

Rare leptonic B decays

Siim Tolk

on behalf of the LHCb collaboration



UNIVERSITY OF
CAMBRIDGE



SUSY
Mumbai 2017

A broad and versatile physics programme

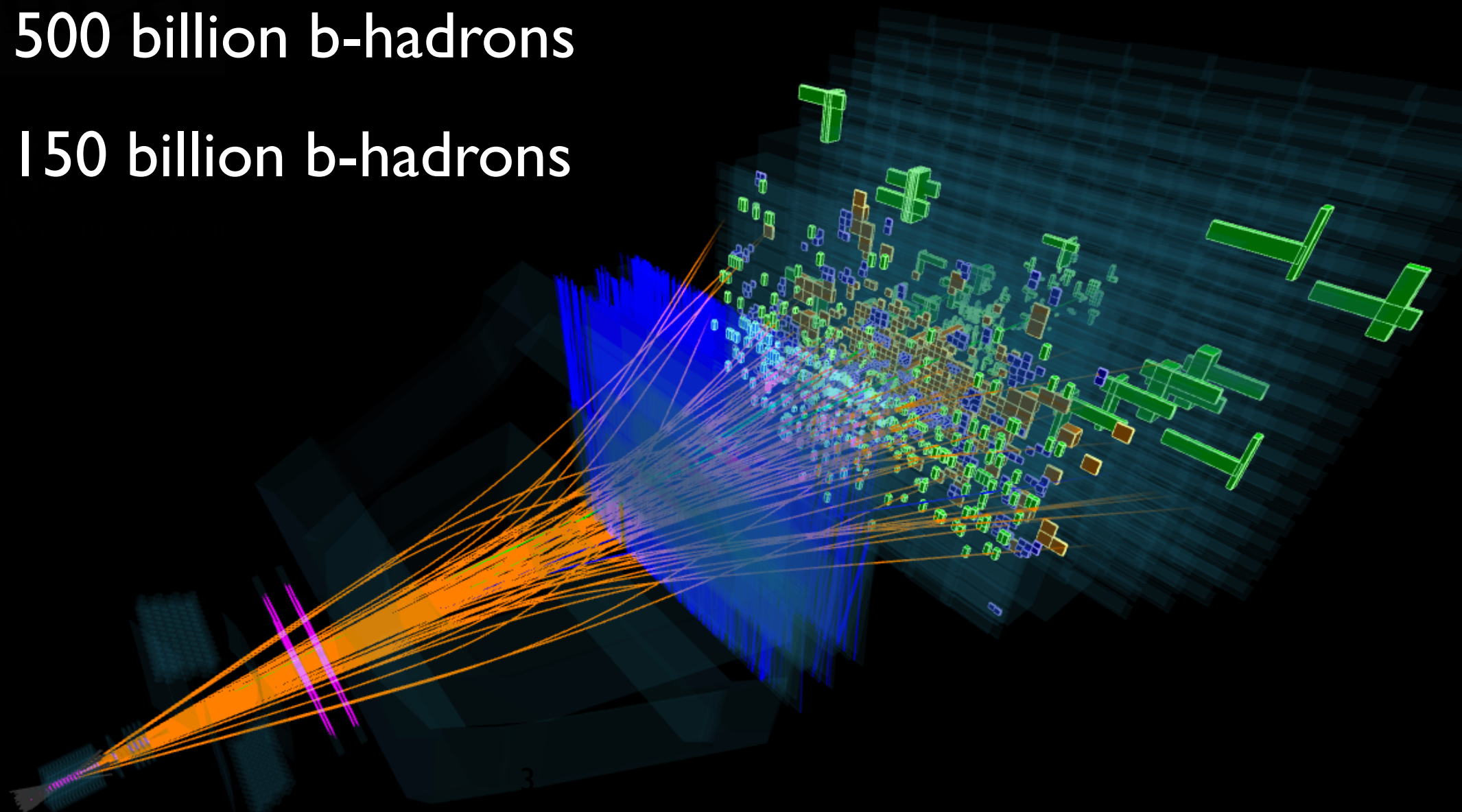
- CP violation in B decays
- New Physics searches at high energy scales
 - In rare beauty and charm decays
- Understanding QCD
 - Heavy flavour production, hadron spectroscopy (pentaquark states, bc states), unique fixed target programme
- Quark Gluon Plasma studies:
 - Rich heavy ion programs (production at p-Pb/Pb-p, fixed target p/pB-Ne)

LHCb is designed for B-physics

- Built in the high b-hadron production cross section region $2 < \eta < 5$

[PRL 118, 052002 (2017)]

- $\sigma(pp \rightarrow bb)^{\text{LHCb}} @ 13\text{TeV} \sim 155\mu\text{b}$
- Run I: 500 billion b-hadrons
- Run II: 1150 billion b-hadrons



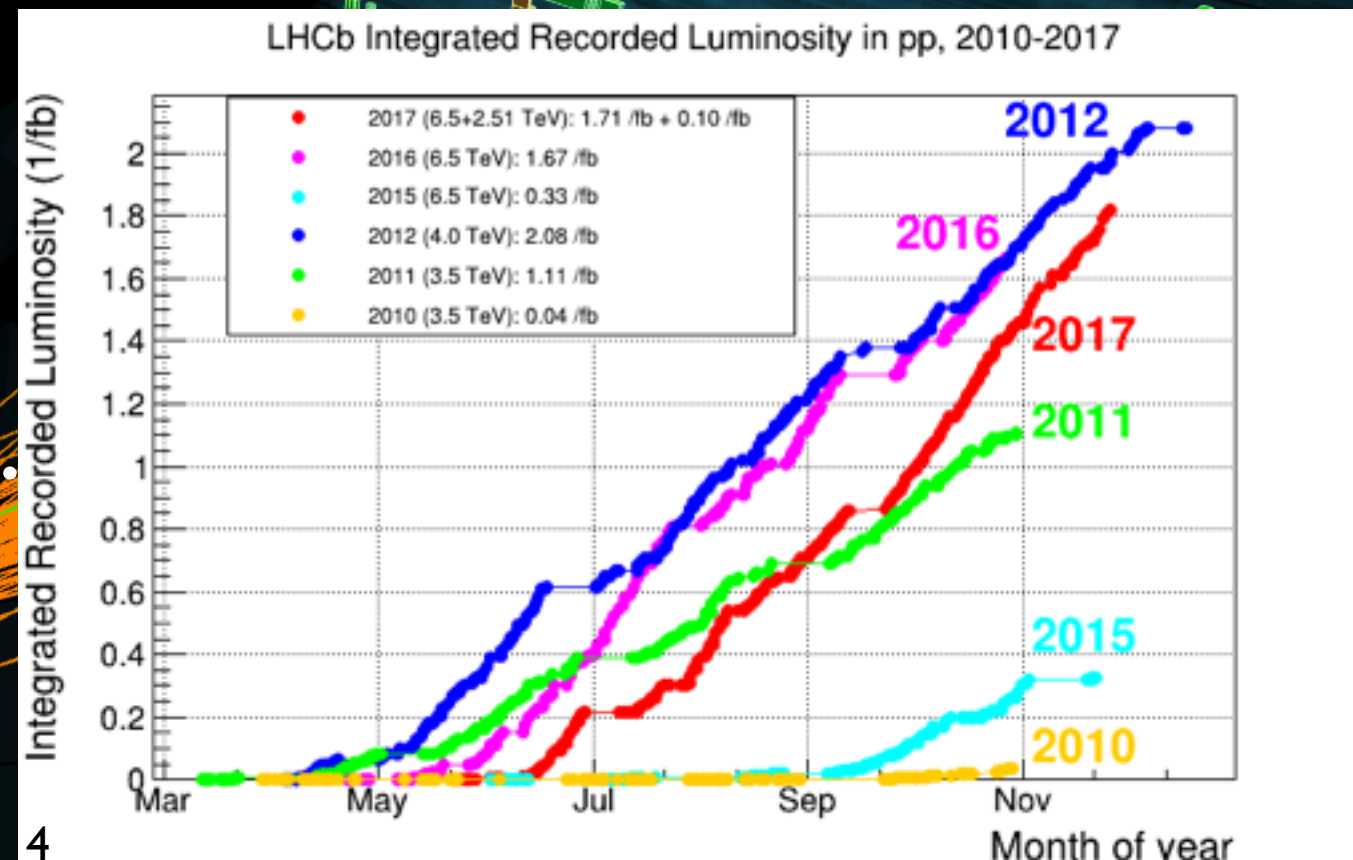
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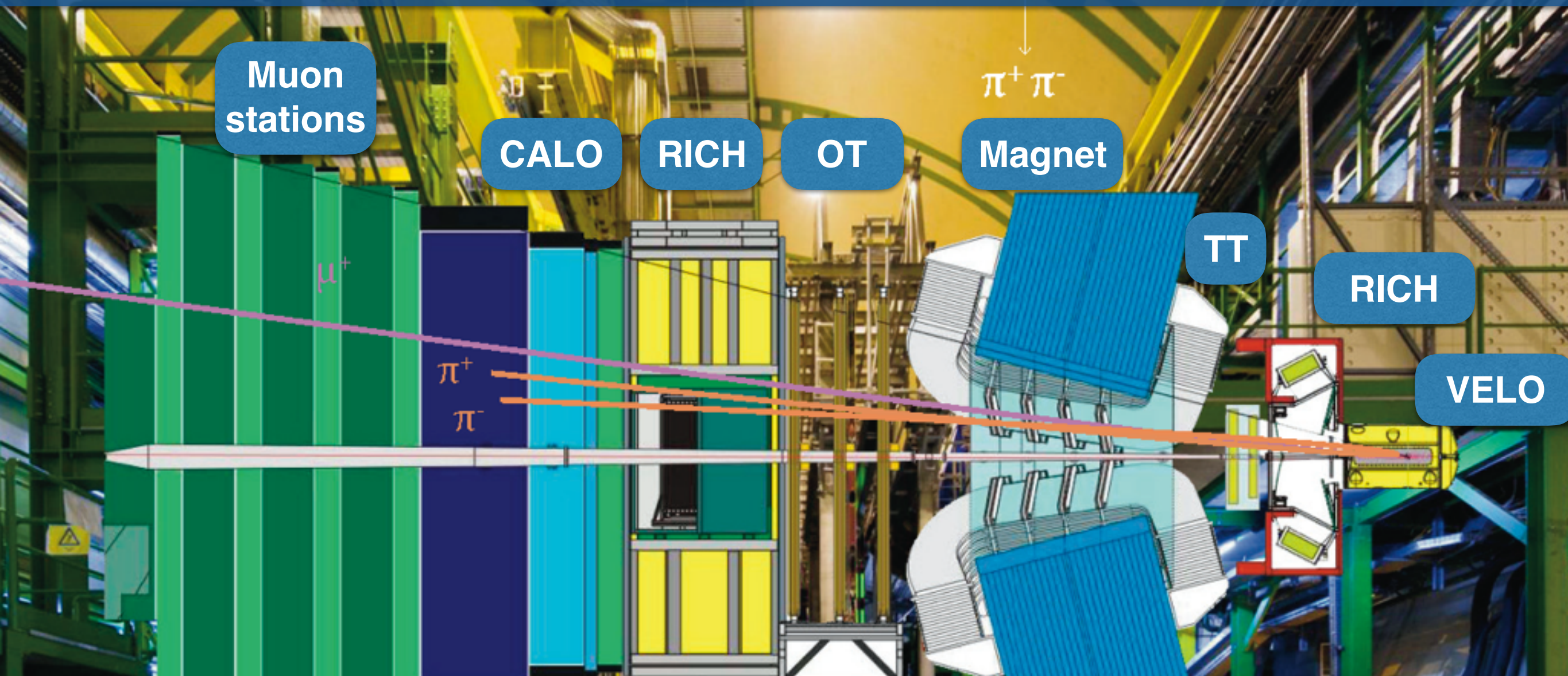
[PRL 118, 052002 (2017)]

- $\sigma(pp \rightarrow bb)^{\text{LHCb}} @ 13\text{TeV} \sim 155\mu\text{b}$
- Run I: 500 billion b-hadrons
- Run II: 1150 billion b-hadrons

- LHCb recorded 3fb^{-1} in Run I and 3.7fb^{-1} in Run II.
- High efficiency in 2017 ($\sim 91.4\%$)



LHCb detector @ LHC



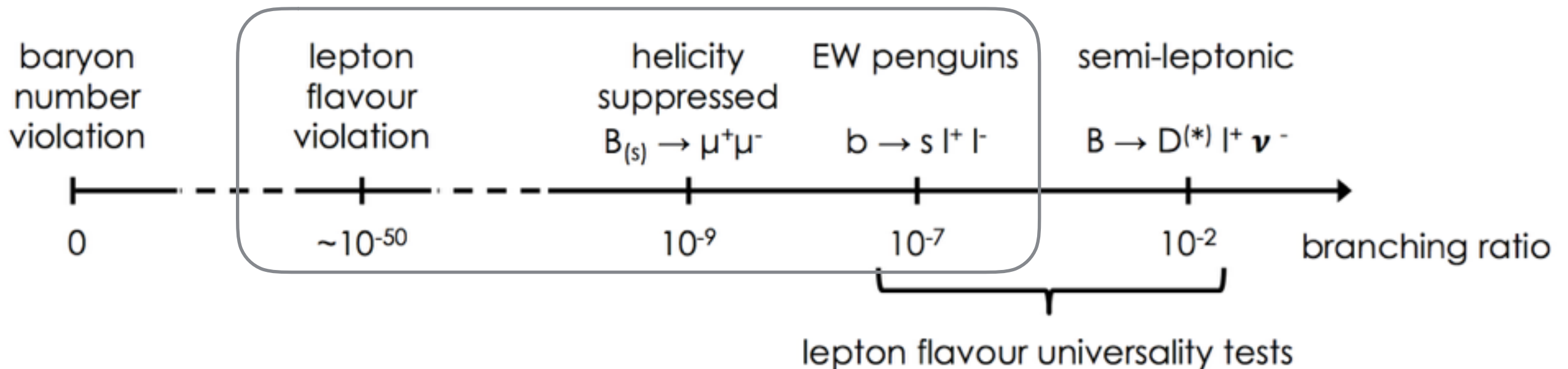
- Clean collision environment ($\mu \sim 1.6$) and high boost ($\gamma \sim 20$)
- Good mass resolution (~ 23 MeV for $B \rightarrow \mu^+ \mu^-$)

Excellent charged hadron identification, vertexing, high trigger and tracking efficiencies ($> \sim 90\%$) also in the low p_T range.

The large sample of precisely reconstructed B-decays is a true **goldmine** for New Physics searches.

Expose New Physics effects where the Standard Model is suppressed

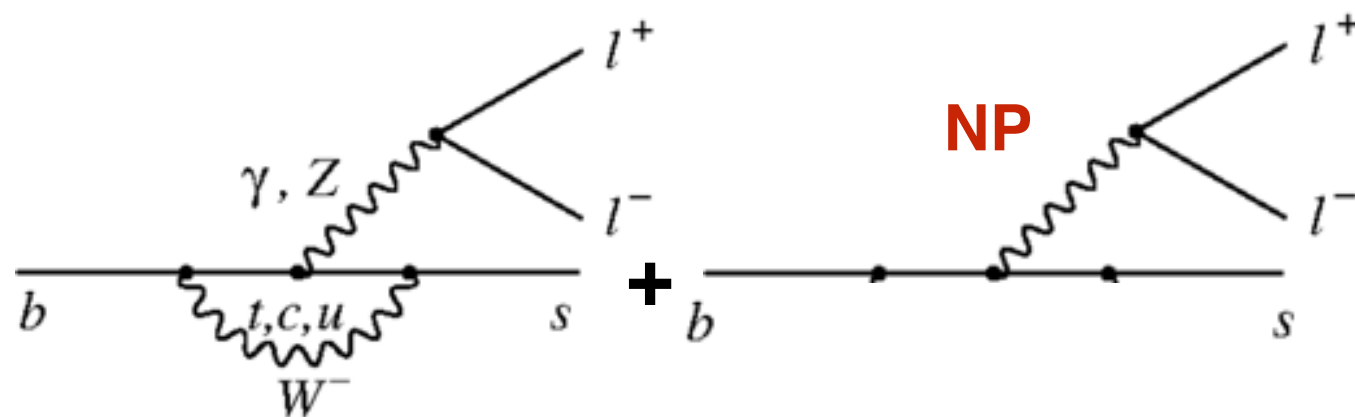
- $b \rightarrow sll$ and $b \rightarrow dll$ transitions are rare in the SM
No tree level contributions
(GIM, CKM, possibly helicity suppressed)



Expose New Physics effects where the Standard Model is suppressed

- New Physics can (in principle) enter at both tree and loop level:

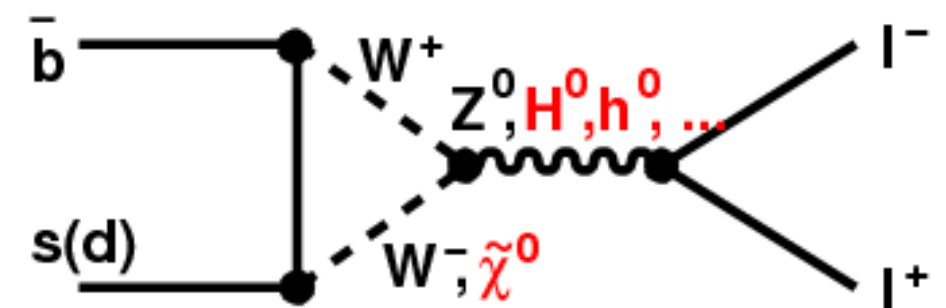
NP at tree level



$B_s \rightarrow \mu^+ \mu^-$ sensitive to Z 's up to $\sim 150 \text{ TeV}$ or new scalars up to 1000 TeV

[A.Buras et al,
JHEP 1411 (2014) 121]

NP at loop level

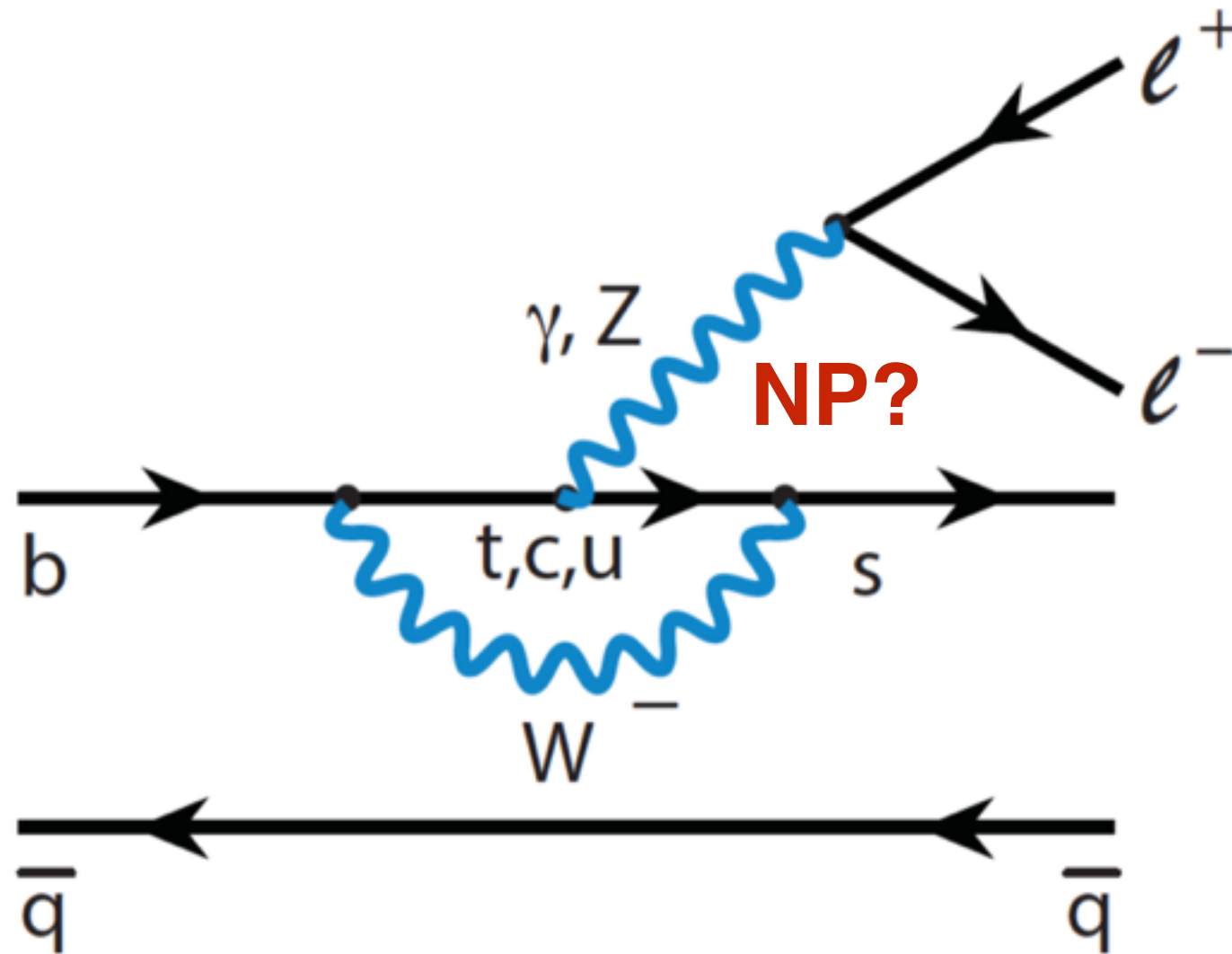


In $B_s \rightarrow \mu^+ \mu^-$ (pseudo)scalars can bypass the helicity suppression

A strong case for indirect searches

- Indirect searches are sensitive to higher energy scales ($\sim 100\text{TeV}$)
- Historically, indirect searches have led the way in shaping the Standard Model (e.g. charm predicted 4 years before the direct proof)
- Complementary to (but no substitute for) the comprehensive direct NP search programmes



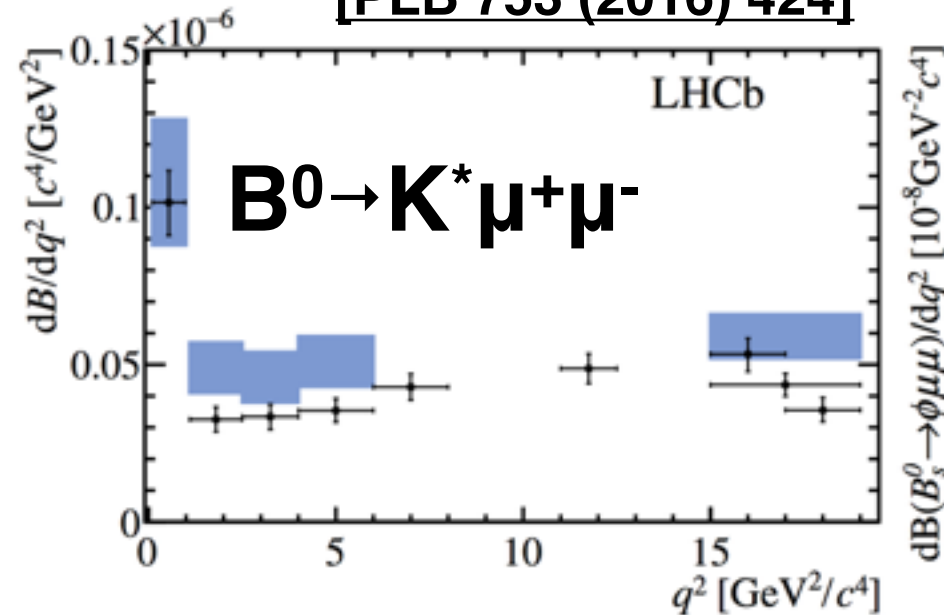


- For several reasons, rare decays involving $b \rightarrow sll$ transitions have emerged as possibly the most interesting phenomena in particle physics..

