2\mathcal{C}_7 \frac{m_\mu + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\},$$

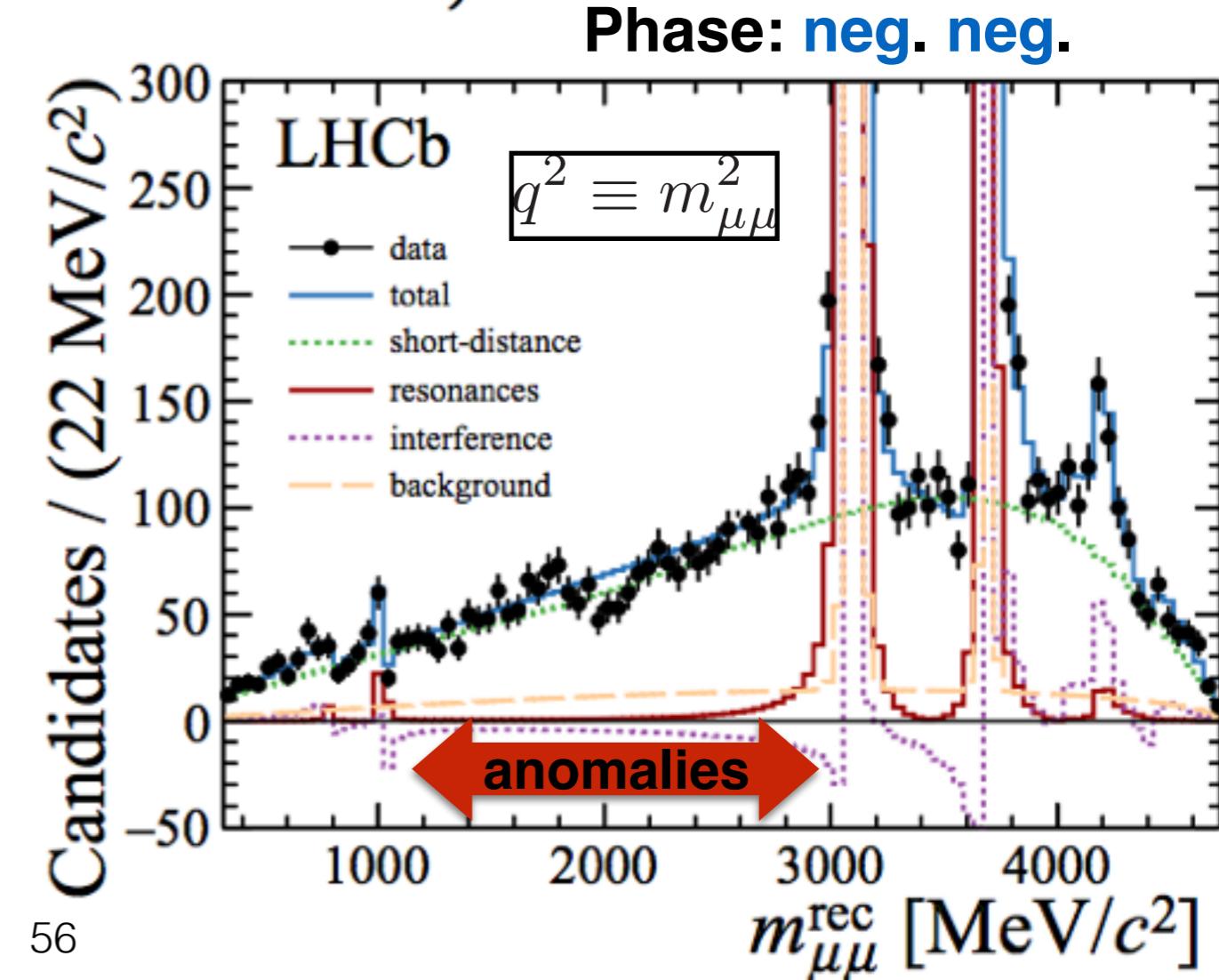
fix C_7 to the SM value (small)

- Parametrise resonance effects:

$$C_9^{\text{eff}} = C_9 + \sum_j \eta_j e^{i\delta_j} \underline{A_j^{\text{res}}(q^2)}$$

relative Breit-Wigner/
phase to C_9 Flatté $\Phi(3770)$

Resonance	$\psi(2S)$
$\rho(770)$	$\psi(3770)$
$\omega(782)$	$\psi(4040)$
$\phi(1020)$	$\psi(4160)$
J/ψ	$\psi(4415)$



Measuring **resonance effects** in C_9

[arXiv:1612.06764]
submitted to EPJC

NEW!