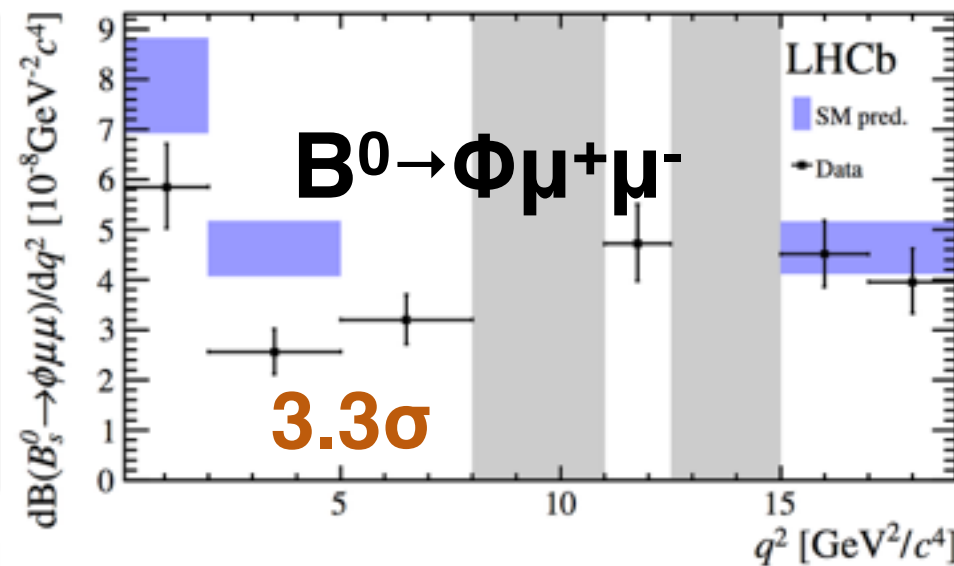
First: exclusive $b \rightarrow s \mu^+ \mu^-$ branching fractions

[JHEP 04 (2017) 142]

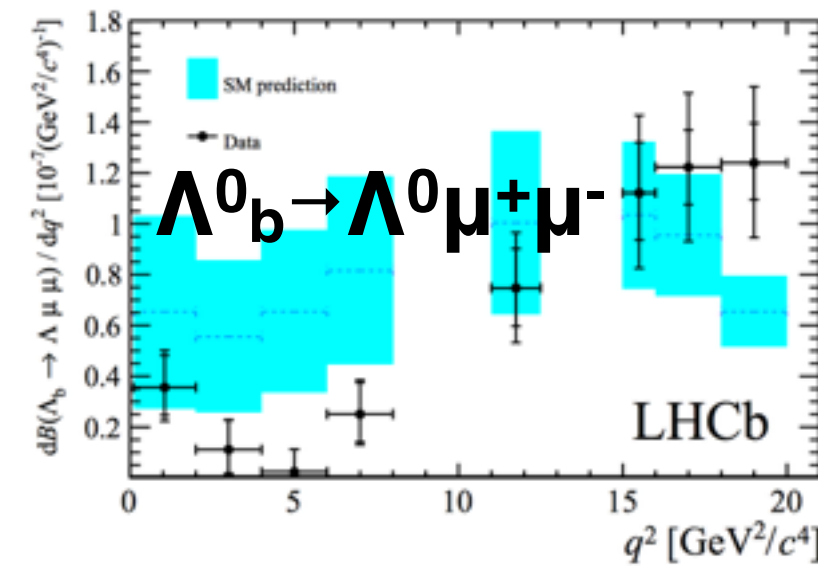
[PLB 753 (2016) 424]



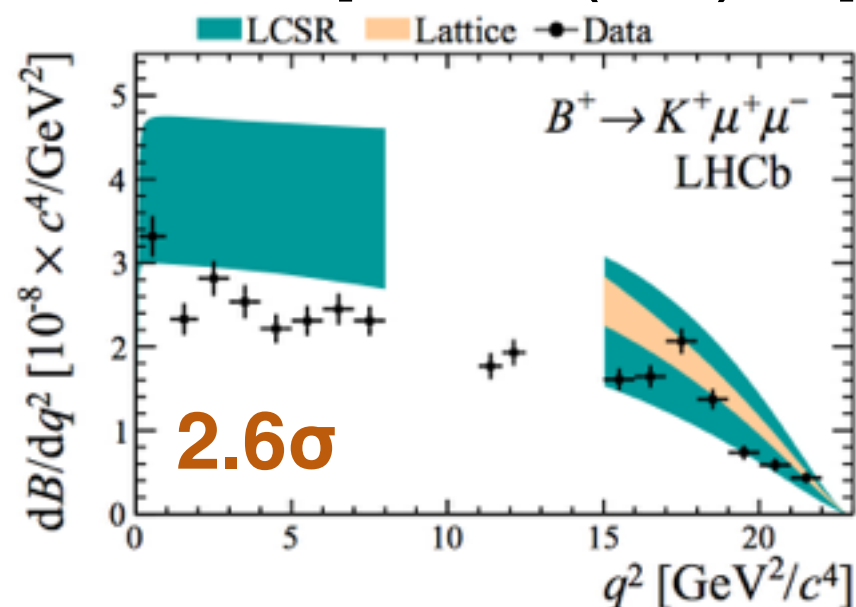
[JHEP 09 (2015) 179]



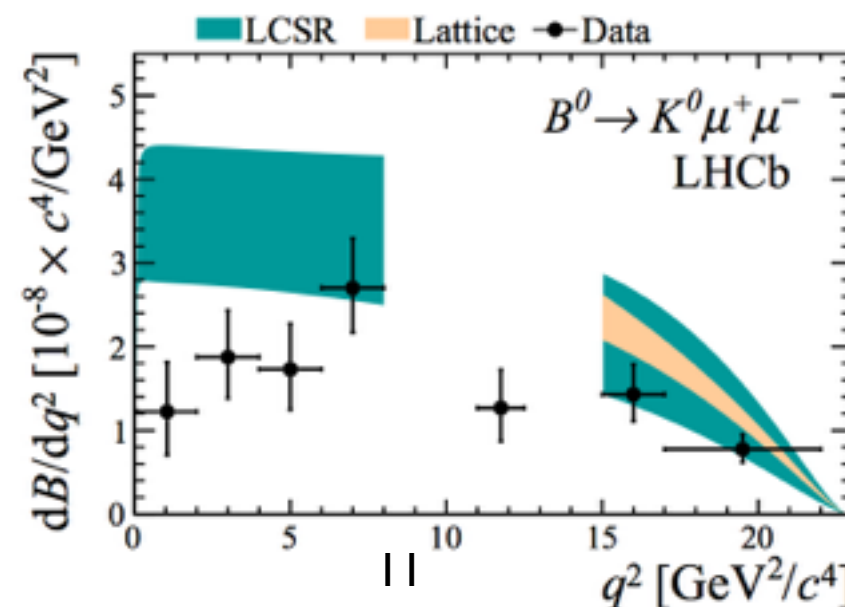
[JHEP 06 (2015) 115]



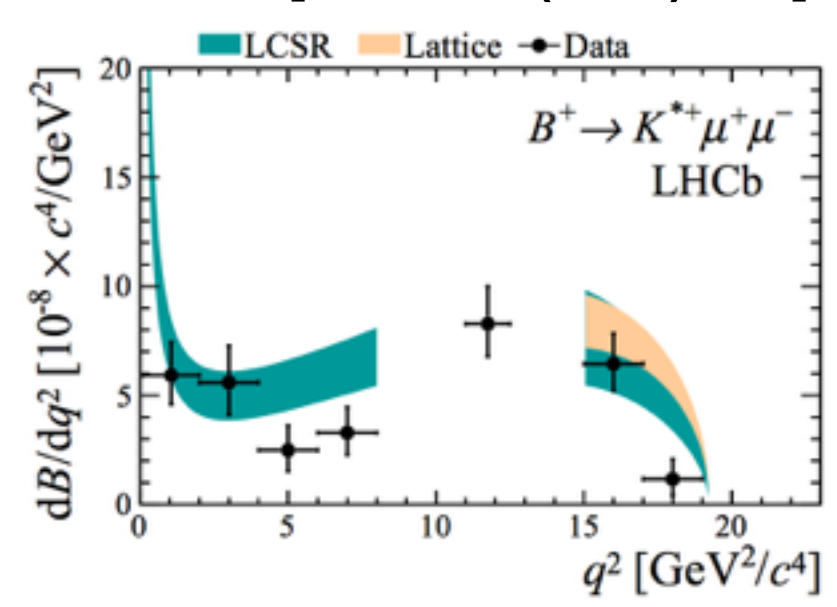
[JHEP 06 (2014) 133]



[JHEP 06 (2014) 133]



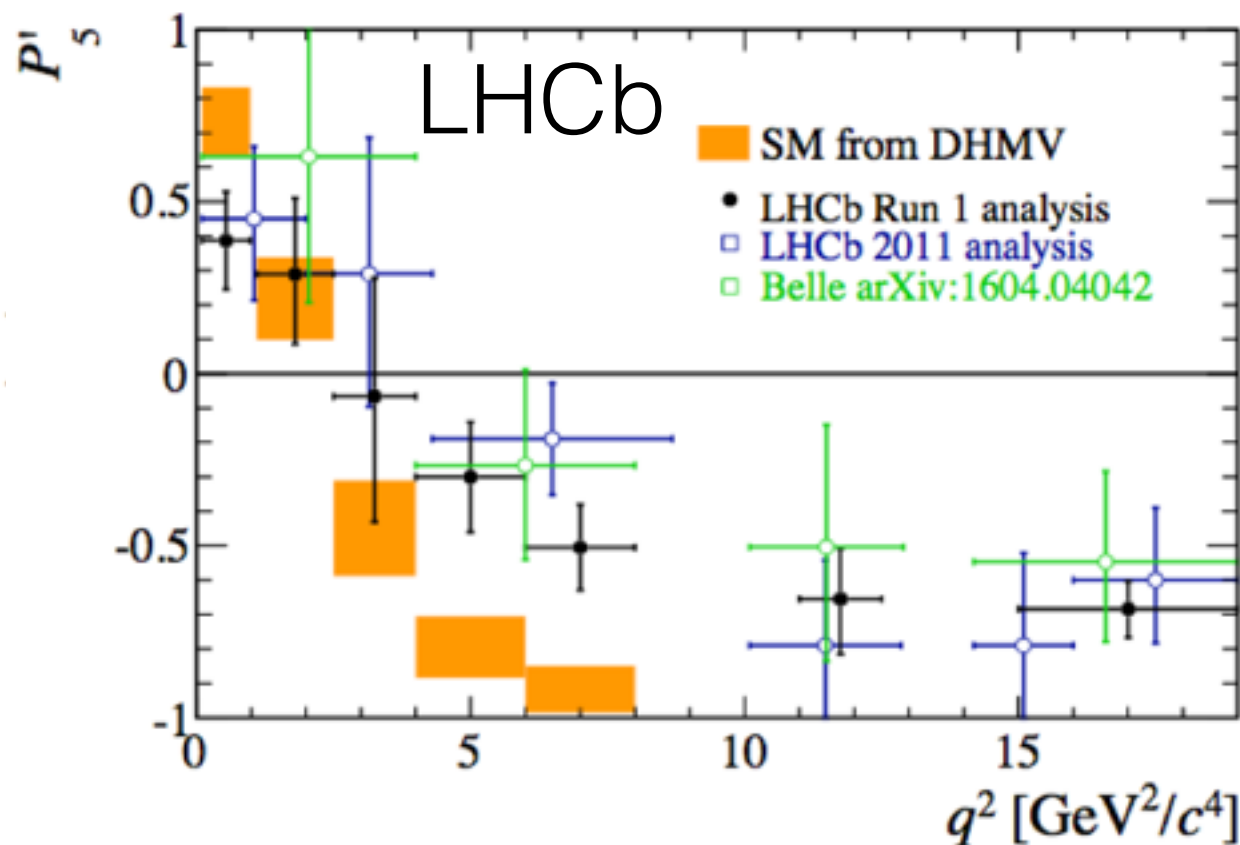
[JHEP 06 (2014) 133]



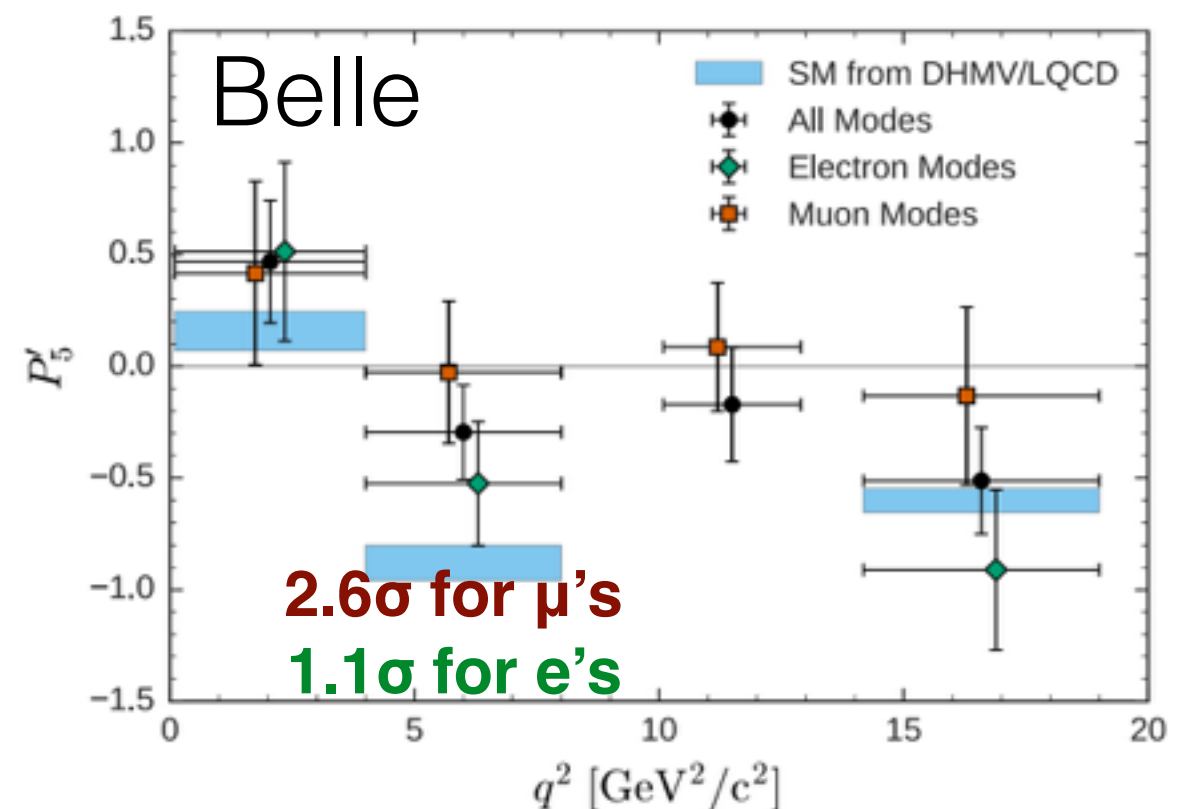
Second: tensions in $b \rightarrow s l^+ l^-$ angular observables

$B^0 \rightarrow K^* \mu^+ \mu^-$

[JHEP 02 (2016) 104]



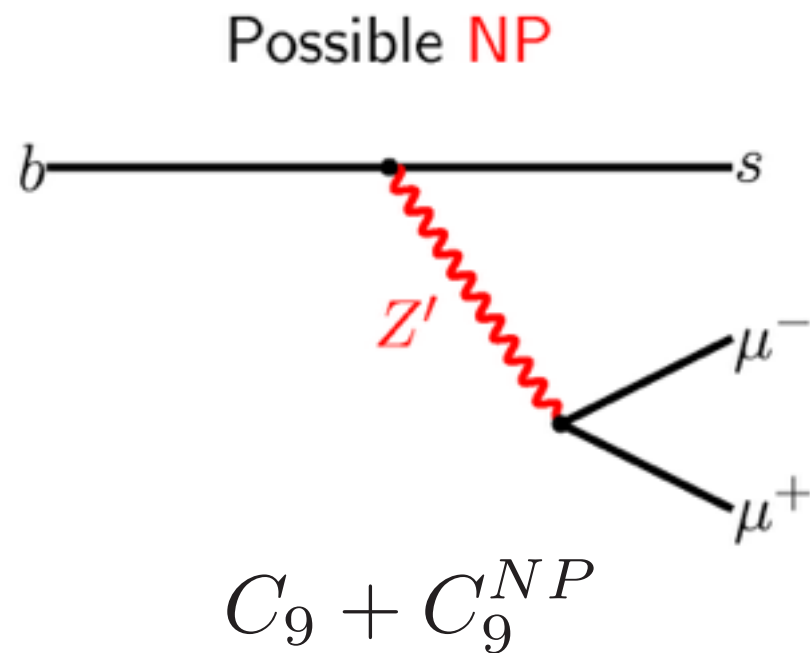
[PRL 118 (2017) 111801]



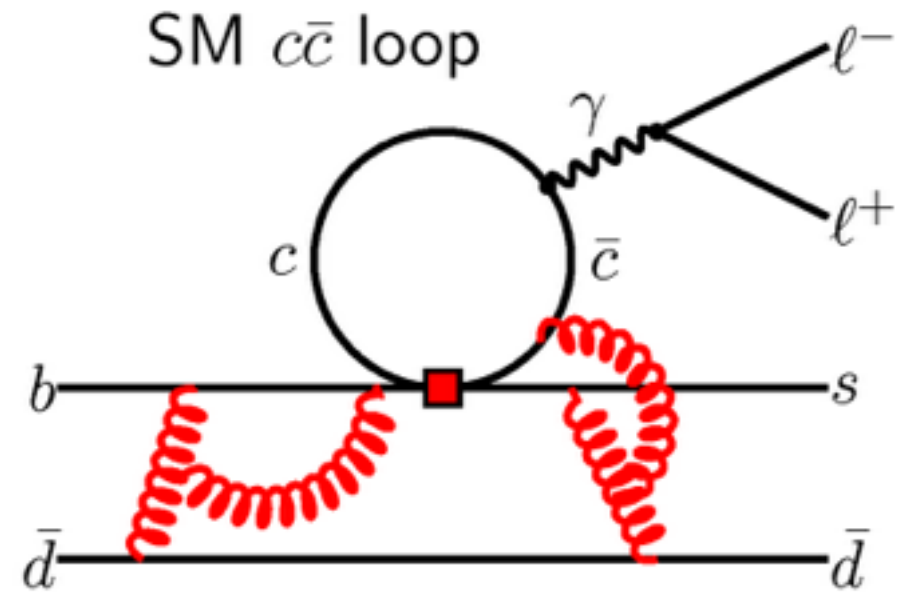
- Theoretically clean angular parameter P'_5 diverges from the predictions (3.4σ)
- The tension is larger for muons

New Physics is not the only possible explanation to these effects:

Z', leptoquarks,...



Hadronic SM effects



$$C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{res}(q^2)$$

Long-distance charm resonance effects far from the resonances on the q^2 plane.

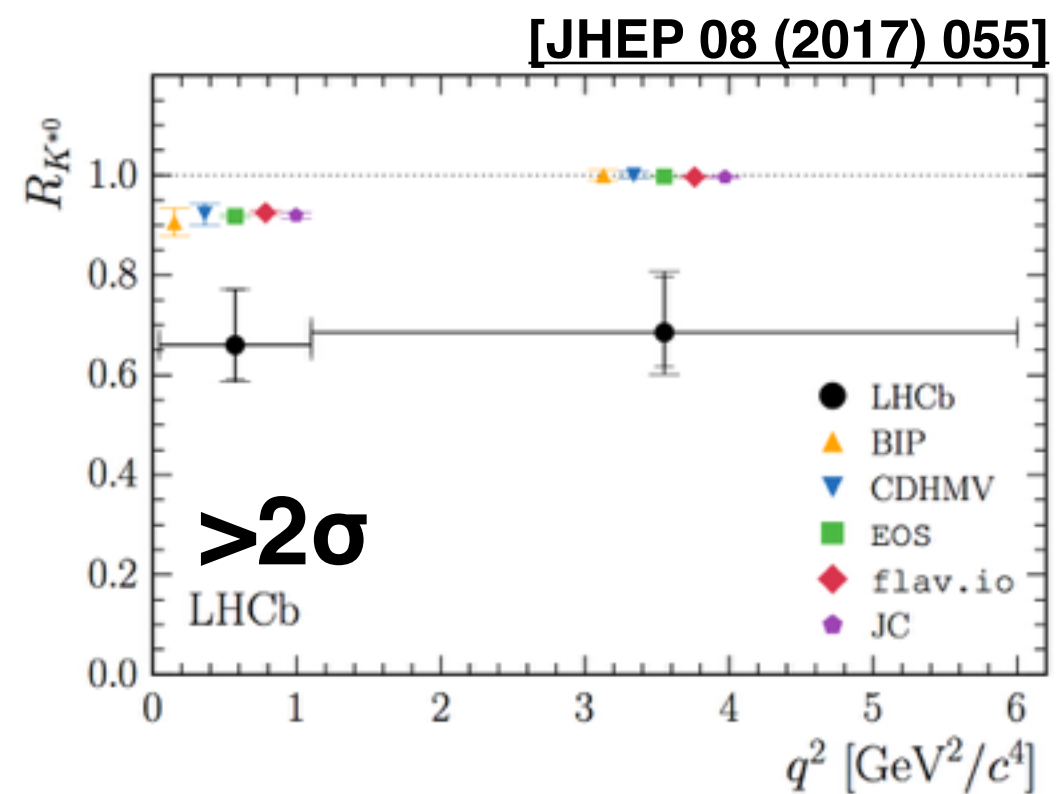
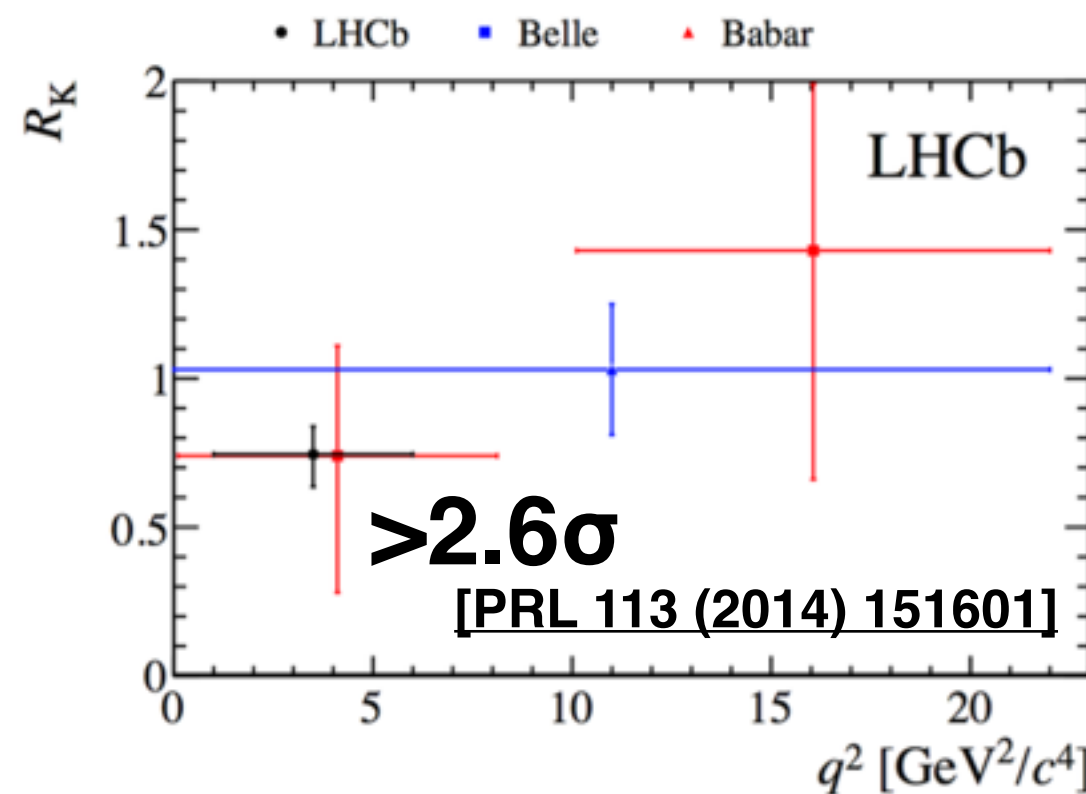
But...if it were due to hadronic effects..

..then we should see no deviations from the SM in the ratios of $b \rightarrow sl$ branching fraction.

Third: tensions in ratios:

$$b \rightarrow s \mu^+ \mu^- / b \rightarrow s e^+ e^-$$

- The measured muon and electron mode ratios are lower than predicted in the SM (LFU)

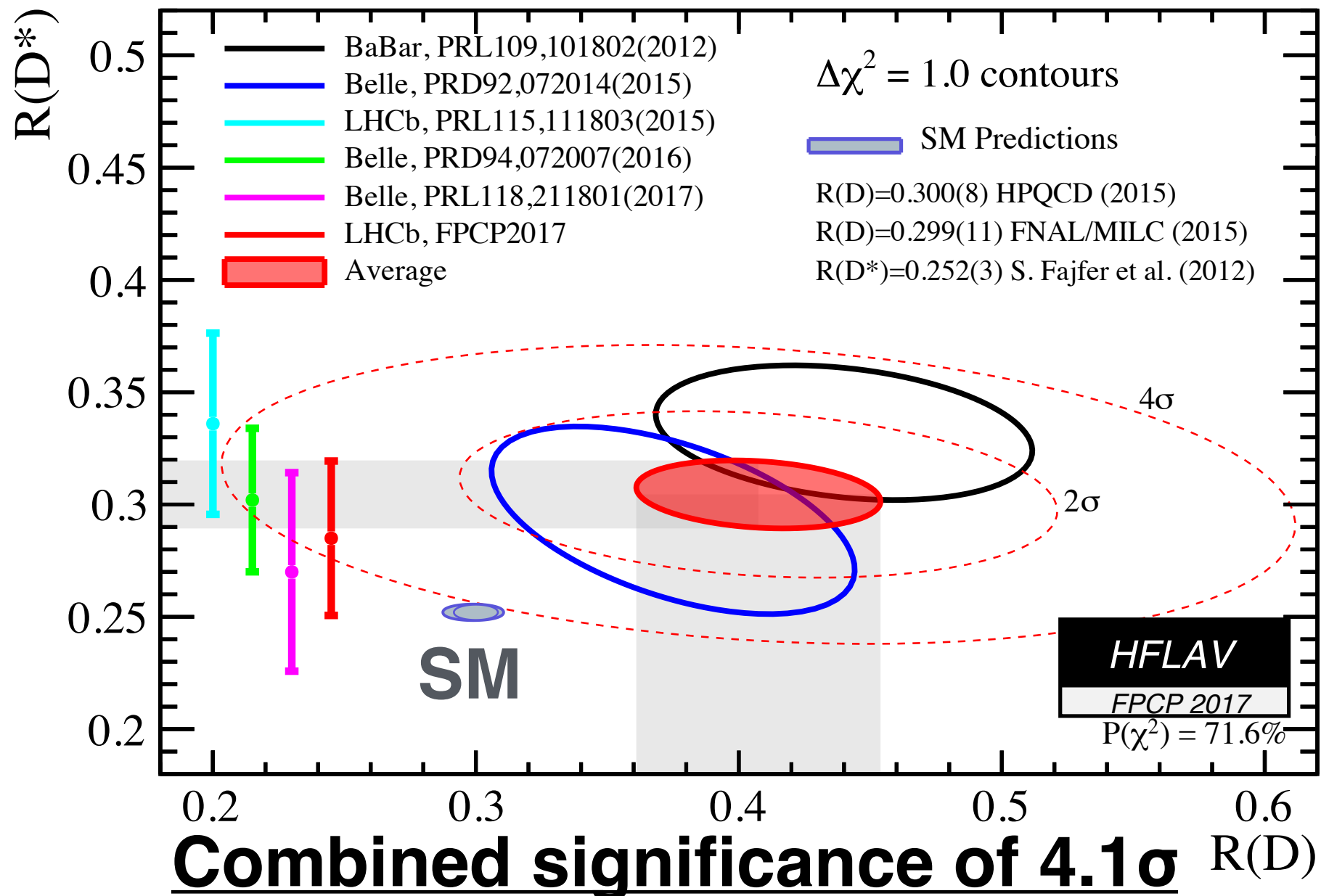


$$\mathcal{R}(K) \equiv \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}$$

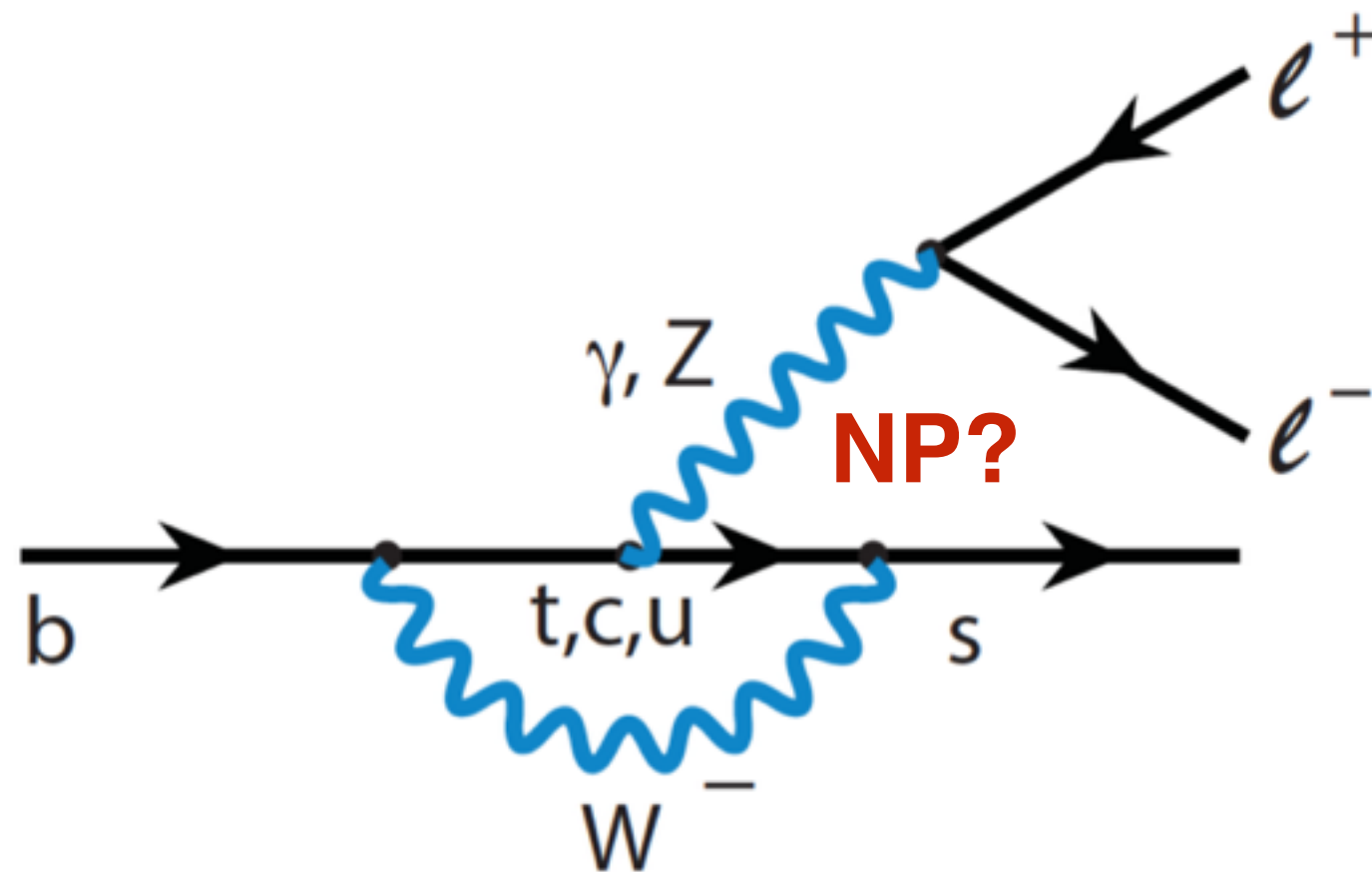
$$\mathcal{R}(K^*) \equiv \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)}$$

...a footnote: LFU divergencies are also seen in the semi-leptonic B decays via $b \rightarrow cl^+l^-$ transitions:

$$\mathcal{R}(D^{(*)}) \equiv \frac{\mathcal{B}(B^0 \rightarrow D^{(*)-} \tau^+ \nu_\tau^-)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \mu^+ \nu_\mu^-)}$$



What can fully leptonic B-decays add?



All B-decays include processes over a wide energy range:



and can be described by the **effective field theory** and **operator product expansion** by splitting the scale at b mass (μ_b):

$$A(B \rightarrow f) = \langle f | \mathcal{H}_{eff} | B \rangle = \frac{G_F}{\sqrt{2}} \sum_i \lambda_{CKM} \underbrace{C_i(\mu_b)}_{\text{Wilson coefficients (perturbative)}} \underbrace{\langle f | \mathcal{Q}_i(\mu_b) | B \rangle}_{\text{Hadronic matrix el. (include non-perturbative QCD)}}$$

Wilson coefficients (perturbative) **Hadronic matrix el.** (include non-perturbative QCD)

Leptonic modes

$$\langle ll | j_{ll} \cdot j_{qq} | B_q \rangle = \langle ll | j_{ll} | 0 \rangle \cdot \underbrace{f_{B_q}}_{\text{Lattice QCD}}$$

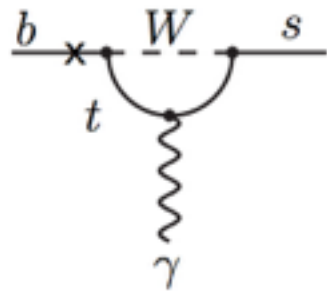
Lattice QCD

Semi-leptonic modes:

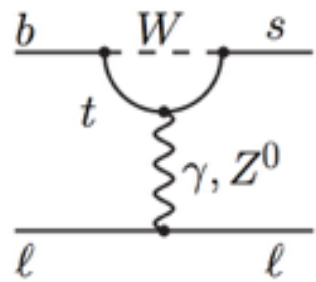
$$\langle ll M | j_{ll} \cdot j_{qq} | B \rangle = \langle ll | j_{ll} | 0 \rangle \cdot \underbrace{F(q^2)}_{\text{Lattice QCD (large } q^2)} + \underbrace{C_{non-fact}}_{\text{corrections}}$$

Lattice QCD (large q^2)
Light Cone Sum Rules (small q^2)

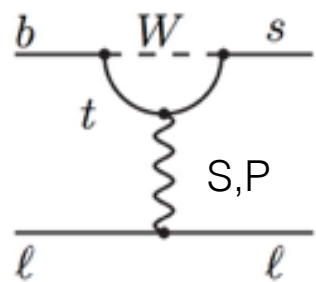
The A-V semi-leptonic current (O_{10}) contributes to both semi-leptonic and fully leptonic B-decays:



Electromagnetic
penguin



Semi-leptonic
vector current
Semi-leptonic
A-V current



Scalar

Pseudo-scalar

$$Q_7^{(')} = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_{R(L)} b) F^{\mu\nu}$$

$$Q_9^{(')} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{l} \gamma^\mu l)$$

$$Q_{10}^{(')} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{l} \gamma^\mu \gamma_5 l)$$

$$Q_S^{(')} = \frac{e^2}{16\pi^2} (\bar{s}_{L(R)} b_{R(L)}) (\bar{l} l)$$

$$Q_P^{(')} = \frac{e^2}{16\pi^2} (\bar{s}_{L(R)} b_{R(L)}) (\bar{l} \gamma_5 l)$$

$b \rightarrow s l^+ l^-$

$B_{(s)}^0 \rightarrow l^+ l^-$

*In SM only O_{10} contributes to the leptonic modes, Higgs contribution via O_S is negligible

➡ **New Physics** can

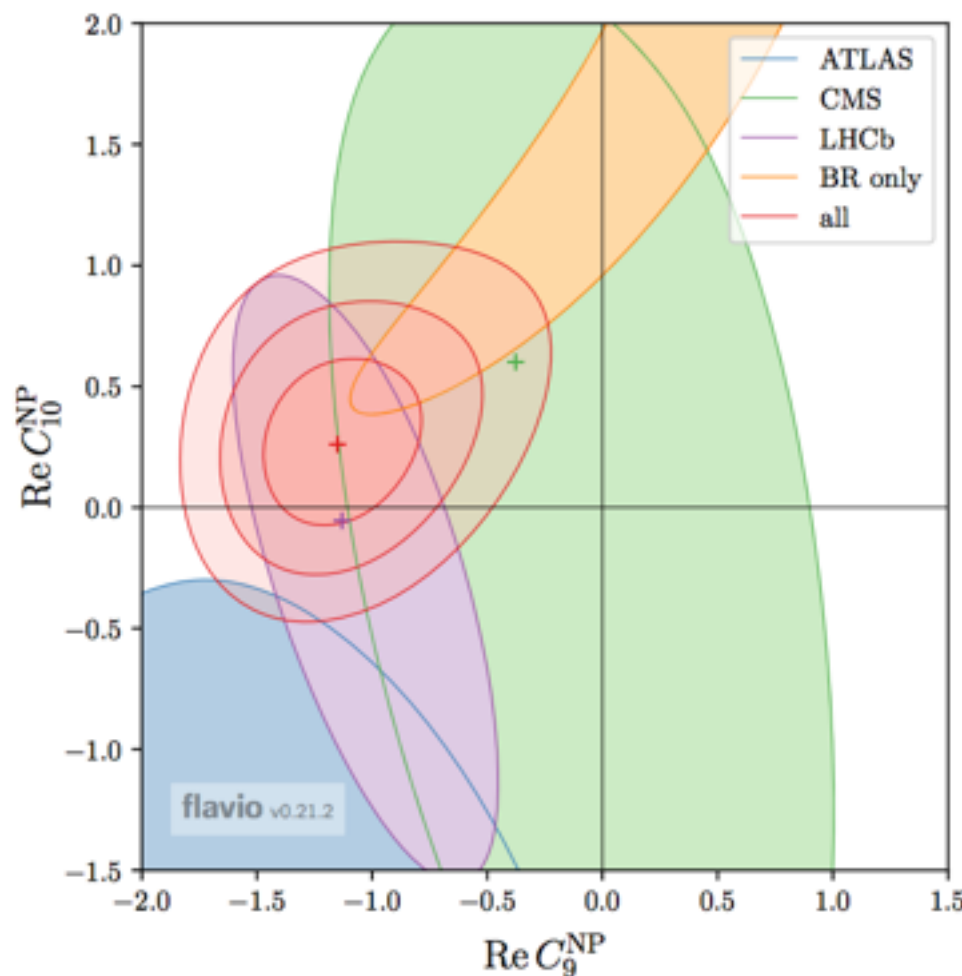
➡ alter the SM operator contributions (Wilson coefficients)