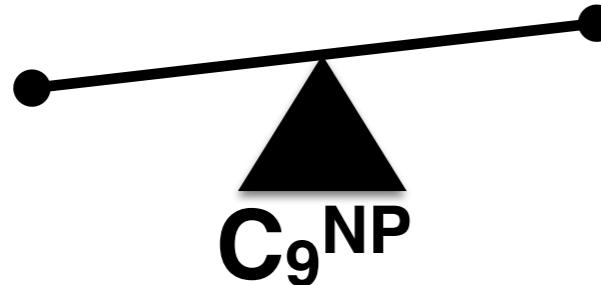
$$B^+ \rightarrow K^+ \mu^+ \mu^-$$

- The **short-distance branching fraction** agrees with the previous (exclusive) result:

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.29 \pm 0.07 \text{ (stat)} \pm 0.21 \text{ (syst)}) \times 10^{-7} \text{ old}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.37 \pm 0.15 \text{ (stat)} \pm 0.23 \text{ (syst)}) \times 10^{-7} \text{ new}$$

- 1D (C_9, C_{10} =SM) fit:
 $C_9 < \text{SM}$ (as the global fits)

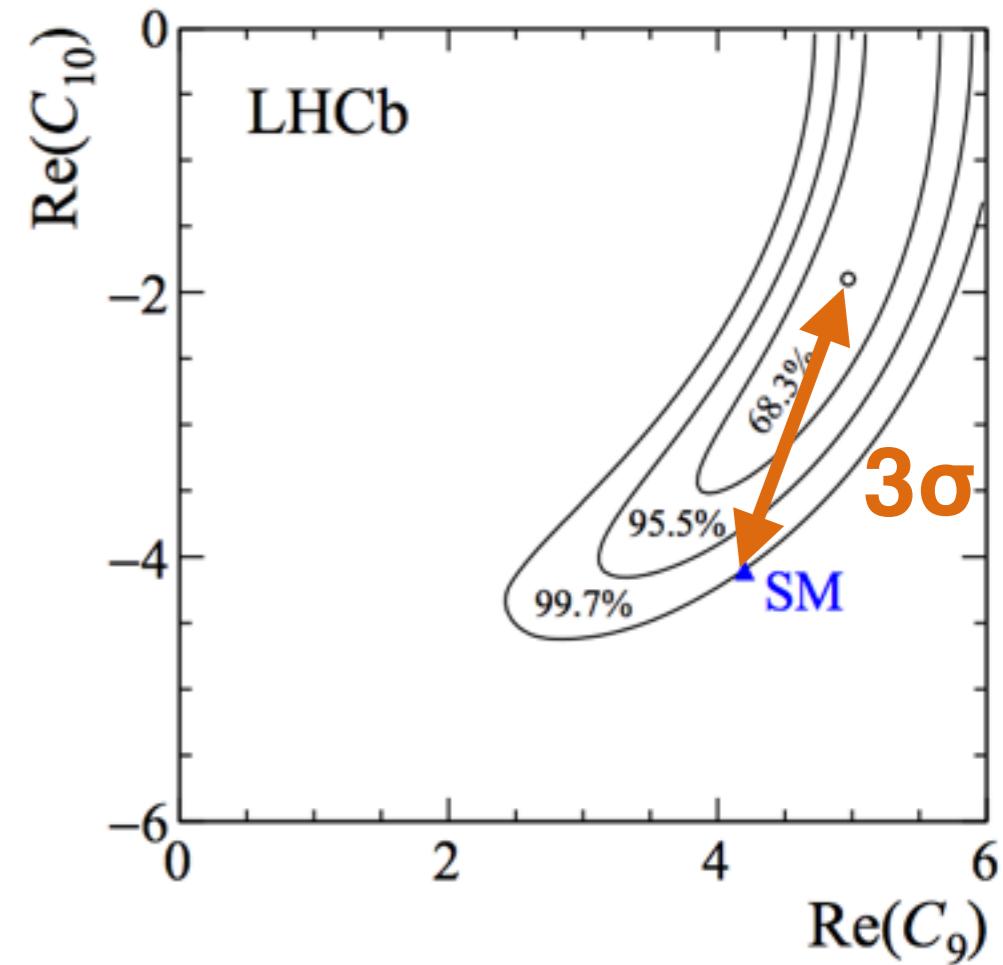
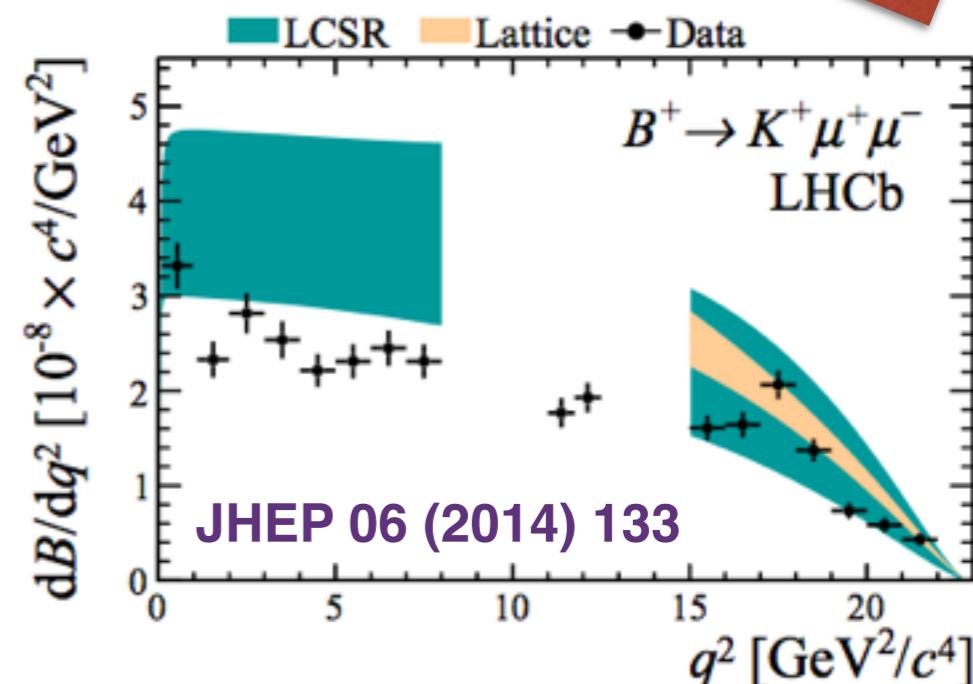