➡ enter through new operators (right-handed Q's, $Q_{S,P}$)

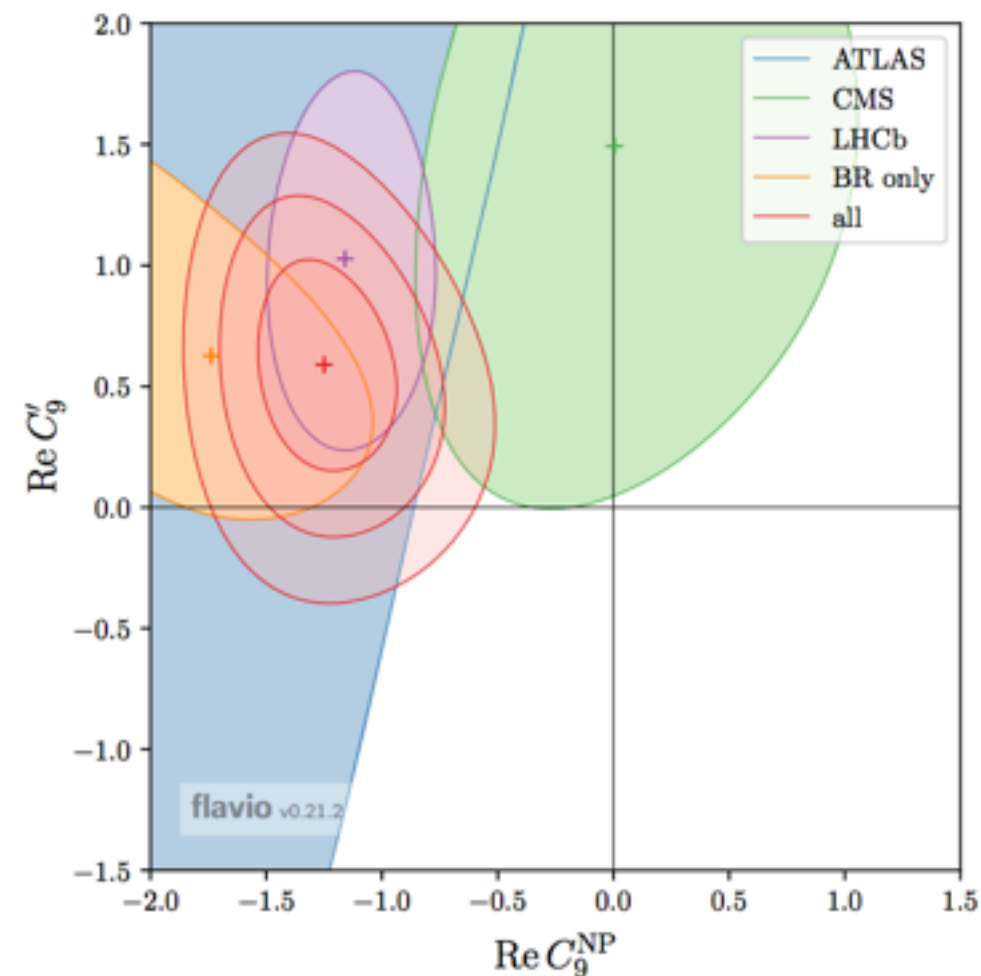
The Wilson coefficients are determined from global $b \rightarrow sl^+l^-(\gamma)$ analysis, which point to

- tensions at 4-5 σ level w.r.t SM in left-handed muon couplings
- two favoured (model independent) solutions to the tensions:

a) $C_9^{\text{NP}} = -C_{10}^{\text{NP}}$



b) $C_9^{\text{NP}} < 0$



Altmannshofer et al [EPJC (2017) 77:377], Capdevila et al [PSI-PR-17-05]

(~90 measurements e.g. in Descotes-Genon, Hofer, Matias, Virto [JHEP 06 (2016) 092], Altmannshofer, Straub [EPJ C 75(8) (2015) 382], Hurth, Mahmoudi, Neshatpour [arXiv:1603.00865])

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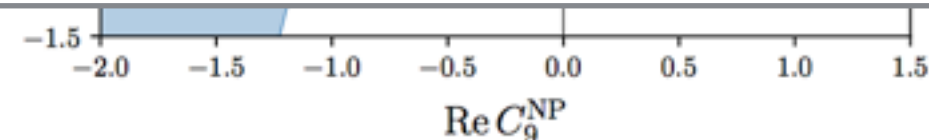
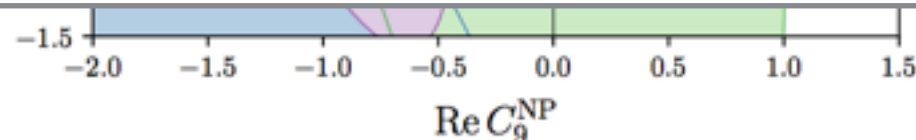
b) $C_9^{\text{NP}} < 0$



Alt
77:
PR

Rare fully leptonic B decays provide:

- a clean, reliable and complementary way to determine the axial-vector contribution (C_{10}^{NP})
- also sensitive to new (pseudo-)scalar contributions ($C_{P,S}$ free from helicity suppression)



The experimental success story of

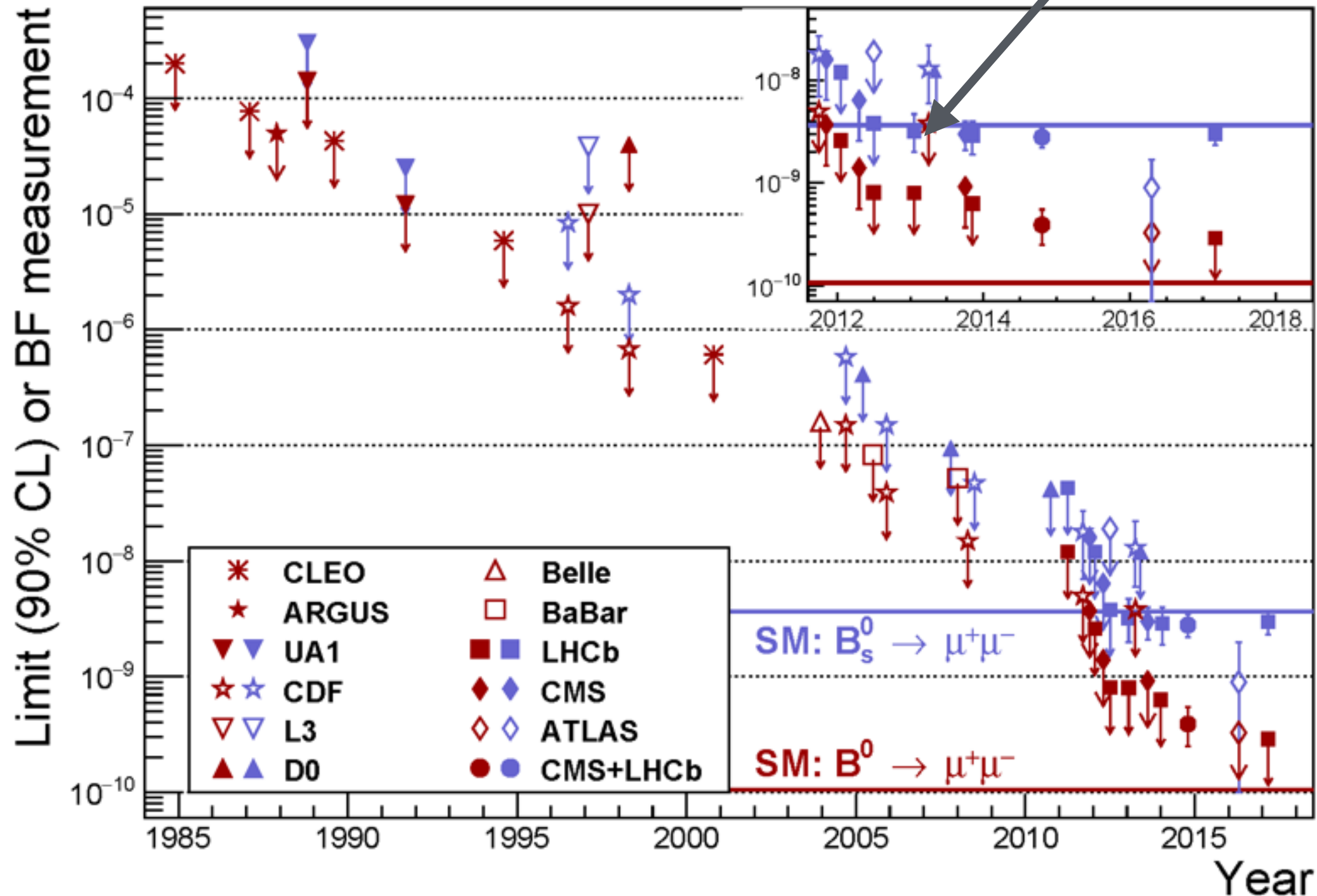
$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

One of the most important indirect
New Physics probes at the LHC.

Persistence that paid off after 30 years

[PRL 110, 021801 (2013)]

2013: first evidence
seen by LHCb



The combined Run I $B^0_{(s)} \rightarrow \mu^+ \mu^-$ analysis models

CMS

LHCb

MisID

Shared

$$\mathcal{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$$

$$f_s/f_d$$

$$\mathcal{BR}(B^+ \rightarrow J/\psi K^+)$$

And common BR values
for exclusive backgrounds

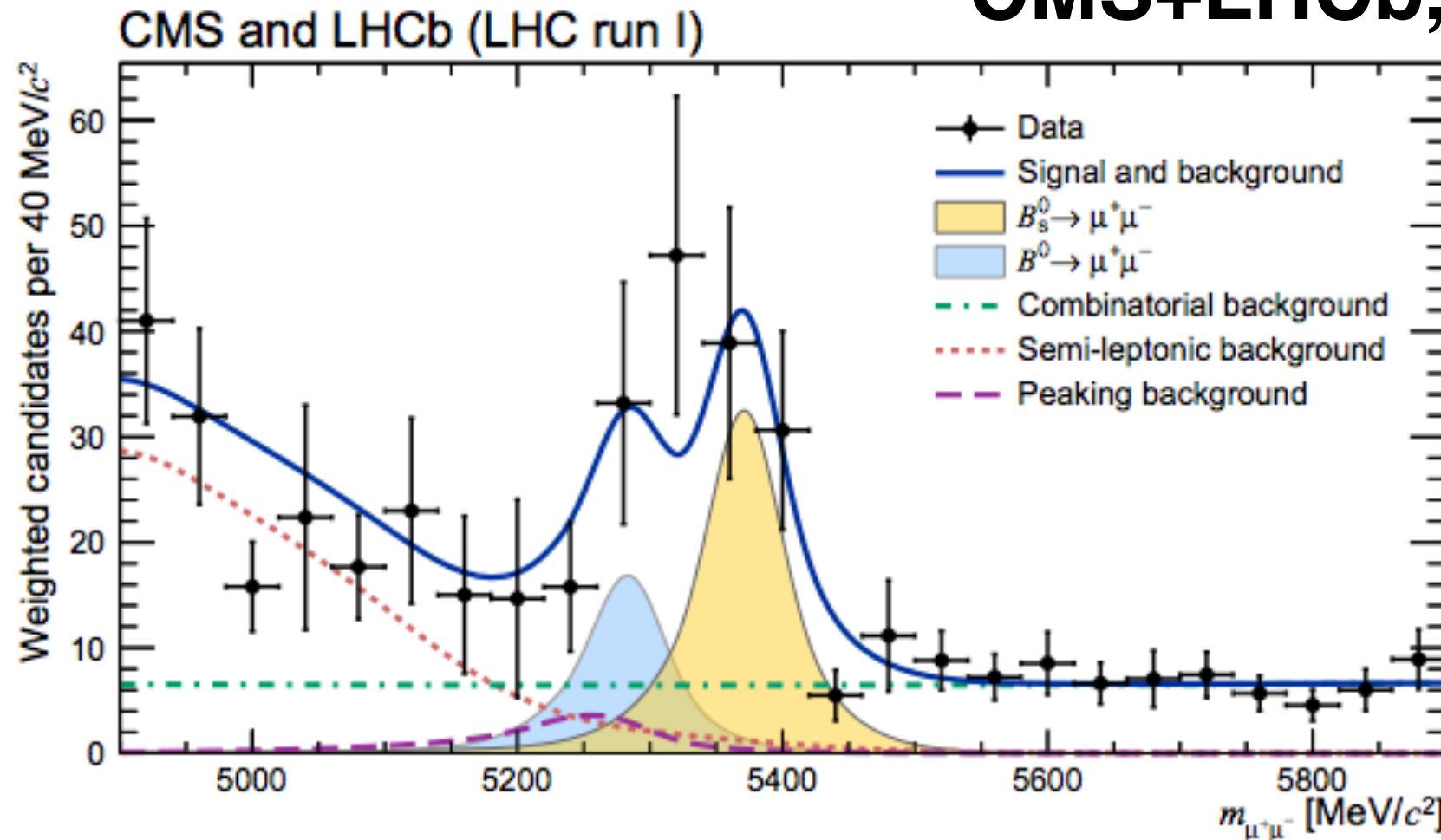
Peaking bkg
shape pars.

Mass and signal shape
parameters

2015

The first observation of $B_s \rightarrow \mu\mu$ decay and the first evidence of $B_d \rightarrow \mu\mu$:

CMS+LHCb, Run I



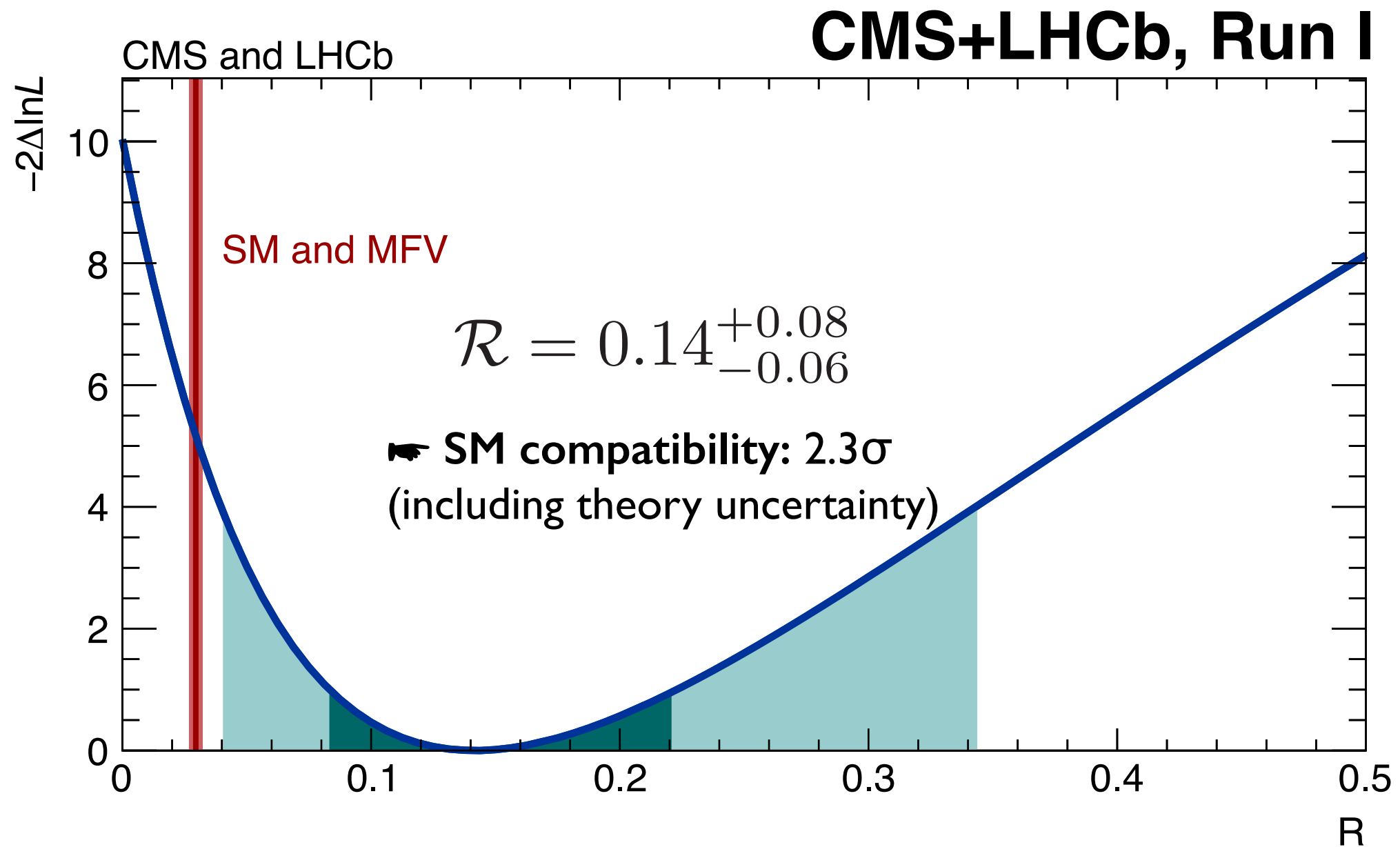
➡ The fitted central BF values

$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-) = 2.8_{-0.6}^{+0.7} \times 10^{-9} \quad \mathbf{6.2\sigma \text{ obs. (expected } 7.2\sigma \text{ in SM)}}$$

$$\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-) = 3.9_{-1.4}^{+1.6} \times 10^{-10} \quad \mathbf{3.2\sigma \text{ obs. (expected } 0.8\sigma \text{ in SM)}}$$

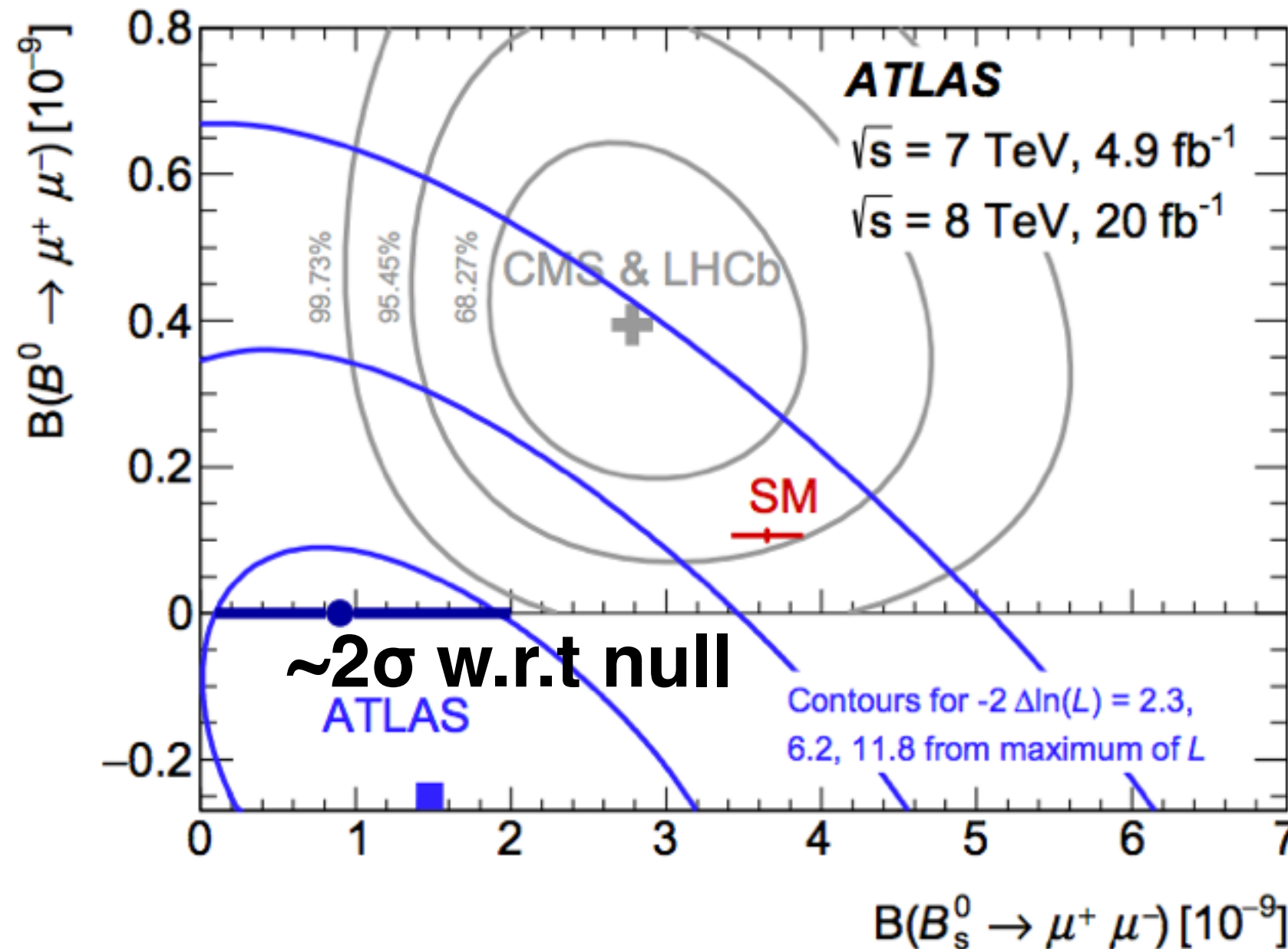
*Cross-checked with Feldman-Cousins:
3.0 σ (official significance)

The ratio $R = \text{BF}(B_d \rightarrow \mu\mu) / \text{BF}(B_s \rightarrow \mu\mu)$ is a precise test of minimal flavour violation (MFV):



Run I results from ATLAS are in agreement.

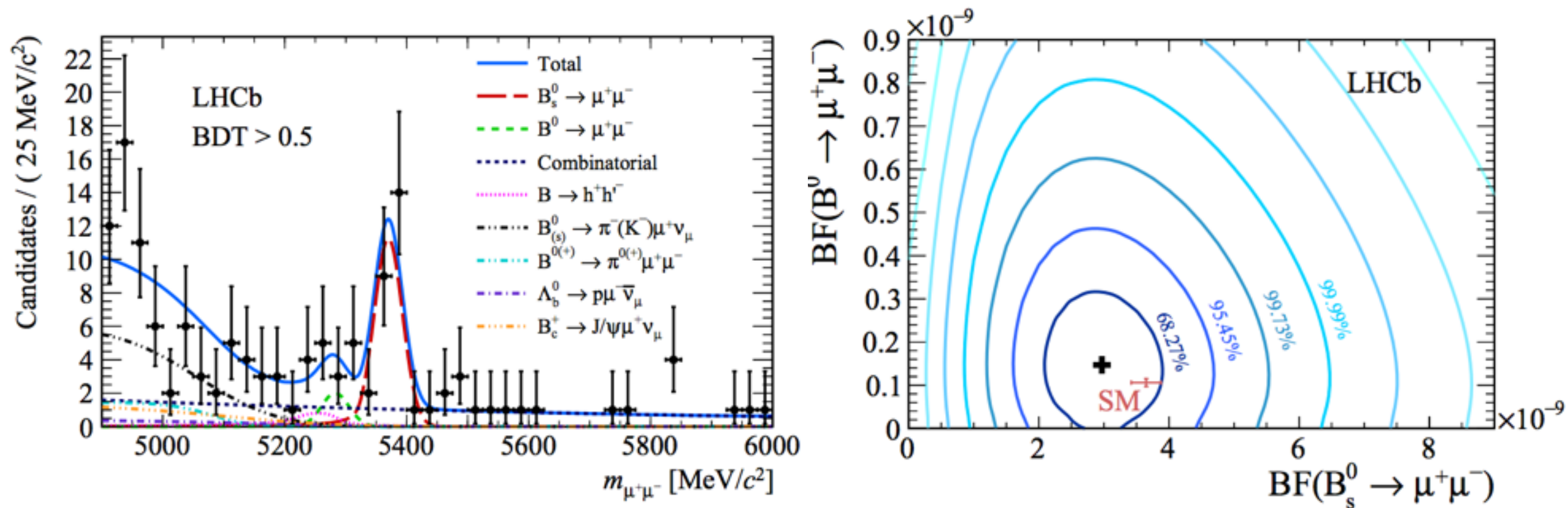
$B_s \rightarrow \mu\mu$ excess at 2σ :



$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-) = 0.9_{-0.8}^{+1.1} \times 10^{-9} \quad (2\sigma)$$

$$\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-) < 4.2 \times 10^{-10} \quad (95\% CL)$$

In Run II, LHCb observes $B_s \rightarrow \mu^+ \mu^-$ independently with 7.8σ :



➡ LHCb Run I data (3fb^{-1}) + 2015 (0.33fb^{-1}) + 2016 (1.4fb^{-1})

➡ Several improvements compared to the old analysis:

- ➡ better di-hadron background rejection (50%)
- ➡ exclusive background estimates validated on data
- ➡ new isolation variables improve BDT

➡ The most precise results up to date,
first single experiment $B_s \rightarrow \mu\mu$ observation.

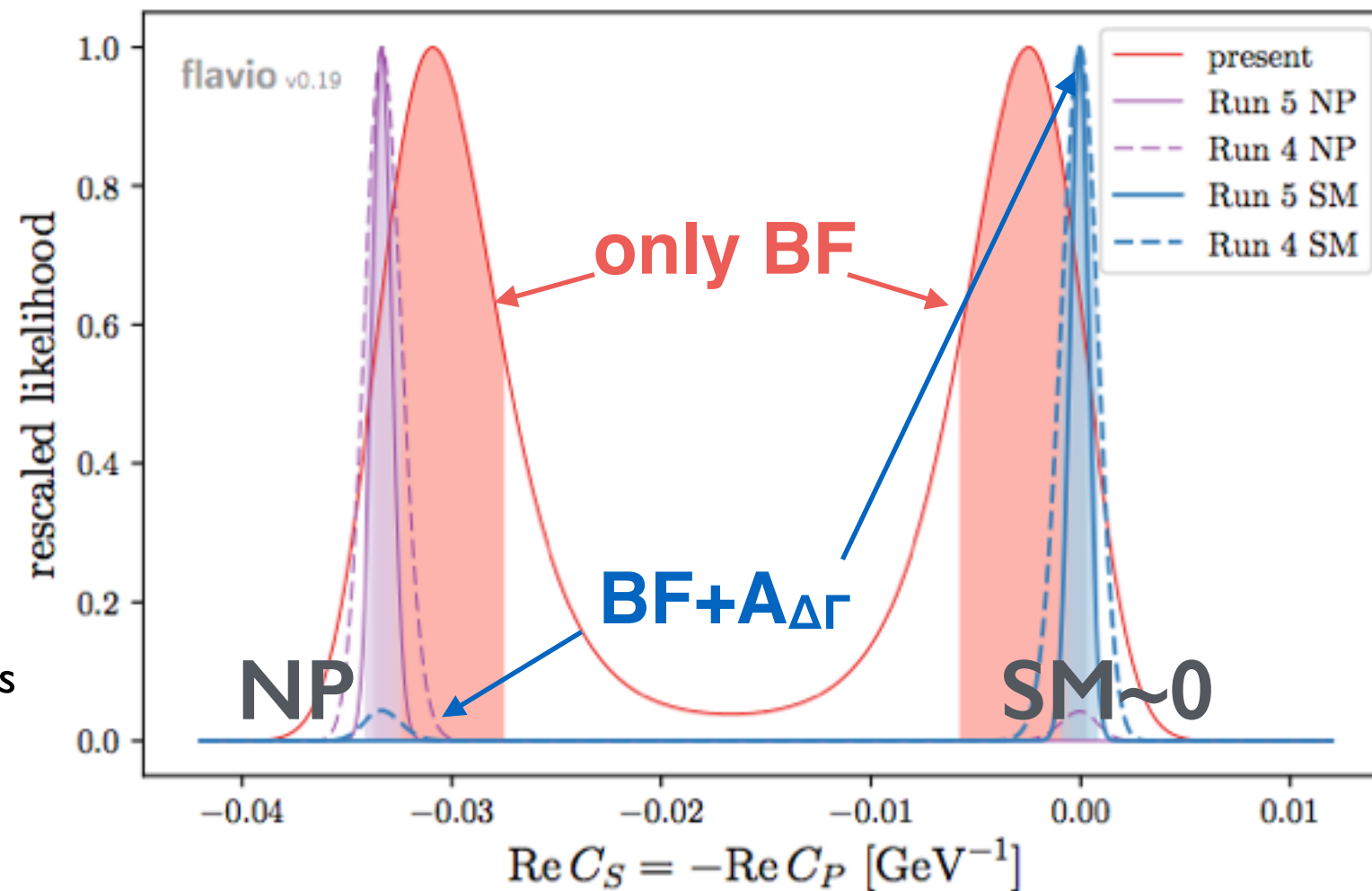
$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6_{-0.2}^{+0.3}) \times 10^{-9}$$

$$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) < 3.4 \times 10^{-10}$$

$B_s \rightarrow \mu\mu$ (7.8σ) and **$B_d \rightarrow \mu\mu$ (1.6σ)**

$B_s \rightarrow \mu^+ \mu^-$ is sensitive to new physics even if its branching ratio is not.

for example..



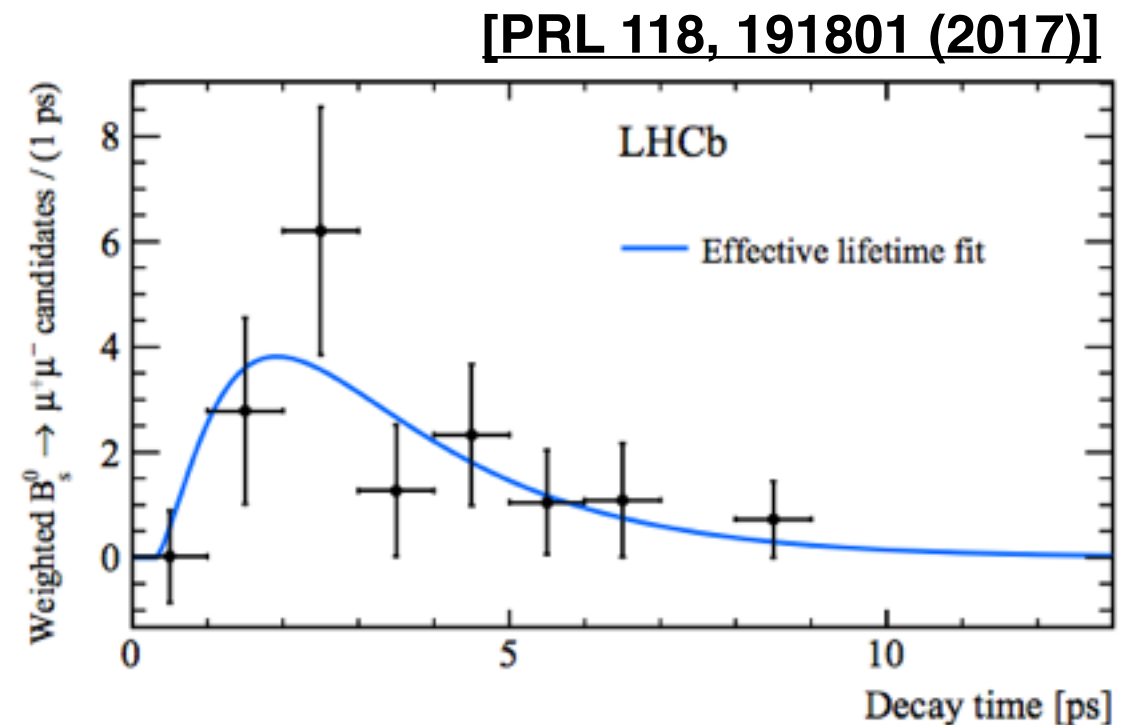
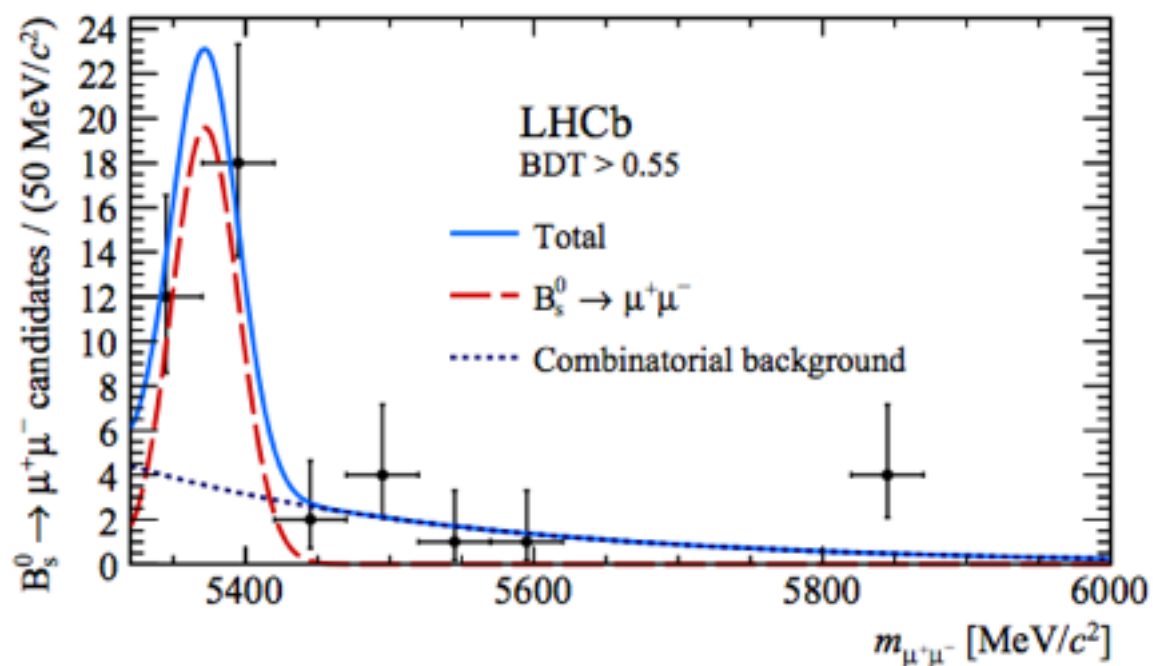
MFV NP: new (pseudo-)scalars
(MSSM, two-leptoquark
scenarios)

- Measured BF alone leads to ambiguity: e.g. $C_S = -C_P$ equally likely to the SM solution ($C_S = C_P = 0$)
- **Mass-eigenstate-rate asymmetry** ($A_{\Delta\Gamma}$) can solve the ambiguity:

$$A_{\Delta\Gamma} = \frac{\Gamma(B_s^H \rightarrow \mu^+ \mu^-) - \Gamma(B_s^L \rightarrow \mu^+ \mu^-)}{\Gamma(B_s^H \rightarrow \mu^+ \mu^-) + \Gamma(B_s^L \rightarrow \mu^+ \mu^-)} \quad \text{SM: } A_{\Delta\Gamma} = +1$$

LHCb goes beyond the counting: the first effective lifetime measurement

- $A_{\Delta\Gamma}$ can be determined from the effective $B_s \rightarrow \mu\mu$ lifetime:



$$\tau(B_s \rightarrow \mu^+\mu^-) = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$$

(stat) (syst)

- ➡ Compatible with the SM: $\tau(B_s \rightarrow \mu^+\mu^-)^{SM} = (1.615 \pm 0.010) \text{ ps}$
- ➡ First (proof of concept) measurement (no attempt to extract $A_{\Delta\Gamma}$ yet)
- ➡ Result consistent with the $A_{\Delta\Gamma} = +1(-1)$ at 1.0σ (1.4σ)

Goals for both before and after the upgrade(s)

2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033+
		Run III						Run IV					Run V	
LS2						LS3					LS4			
LHCb 40 MHz UPGRADE Phase I	$L = 2 \times 10^{33}$			LHCb Consolidation			$L = 2 \times 10^{33}$ 50 fb^{-1}			LHCb Ph II UPGRADE *		$L = 2 \times 10^{34}$ 300 fb^{-1}		
ATLAS Phase I Upgr	$L = 2 \times 10^{34}$			ATLAS Phase II UPGRADE			HL-LHC $L = 5 \times 10^{34}$			ATLAS		HL-LHC $L = 5 \times 10^{34}$		
CMS Phase I Upgr	300 fb^{-1}			CMS Phase II UPGRADE						CMS		3000 fb^{-1}		
Belle II		5 ab^{-1}	$L = 8 \times 10^{35}$		50 ab^{-1}									

- Improve the $\text{BF}(B_s \rightarrow \mu\mu)$ to constrain NP in $C_{10,S,P}$
- Measure $B^0 \rightarrow \mu\mu$ and test MFV in the BF ratio
 - If very lucky, could see evidence as early as 2019 (expect ~20 SM candidates after Run 2, ~60 together with Run 3)
- Determine the $A_{\Delta\Gamma}$ to probe the hidden New Physics effects in C_S and C_P
 - First discriminating $A_{\Delta\Gamma}$ measurement expected after Run 3 with ~35% rel. precision (~20%, <10% uncertainty after Run 4,5)

Other $B \rightarrow l^+ l^-$ modes

Other $B \rightarrow l^+ l^-$ modes

- $B_{(s)} \rightarrow e^+ e^-$ heavily helicity suppressed ($\sim 10^{-13}$) in the SM and experimentally difficult
- $B_{(s)} \rightarrow \tau^+ \tau^-$ challenging experimentally, but also affected the least by the helicity suppression:

- $BF_{SM}(B_s \rightarrow \tau^+ \tau^-) = 7.7(5) \times 10^{-7}$

Bobeth et al
[PRL 96:241802 (2014)]

- previous limit only for B^0

$$BF(B^0 \rightarrow \tau^+ \tau^-) < 4.1 \times 10^{-3} @ 90\%CL \quad \text{BaBar}$$

Aubert et al
[PRL 96:241802 (2006)]

- LFU tensions $R(D)$, $R(D^*)$ could imply a $O(10^3)$ boost (Z' , leptoquarks, 2HDM,...) Alonso et al
[1505.05164]

$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

[PRL 118, 251802 (2017)]

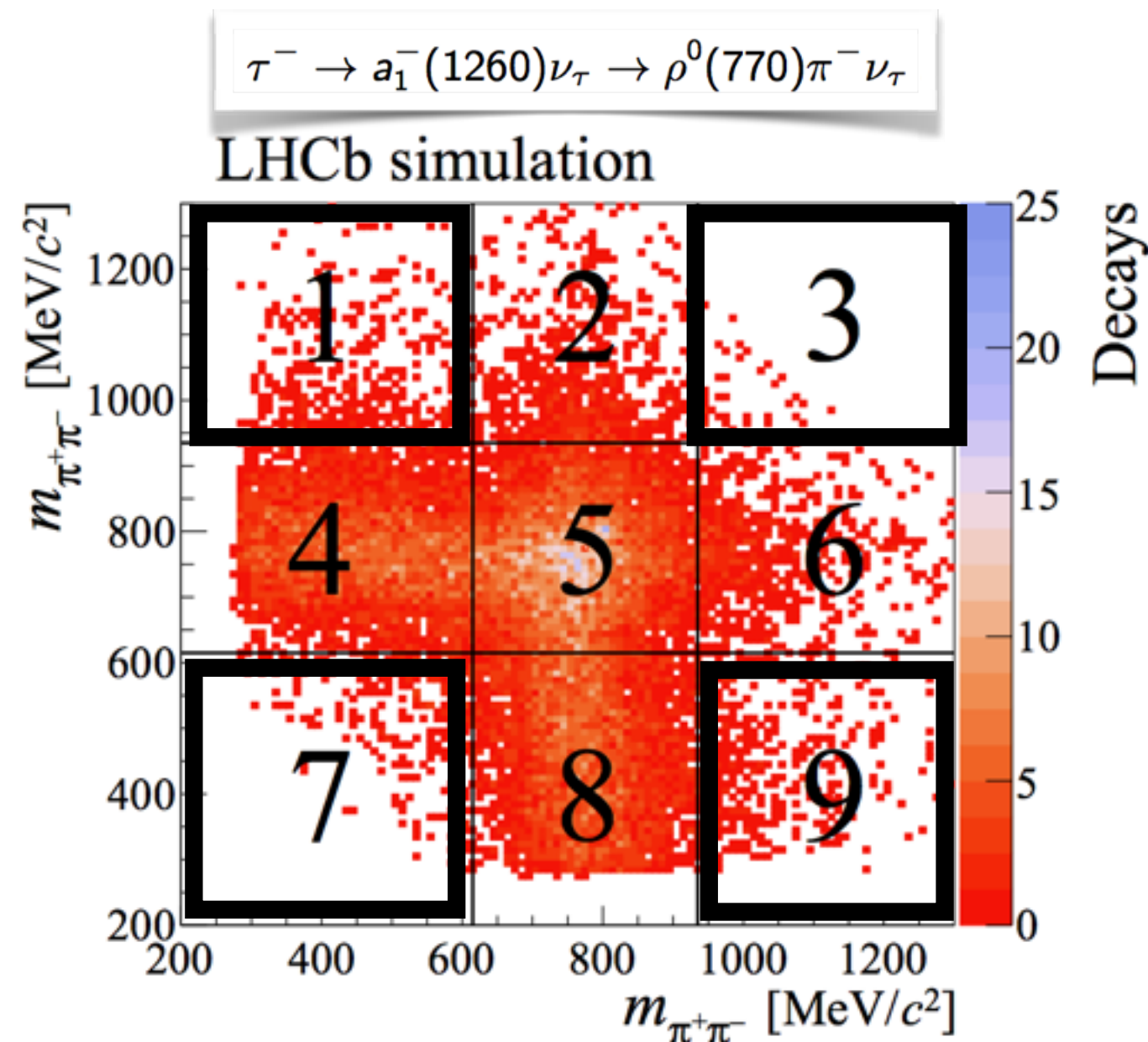
- LHCb analyses Run I data (3fb^{-1}) for the **hadronic τ -modes**: $\text{BF}(\tau \rightarrow \pi\pi\pi\nu) = 9.31(5)\%$
- Two final state neutrinos render B-mass useless for signal/background (and B^0/B_s) separation
- Instead use the intermediate $\rho^0(770) \rightarrow \pi^+ \pi^-$ resonance of the predominant decay chain:

$$\tau^- \rightarrow a_1^-(1260) \nu_\tau \rightarrow \rho^0(770) \pi^- \nu_\tau$$