- 2D (C_9, C_{10}) fit:
 $C_9 > \text{SM}$ $C_{10} < \text{SM}$

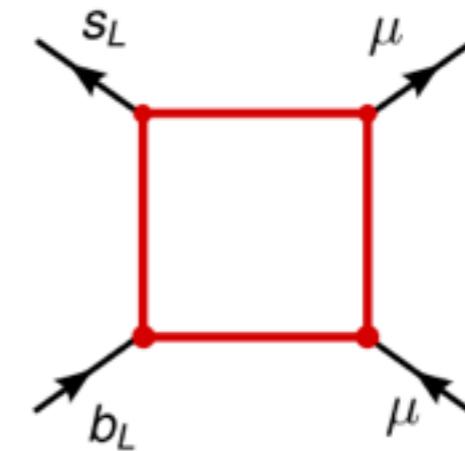
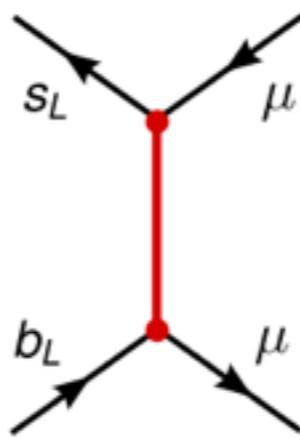
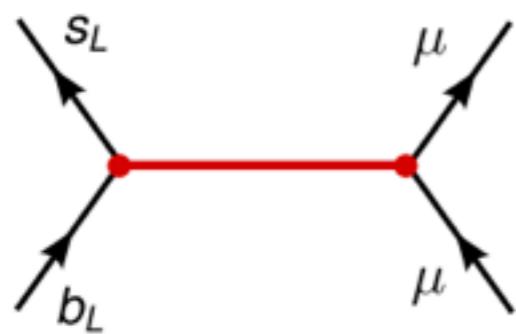
(as [JHEP06(2015)115])

- The main conclusion: contributions from J/ψ and $\psi(2S)$ are contained around their (narrow) resonances.

- Inclusive $B^0 \rightarrow K^* \mu^+ \mu^-$ analysis will follow



Possible New Physics



- ▶ Z'
- ▶ $SU(2)_L$ singlet or triplet

- ▶ Leptoquark
- ▶ Spin 0 or 1

- ▶ New scalars/vectors, also leptoquarks possible

Talk by I. Nisandžić, B. Grinaić