$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

PRL 118, 251802 (2017)

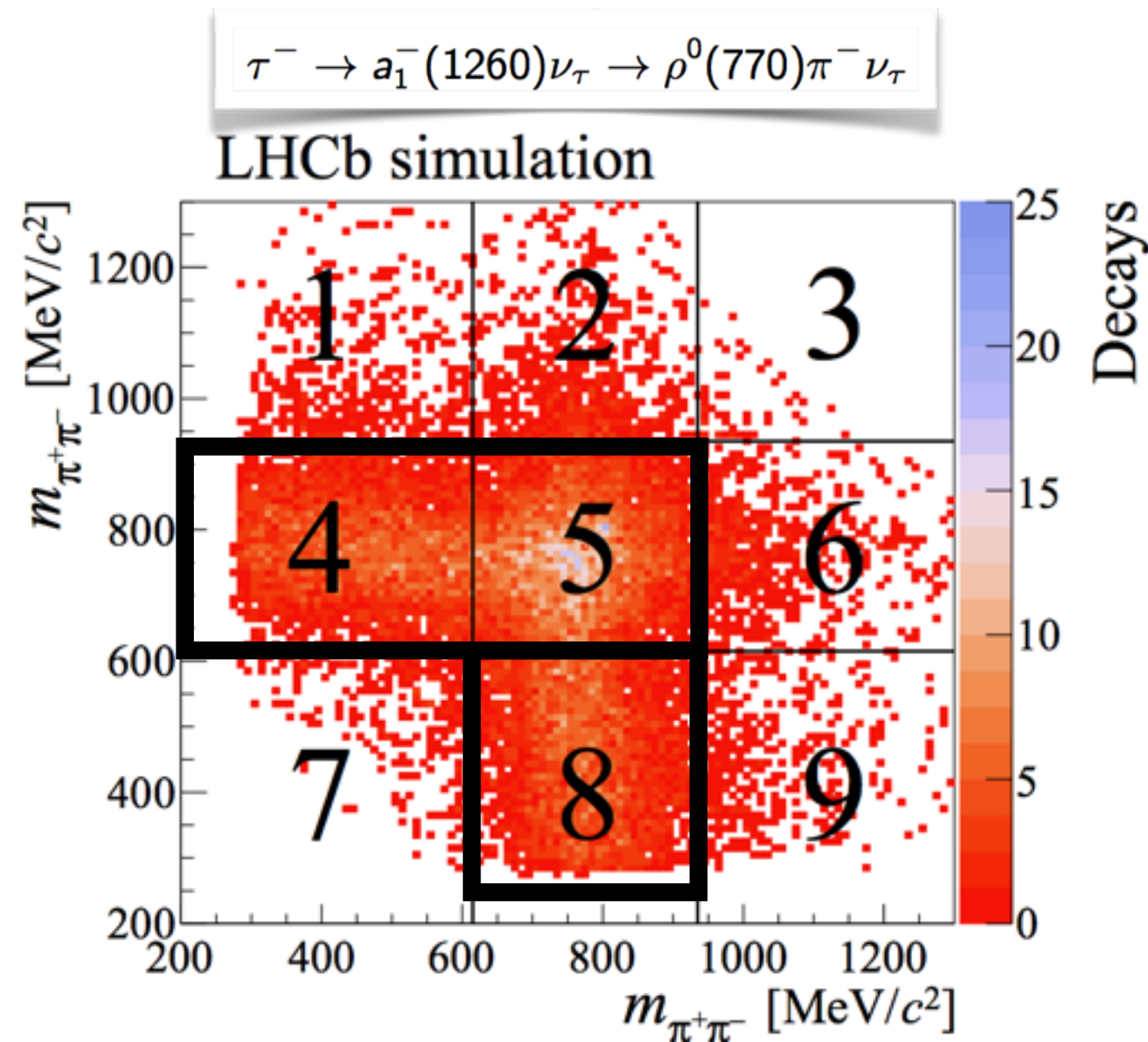
- Optimise the selection, train NN: one- τ in 1-3-7-9 (13% N_{Sig})
- Background model from: one- τ in 4-5-8 and other in one- τ 4-8 (58% N_{Sig})
- Signal region: both τ 's in 5 (16% N_{Sig})



$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

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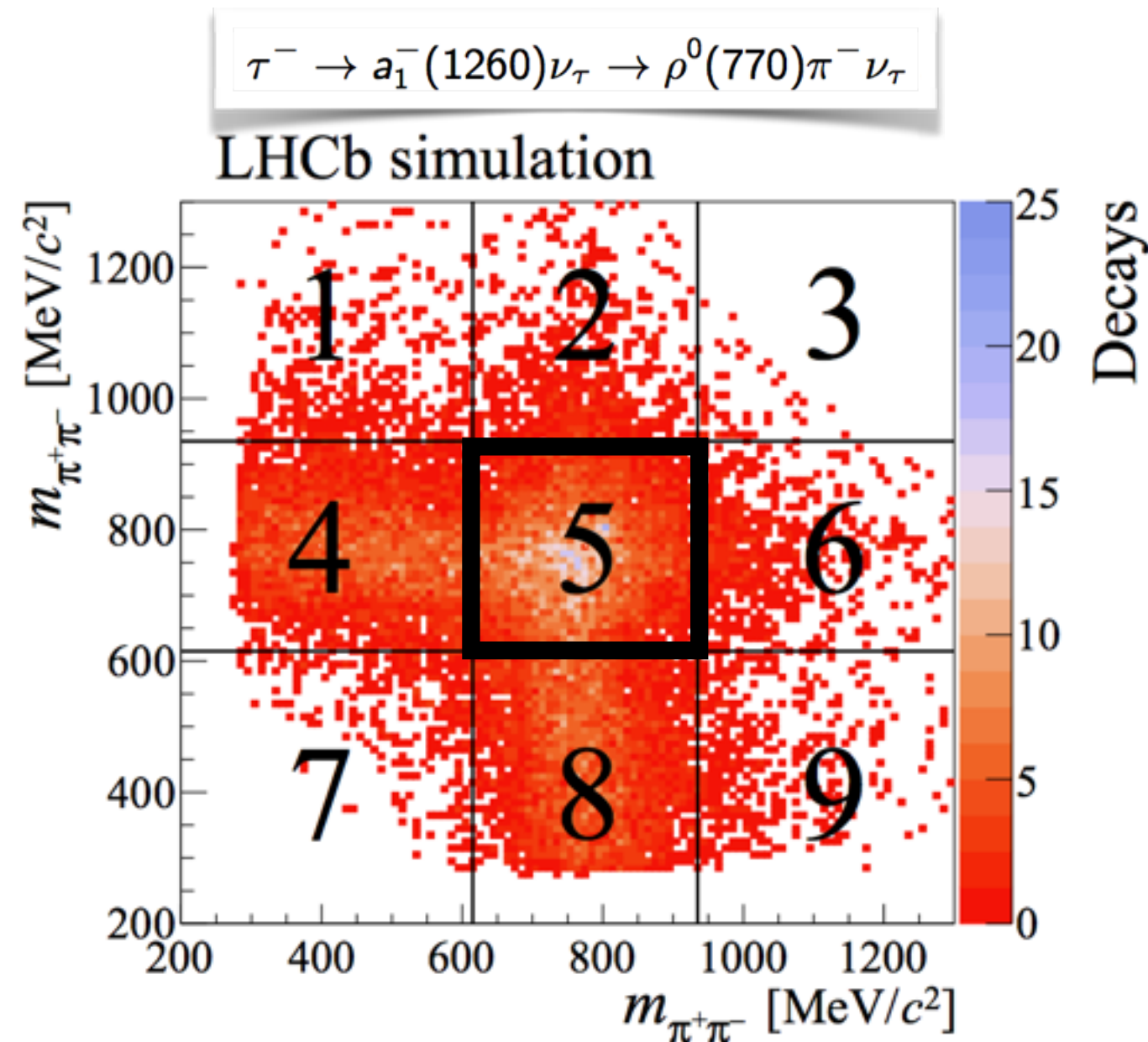
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PRL 118, 251802 (2017)

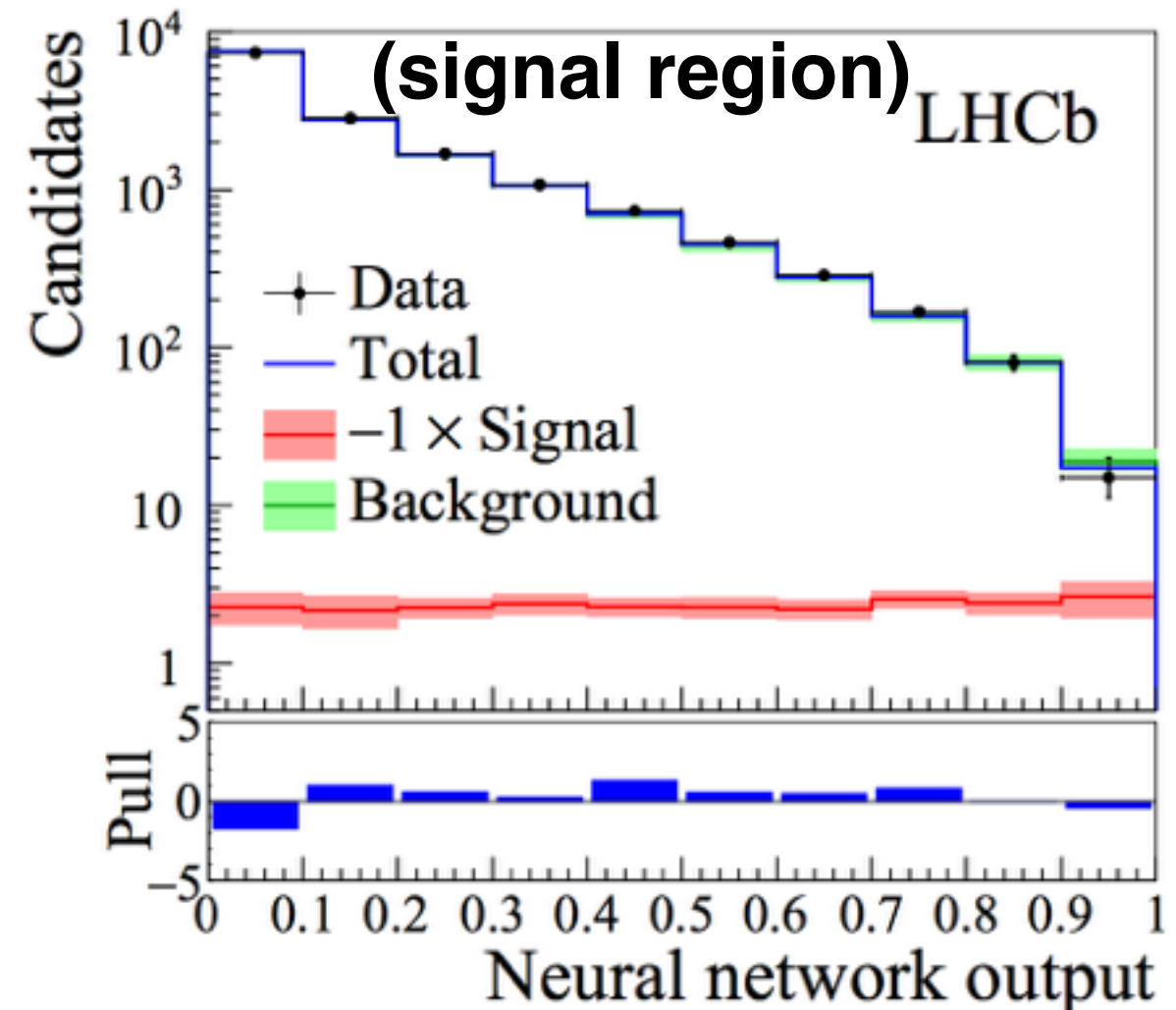
- Optimise the selection, train NN: one- τ in 1-3-7-9 (13% N_{Sig})
- Background model from: one- τ in 4-5-8 and other in one- τ 4-8 (58% N_{Sig})
- **Signal region: both τ 's in 5 (16% N_{Sig})**



$B_{(s)} \rightarrow \tau^+ \tau^-$ search in Run I data

PRL 118, 251802 (2017)

- The separate signal from the background using a neural-net
- 29 discriminating variables (geom., kin., iso., τ params.)
- Signal MC distributions calibrated on the normalisation modes
- Normalise the BF to $B_0 \rightarrow D^- D_s^+$ (where $D \rightarrow 3h$):



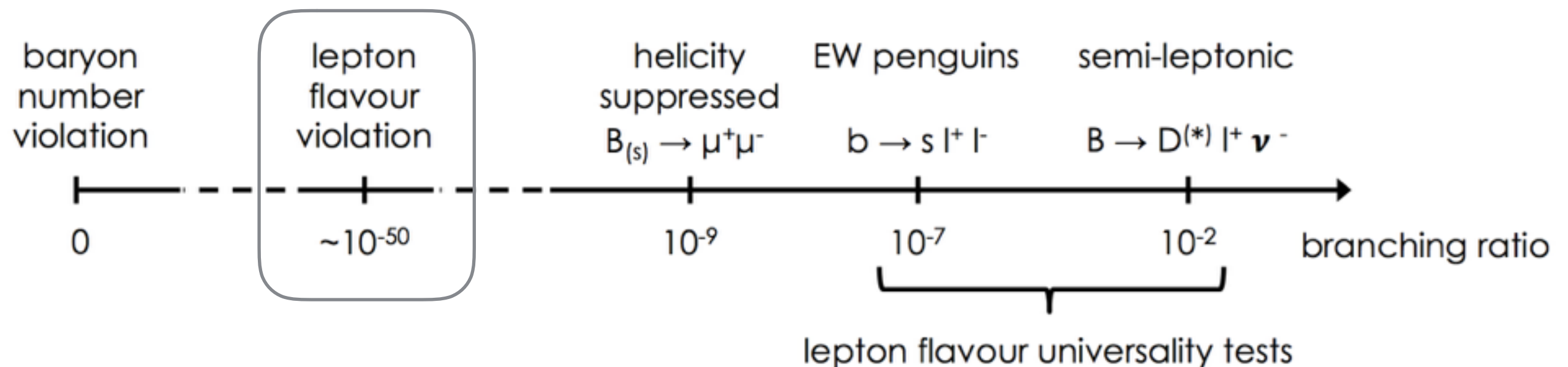
$$\mathcal{B}(B^0 \rightarrow \tau^+ \tau^-) < 2.1 \times 10^{-3} @ 95\%CL$$

$$\mathcal{B}(B_s \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3} @ 95\%CL$$

(assuming one or the other B mode) 38

PRL 118, 251802 (2017)

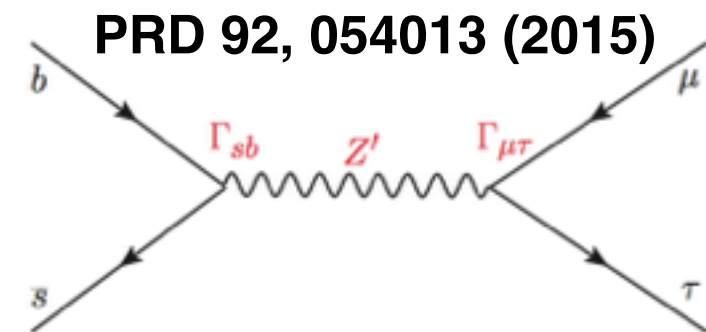
Leptonic B decays have more to offer..



Fully leptonic $B \rightarrow l_x^+ l_y^-$ decays are practically non-existent in the SM

Lepton flavour violation searches in LHCb

- Especially interesting in the light of the recent lepton non-universality hints: $R(K^{(*)})$, $R(D^{(*)})$.
- A large number of modes (SUSY, Z' , leptoquark, Pati-Salam,..) could enhance
 - $\text{BF}(B_{(s)} \rightarrow \tau^+ \mu^-) \sim \mathcal{O}(10^{-8})$ in generic Z'
 - $\text{BF}(B_{(s)} \rightarrow e^+ \mu^-) \sim \mathcal{O}(10^{-11})$
- Existing limits:
 - $\text{BF}(B^0 \rightarrow \tau^+ \mu^-) < 2.2 \times 10^{-5}$ @90% BaBar
 - $\text{BF}(B^0 \rightarrow e^+ \mu^-) < 3.7 \times 10^{-9}$ @95% LHCb 1 fb^{-1}
 - $\text{BF}(B_s \rightarrow e^+ \mu^-) < 1.4 \times 10^{-8}$ @95% LHCb 1 fb^{-1}



PRD 77, 091104 (2008)

PRL 111 (2013) 141801

New!

$B_{(s)} \rightarrow e^+ \mu^-$ search in Run I data

arXiv:1710.04111
submitted to JHEP

- Analyse full Run I sample (3fb^{-1}) with improved selection (esp. BDT)
- Similar to $B_{(s)} \rightarrow \mu^+ \mu^-$, yet more challenging
 - Bremsstrahlung correction to the e-momentum
- Selected $e^+ \mu^-$ candidates in $m_{e\mu} \in [4.9, 5.85] \text{GeV}/c^2$
 - contaminated by combinatorial background
 - sample split in two depending on the nr. of recovered photons: a) $e+0\gamma$ and b) $e+n\gamma$

New!

$B_{(s)} \rightarrow e^+ \mu^-$ search in Run I data

arXiv:1710.04111
submitted to JHEP

- The combinatorial is suppressed using a multivariate classifier (BDT):
 - trained on $B_{(s)} \rightarrow e^+ \mu^-$ MC and same sign $e^{+/-} \mu^{+/-}$ data
 - signal response calibrated on $B^0 \rightarrow K^+ \pi^-$ data (accounting for Bremsstrahlung)
- Simultaneous fit on 2x7 BDT bins. Model:
 - Signal+mis-identified bkg. ($B \rightarrow hh, B \rightarrow hlv$) +combinatorial bkg.
 - individual for both bremsstrahlung categories

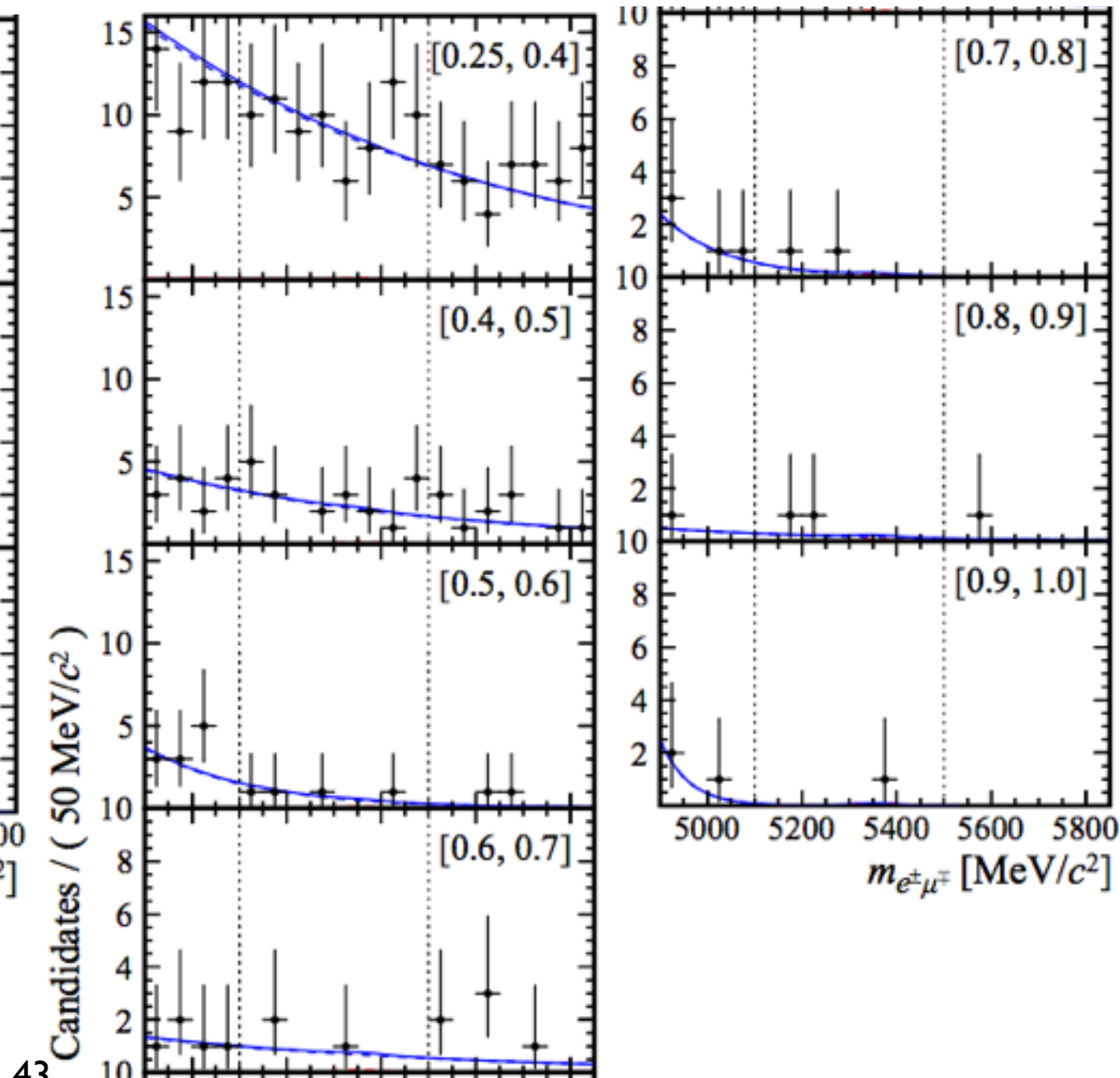
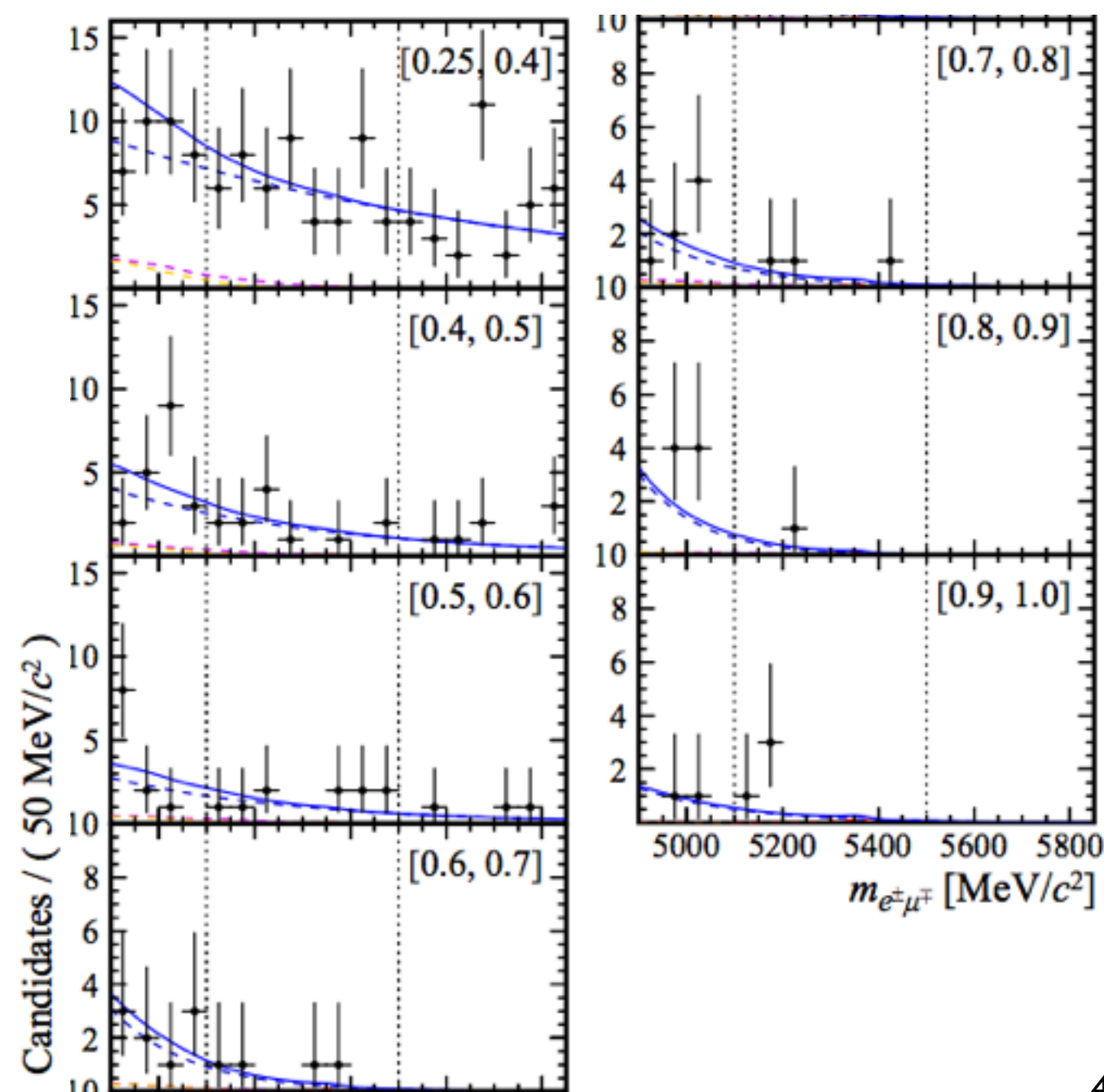
New!

No $B_{(s)} \rightarrow e^+ \mu^-$ signal in Run I data

arXiv:1710.04111
submitted to JHEP

- a) No Bremsstrahlung

- b) Bremsstrahlung



New!

$B_{(s)} \rightarrow e^+ \mu^-$ search in Run I data

arXiv:1710.04111
submitted to JHEP

- LHCb sets the most stringent limits up to date:

channel	expected	observed
$\mathcal{B}(B_s^0 \rightarrow e^\pm \mu^\mp)$	$3.9 (5.0) \times 10^{-9}$	$5.4 (6.3) \times 10^{-9}$
$\mathcal{B}(B^0 \rightarrow e^\pm \mu^\mp)$	$0.9 (1.2) \times 10^{-9}$	$1.0 (1.3) \times 10^{-9}$

- The limit on $B_s \rightarrow e^+ \mu^-$ is set assuming only B_{Heavy} decays (as in SM).
- B_{Light} : $\text{BF}(B_s \rightarrow e^+ \mu^-) < 6.0(7.2) \times 10^{-9} @ 90(95)\% \text{CL}$

Rare leptonic B-decays at the end of 2017

- B-decays have provided us with some of the most interesting puzzles in particle physics:
- global W. coefficient analysis show a coherent picture
- anomalies either in **vector (C_9)** OR in both **vector and axial-vector currents (C_9, C_{10})**

- Fully leptonic B-decays can **constrain the axial-vector contributions (C_{10})**
- SM like $\text{BF}(B_s \rightarrow \mu^+ \mu^-)$ excludes very large contributions to $C_{10,S,P}$, but **not yet precise enough to distinguish btw. $C_{10}^{\text{NP}} + C_9^{\text{NP}}$ and C_9^{NP} alone scenarios.**
- Only beginning to tap into $B_{(s)} \rightarrow \mu^+ \mu^-$
 - Effective $B_s \rightarrow \mu^+ \mu^-$ lifetime will help to expose/exclude $C_{S,P}$ contributions invisible to the BF alone (first LHCb results on Run I + Run 2 are out, $A_{\Delta\Gamma}$ accessible in Run 3)
 - $B_d \rightarrow \mu^+ \mu^-$ could enter the game soon (2019? but most likely in Run 3)

- In the light of the recent LFU tensions **other leptonic B modes are as important:**
 - LHCb sets best/first $B_{(s)} \rightarrow \tau^+ \tau^-$ limits on Run I data at $O(10^{-3})$
 - LHCb sets best $B_{(s)} \rightarrow e^+ \mu^-$ limits on Run I data at $O(10^{-9})$

Back-up

Historical success of the ‘effective’ approach

- The ‘effective’ model independent approach has historically played a crucial role in understanding the underlying theory from both direct and indirect measurements:
 - **1933**: First model for the weak decays. Similar coupling in the beta decay and muon decay suggested an **underlying structure (V-A)**
 - **1960’s**: Motivated **charm** prediction to make **GIM** work and explain missing FCNC.
 - **1970’s**: In predicting lower bounds on **Z** and **W** masses from muon lifetime (motivate SPS)
 - **2010’s**: **Lepton Flavour Universality Violation? Z’? Leptoquarks?**

$B \rightarrow \mu\mu$ future in numbers

Unofficial crude back-of-the-envelope Standard Model yield estimates based on the Run I performance:

Assuming SM and Run1 performance (raw est.)	Run1	+Run 2 (2019)	+Run3 (2024)	+Run4 (2030)	+Run 5 (assume 30% have good S/B)
Lumi (fb⁻¹)	3	5,3	15	15	250
N($B_s \rightarrow \mu^+\mu^-$)	35	155	0.5k	0.9k	2.7k
N($B_d \rightarrow \mu^+\mu^-$)	4	20	60	0.1k	0.3k
$\sigma_{\text{Relative}}(\text{BF}(B_s \rightarrow \mu^+\mu^-))$	40%	20%	15%	13%	~10%
$\sigma_{\text{Relative}}(A_{\Delta\Gamma})$	-	115%	35%	20%	<10%

Rare di-lepton modes

$$B_{(s)} \rightarrow \mu^+ \mu^-$$

[Phys. Rev. Lett. 112, 101801 (2014)]

with updated **top mass**

[<http://arxiv.org/abs/1403.4427>]

► Precise Standard Model predictions for individual modes:

$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-)^{<t><CP>} = 3.66 \pm 0.23 \times 10^{-9} \text{ (6.4\% unc.)}$$

$$\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-)^{<t><CP>} = 1.06 \pm 0.09 \times 10^{-10} \text{ (8.5\% unc.)}$$

$B_s^0 \rightarrow \mu^+ \mu^-$	f_{B_s}	CKM	τ_H^s	M_t	α_s	other param.	non-param.	Σ
	4.0%	4.3%	1.3%	1.6%	0.1%	< 0.1%	1.5%	6.4%
$B^0 \rightarrow \mu^+ \mu^-$	f_{B_d}	CKM	τ_H^s	M_t	α_s	other param.	non-param.	Σ
	4.5%	6.9%	0.5%	1.6%	0.1%	< 0.1%	1.5%	8.5%

► Even more precise Standard Model predictions for the ratio (MVF test):

$$\mathcal{R} = \frac{\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)}{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)} = \frac{\tau_{B_d}}{1/\Gamma_H^s} \left(\frac{f_{B_d}}{f_{B_s}} \right)^2 \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{M_{B_d} \sqrt{1 - \frac{4m_\mu^2}{M_{B_d}^2}}}{M_{B_s} \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}}} = 0.0295^{+0.0028(8.7\%)}_{-0.0025(7.7\%)}$$

Error budget of R:

- 8% from V_{td}/V_{ts}
- 3.7% from f_{B_d}/f_{B_s}
- 1.4% from B_s lifetime

- Top mass, Wilson coefficients, and V_{tb} cancel in theory predictions

- Experimental side: no need for the normalisation

Nature 522, 68-72 (04 June 2015)

Coefficients $\mathbf{C_{10}}$, $\mathbf{C_S}$ and $\mathbf{C_P}$ in fully leptonic B decays

$$B_{(s)} \rightarrow \mu^+ \mu^-$$

- ➡ Only $\mathbf{C_{10}}$ contributes in the Standard Model
- ➡ NP sensitivity in $\mathbf{C_S}$ and $\mathbf{C_P}$ is larger than in $\mathbf{C_{10}}$ (no helicity suppression)
($K^*\mu\mu$ sensitivity to C_S is lower than initially expected)

$$\frac{\text{BR}(B_q \rightarrow \ell^+ \ell^-)}{\text{BR}(B_q \rightarrow \ell^+ \ell^-)_{\text{SM}}} = \frac{|S|^2 \left(1 - \frac{4m_\ell^2}{m_{B_q}^2}\right) + |P|^2}{|C_{10}^{\text{SM}}|^2} \quad \begin{array}{l} \text{SM: } S=0 \\ \text{SM: } P=1 \end{array}$$

$$S = \frac{m_{B_q}^2}{2m_\ell} [(C_S)_q^\ell - (C'_S)_q^\ell] \quad P = [(C_{10})_q^\ell - (C'_{10})_q^\ell] + \frac{m_{B_q}^2}{2m_\ell} [(C_P)_q^\ell - (C'_P)_q^\ell]$$

- ➡ Very precise Standard Model predictions (limited by CKM and B decay constant):

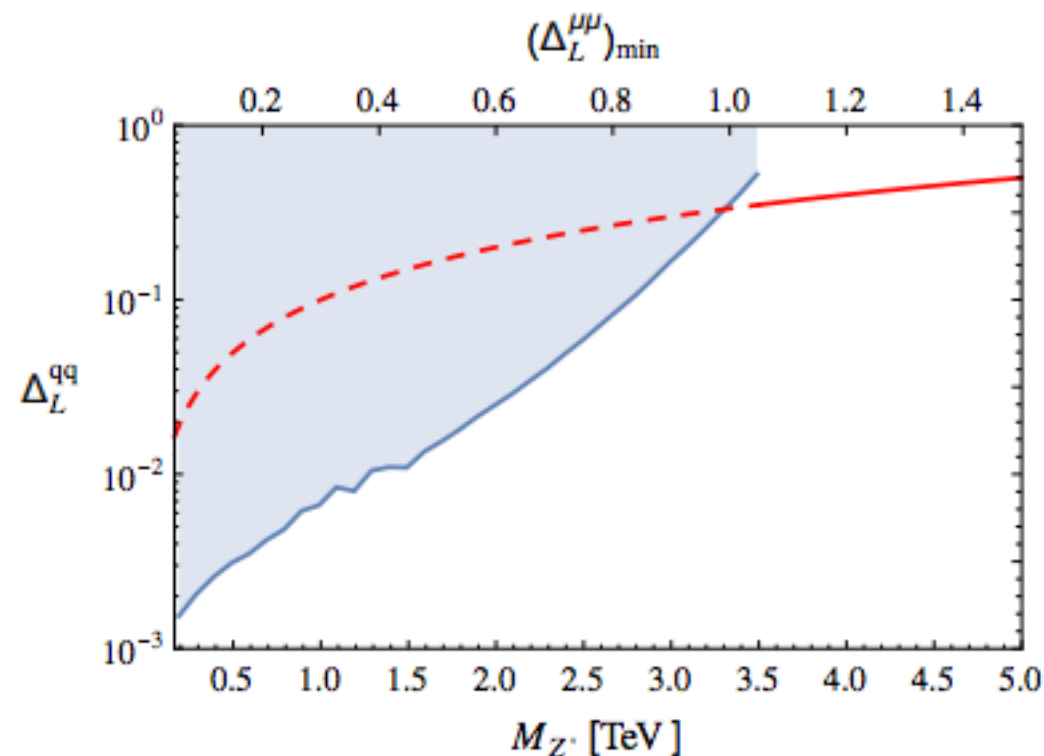
$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.59 \pm 0.18) \times 10^{-9}$$

Rel. Unc. from 6.4% -> 5%

Phys. Rev. Lett. 112, 101801 (2014)

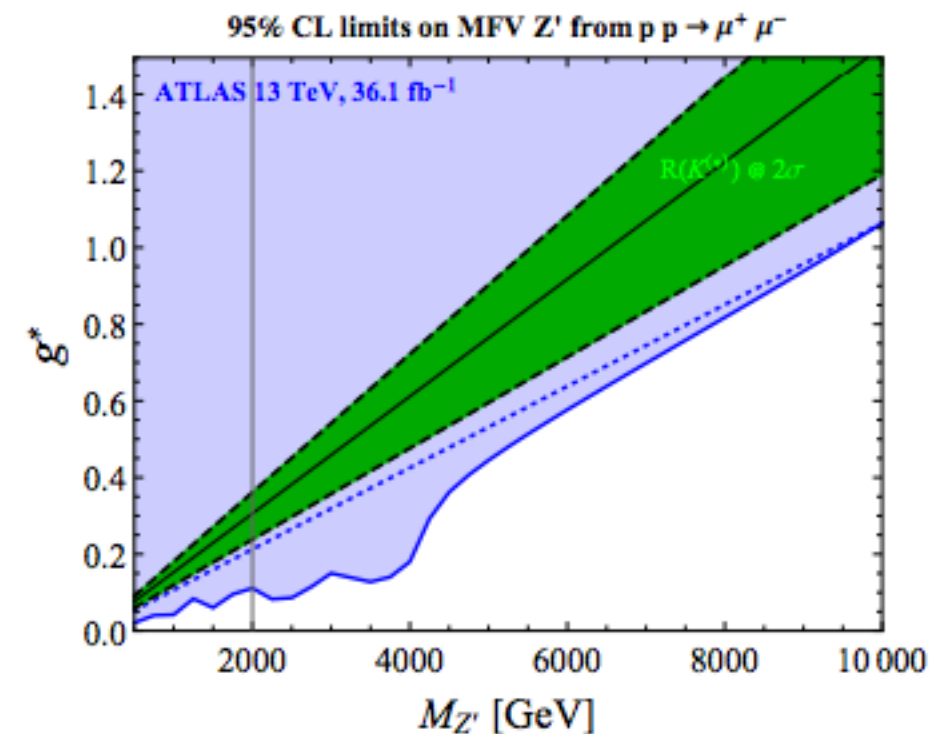
updated in arXiv:1702.05498

Dimuon constraints: two examples



Altmannshofer and Straub 1411.3161

- For $M_{Z'} \lesssim 3.5$ TeV, coupling to light quarks must be suppressed



Greljo and Marzocca 1704.09015

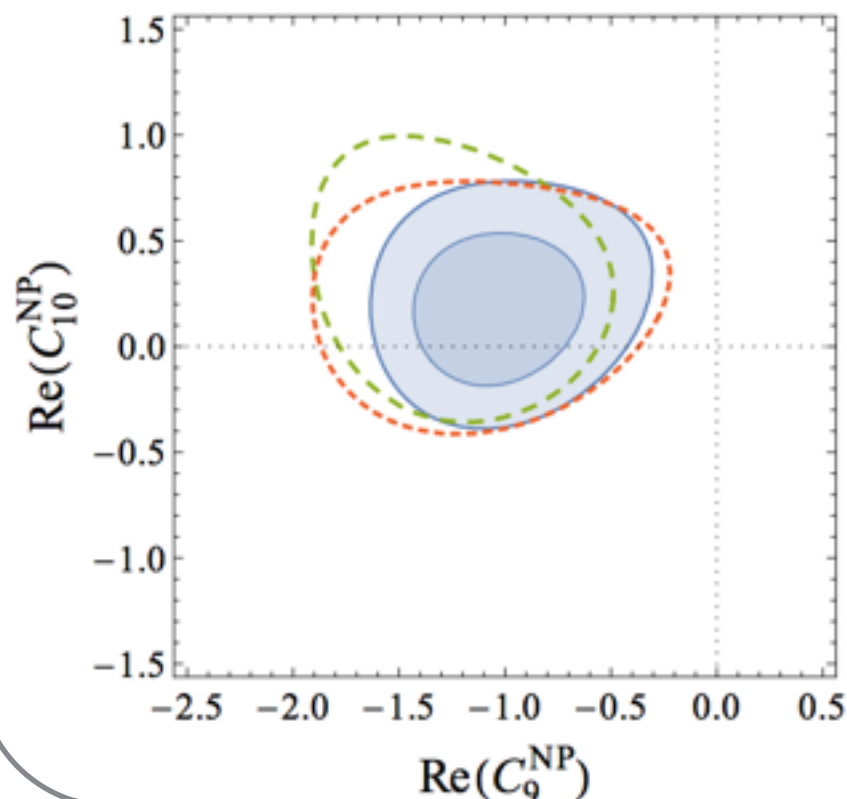
- MFV-like coupling to quarks is already excluded

Wilson coefficients are measured in **global $b \rightarrow sl^+l^-(\gamma)$ analysis**

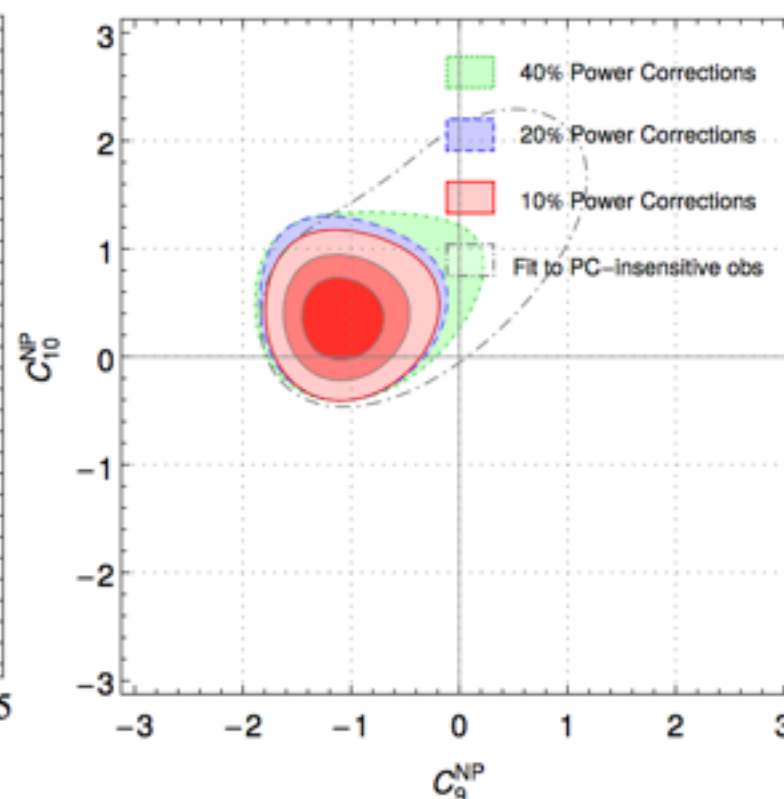
- ➡ No evidence for right-handed FCNC ($C'_i = 0$) and $C_{(7,9,10)}$ signs $[-, +, -]$ agree with the predictions (pre LHC discussion)
- ➡ There are tensions w.r.t SM (up to 4σ)
- ➡ Tensions are **driven** by **$B^0 \rightarrow K^* \mu^+ \mu^-$ angular observables** and by several **exclusive $b \rightarrow sl^+l^-$ branching fraction** measurements; supported by $R(K)$.
- ➡ **Tensions are relieved** by (NP effects?):

$$[(C_9)_s^\mu]^{NP} \approx -1.1 \quad \text{or} \quad [(C_9)_s^\mu]^{NP} = -[(C_{10})_s^\mu]^{NP} \approx -0.5$$

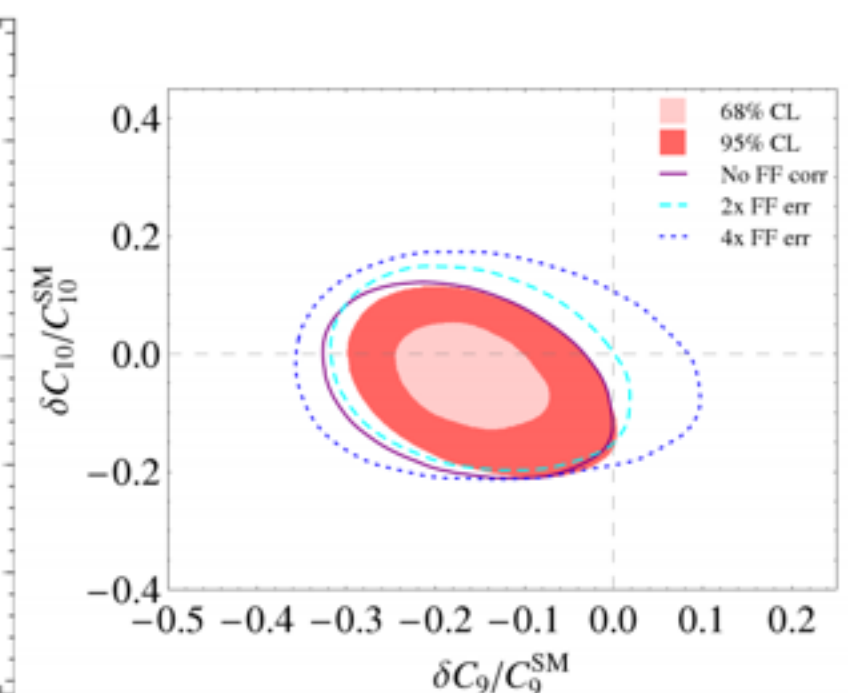
Altmannshofer, Straub
[Eur.Phys.J.C75(8)(2015)382]



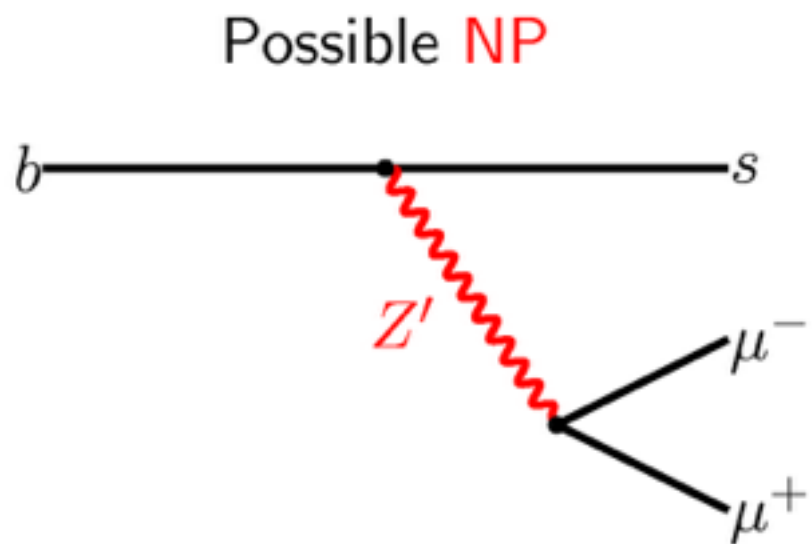
Descotes-Genon, Hofer, Matias, Virto [JHEP 06 (2016) 092]



Hurth, Mahmoudi, Neshatpour
[arXiv:1603.00865]

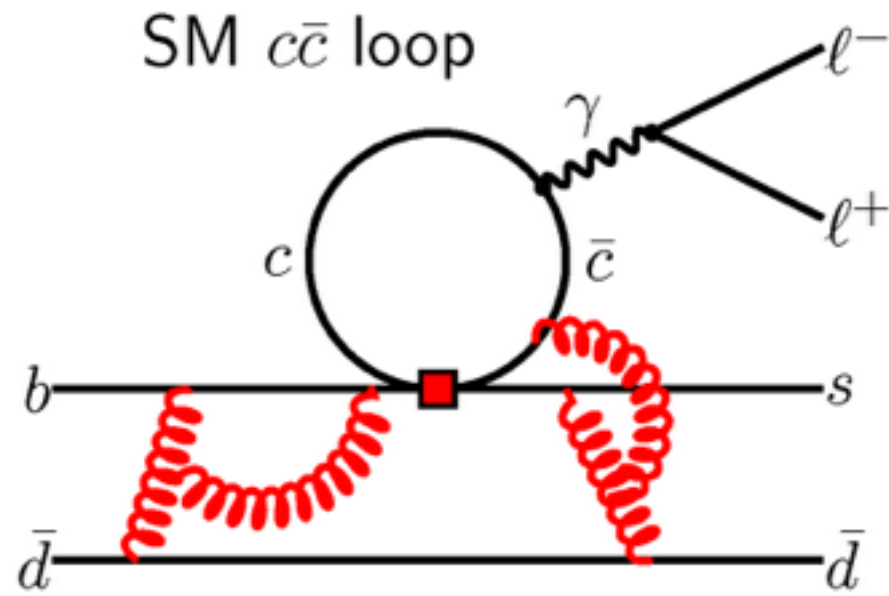


Z', leptoquarks,...



$$C_9 + C_9^{NP}$$

Hadronic SM effects



$$C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{res}(q^2)$$

Large long-distance charm resonance effects far from the resonances on the q^2 plane.

NEW!

➡ Measure the resonance effects in **C₉** in an inclusive analysis:

$$B^+ \rightarrow K^+ \mu^+ \mu^- + B^+ \rightarrow K^+ X_{c\bar{c}} (\rightarrow \mu^+ \mu^-)$$

Excellent review:
[\[arXiv:1606.00916\]](https://arxiv.org/abs/1606.00916)



$B^+ \rightarrow K^+ \mu^+ \mu^-$

➡ The differential decay rate depends on the Wilson coefficients:

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 \alpha^2 |V_{tb} V_{ts}^*|^2}{128 \pi^5} |\mathbf{k}| \beta \left\{ \frac{2}{3} |\mathbf{k}|^2 \beta^2 |C_{10} f_+(q^2)|^2 + \frac{4 m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} |C_{10} f_0(q^2)|^2 \right. \\ \left. + |\mathbf{k}|^2 \left[1 - \frac{1}{3} \beta^2 \right] \left| C_9 f_+(q^2) + 2 C_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\},$$

fix C_7 to the SM value (small)

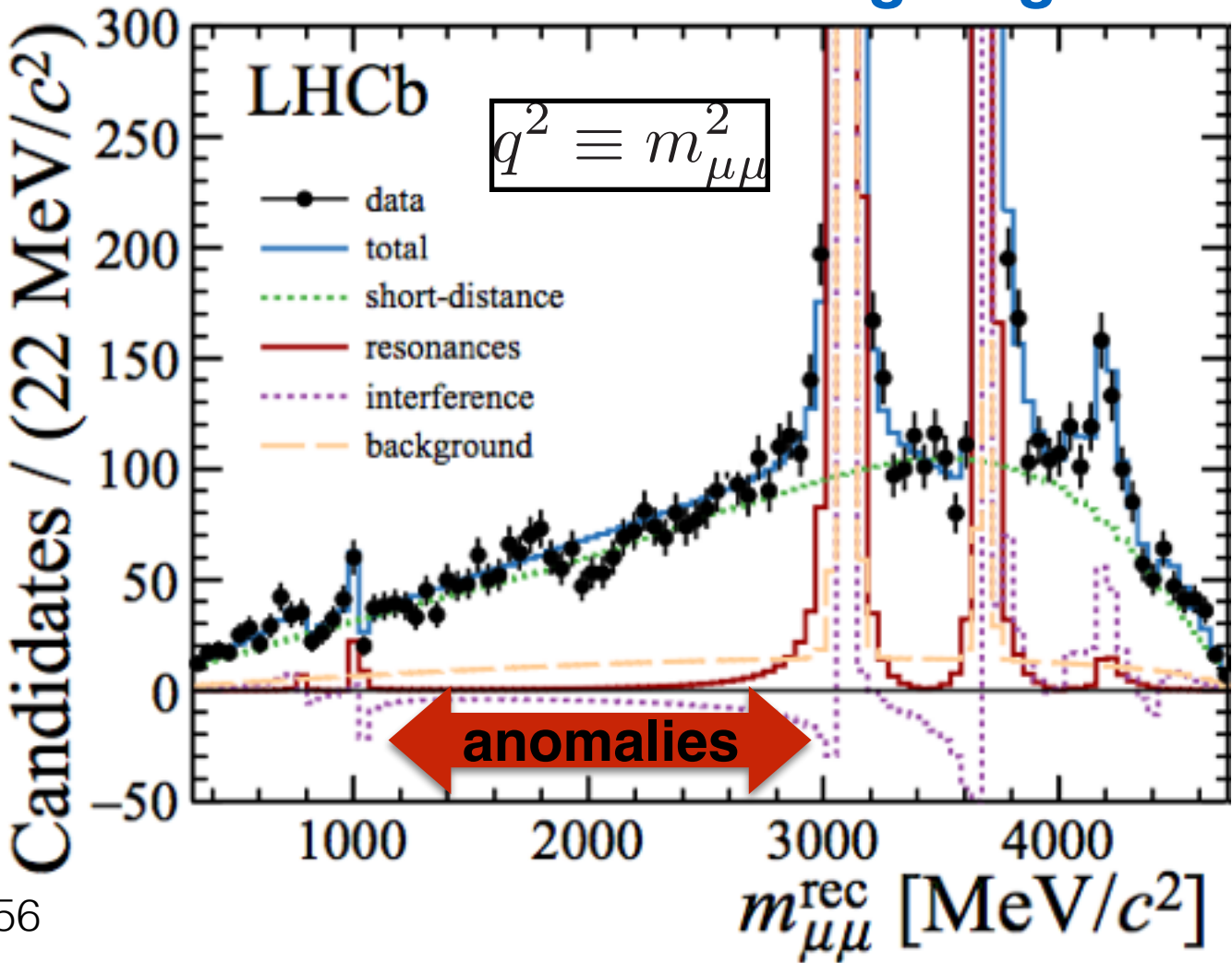
Phase: **neg. neg.**

➡ Parametrise resonance effects:

$$C_9^{\text{eff}} = C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{\text{res}}(q^2)$$

relative Breit-Wigner/
phase to C_9 Flatté $\Phi(3770)$

Resonance	$\psi(2S)$
$\rho(770)$	$\psi(3770)$
$\omega(782)$	$\psi(4040)$
$\phi(1020)$	$\psi(4160)$
J/ψ	$\psi(4415)$





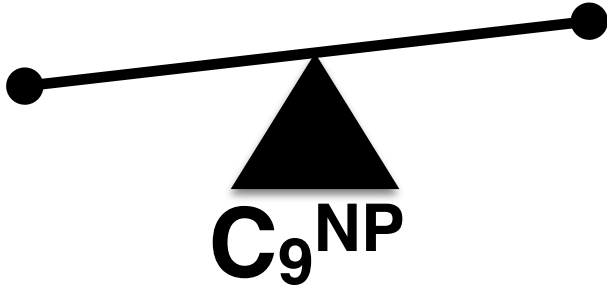
$$B^+ \rightarrow K^+ \mu^+ \mu^-$$

➡ The **short-distance branching fraction** agrees with the previous (exclusive) result:

$$B(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.29 \pm 0.07 \text{ (stat)} \pm 0.21 \text{ (syst)}) \times 10^{-7} \text{ old}$$

$$B(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.37 \pm 0.15 \text{ (stat)} \pm 0.23 \text{ (syst)}) \times 10^{-7} \text{ new}$$

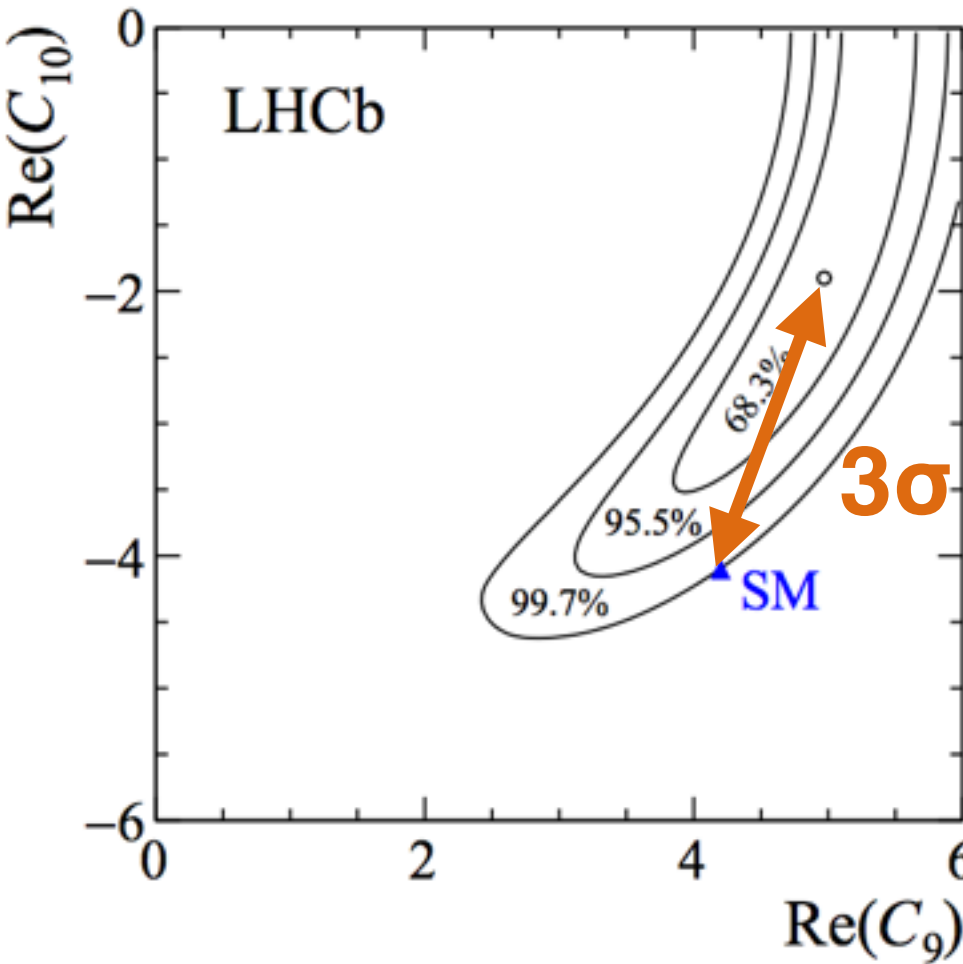
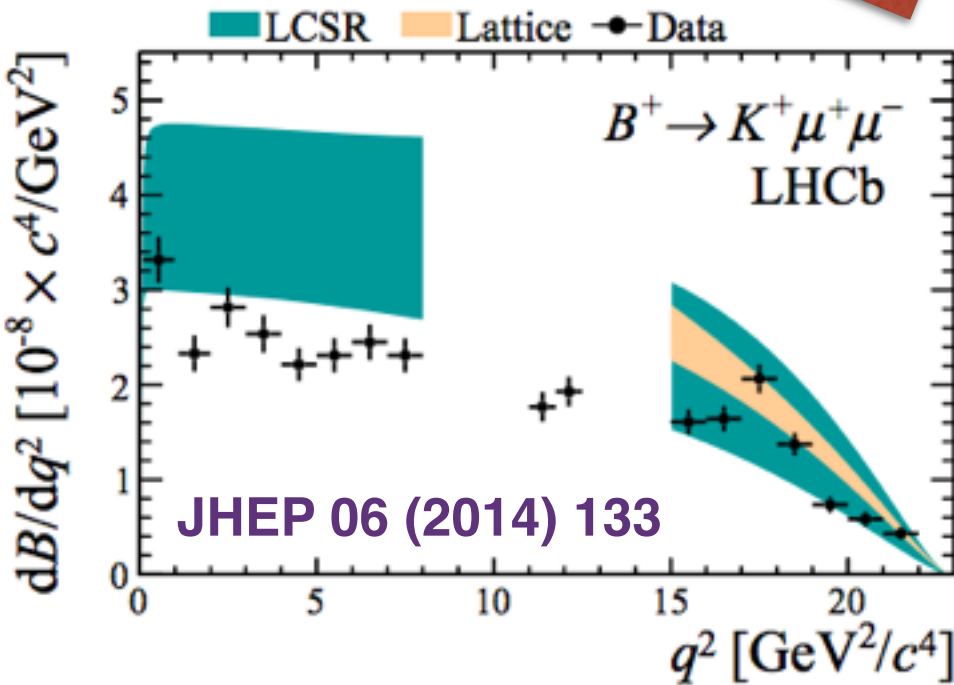
➡ 1D ($C_9, C_{10} = \text{SM}$) fit:
 $C_9 < \text{SM}$ (as the global fits)



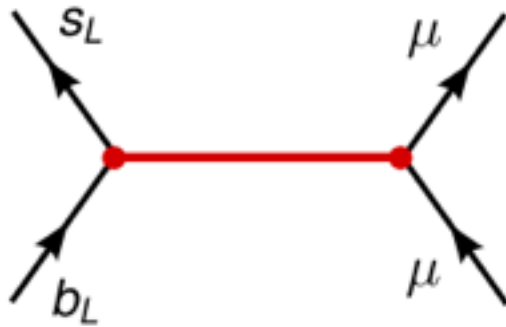
➡ 2D (C_9, C_{10}) fit:
 $C_9 > \text{SM}$ $C_{10} < \text{SM}$
(as [JHEP06(2015)115])

➡ The main conclusion: contributions from J/ψ and $\psi(2S)$ are contained around their (narrow) resonances.

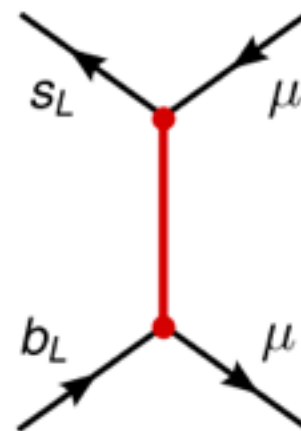
➡ Inclusive $B^0 \rightarrow K^* \mu^+ \mu^-$ analysis will follow



Possible New Physics

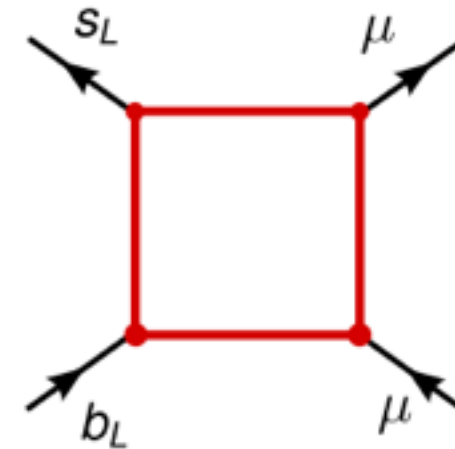


- Z'
- $SU(2)_L$ singlet or triplet



- Leptoquark
- Spin 0 or 1

Talk by I. Nisandzic, B. Grinstein



- New scalars/vectors, also leptoquarks possible